

# ExoPAG SAG13: Exoplanet Occurrence Rates and Distributions

Ruslan Belikov  
on behalf of SAG13

Note: some results in this presentation are still  
preliminary



# SAG13 members

Belikov, Ruslan (Chair, [rulsan.belikov@nasa.gov](mailto:rulsan.belikov@nasa.gov))

Stark, Christopher (Co-chair)

Batalha, Natalie (Steering Committee)

Burke, Chris (Steering Committee)

Angerhausen, Daniel

Apai, Daniel

Bendek, Eduardo

Bennett, David

Blackwood, Gary

Boss, Alan

Brown, Robert

Bryden, Geoff

Bryson, Stephen

Cahoy, Kerri

Catanzarite, Joe

Ciardi, David

Clanton, Christian

Cowan, Nick

Danchi, William

Domagal-Goldman, Shawn

Dressing, Courtney

Farr, Will

Foreman-Mackey, Daniel

Fressin, Francois

Gaudi, Scott

Ge, Jian

Gould, Andy

Hogg, David W

Howard, Andrew

Kane, Stephen

Kasting, Jim

Kopparapu, Ravi

Macintosh, Bruce

Mandell, Avi

Mendez, Abel

Meyer, Michael

Morgan, Rhonda

Mulders, Gijs

Nielsen, Eric

Petigura, Erik

Ragozzine, Darin

Roberge, Aki

Rogers, Leslie

Savransky, Dmitry

Serabyn, Gene

Shabram, Megan

Shao, Mike

Solmaz, Arif

Sparks, William

Stahl, Philip

Stapelfeldt, Karl

Still, Martin

Suzuki, Daisuke

Swain, Mark

Traub, Wes

Turnbull, Margaret

Unwin, Stephen

Vanderbei, Bob

Walkowicz, Luzianne

Weiss, Lauren M.

Wolfgang, Angie

Youdin, Andrew

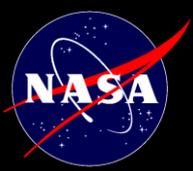


# Charter

Over 5000 exoplanets and exoplanet candidates have been discovered to date. Many studies have been published and are on-going to determine exoplanet occurrence rates and distributions, particularly for potentially habitable worlds. These studies employ different statistical and debiasing methods, different definitions of terms such as  $\eta_{\text{Earth}}$  and habitable zone, different degrees of extrapolation, and present distributions in different units from each other. The primary goal of this SAG is to evaluate what we currently know about planet occurrence rates, and especially  $\eta_{\text{Earth}}$ , by consolidating, comparing, and reconciling discrepancies between different studies. A secondary goal is to establish a standard set of occurrence rates accepted by as much of our community as possible to be used for mission yield estimates for missions to be considered by the decadal survey.

## Key objectives and questions:

- Completed → 1. Propose standard nominal conventions, definitions, and units for occurrence rates/distributions to facilitate comparisons between different studies.
- Current activity → 2. Do occurrence estimates from different teams/methods agree with each other to within statistical uncertainty? If not, why?
- Current activity → 3. For occurrence rates where extrapolation is still necessary, what values should the community adopt as standard conventions for mission yield estimates?



# SAG13 role



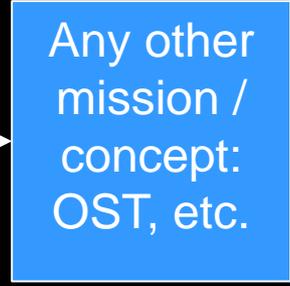
- Planet occurrence rates from individual teams
- Consensus on conventions / definitions
- Conversions between parameters (e.g. mass and radius)
- General feedback and endorsement of SAG13 products



- Survey and meta-analysis of occurrence rates
- Parametrized distributions for mission yield calculations

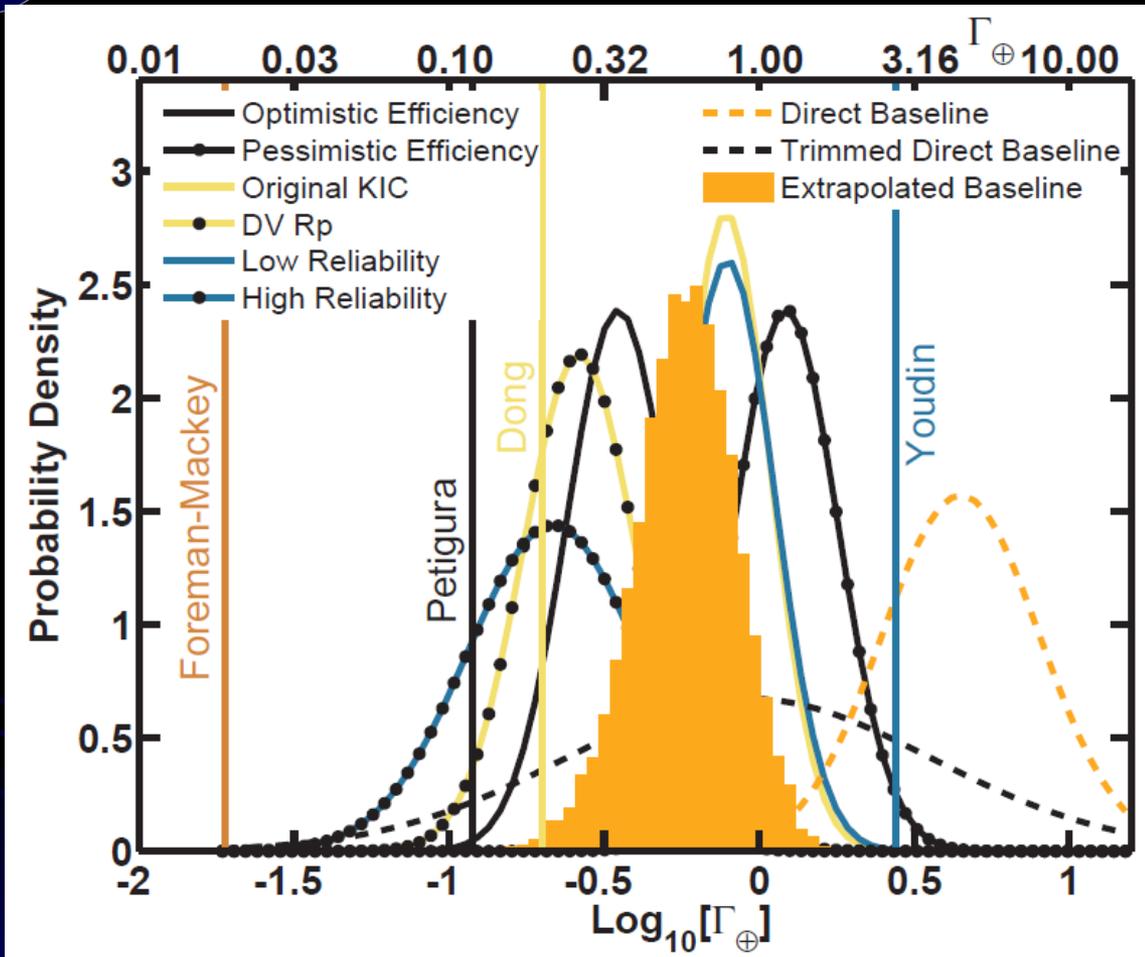


- mission yield code w/ standardized assumptions
- Mission yields





# From Burke et al. 2015

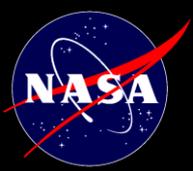


$$\Gamma_{\text{earth}} = \left. \frac{\partial^2 N(R,P)}{\partial \ln R \partial \ln P} \right|_{R=1, P=1y}$$

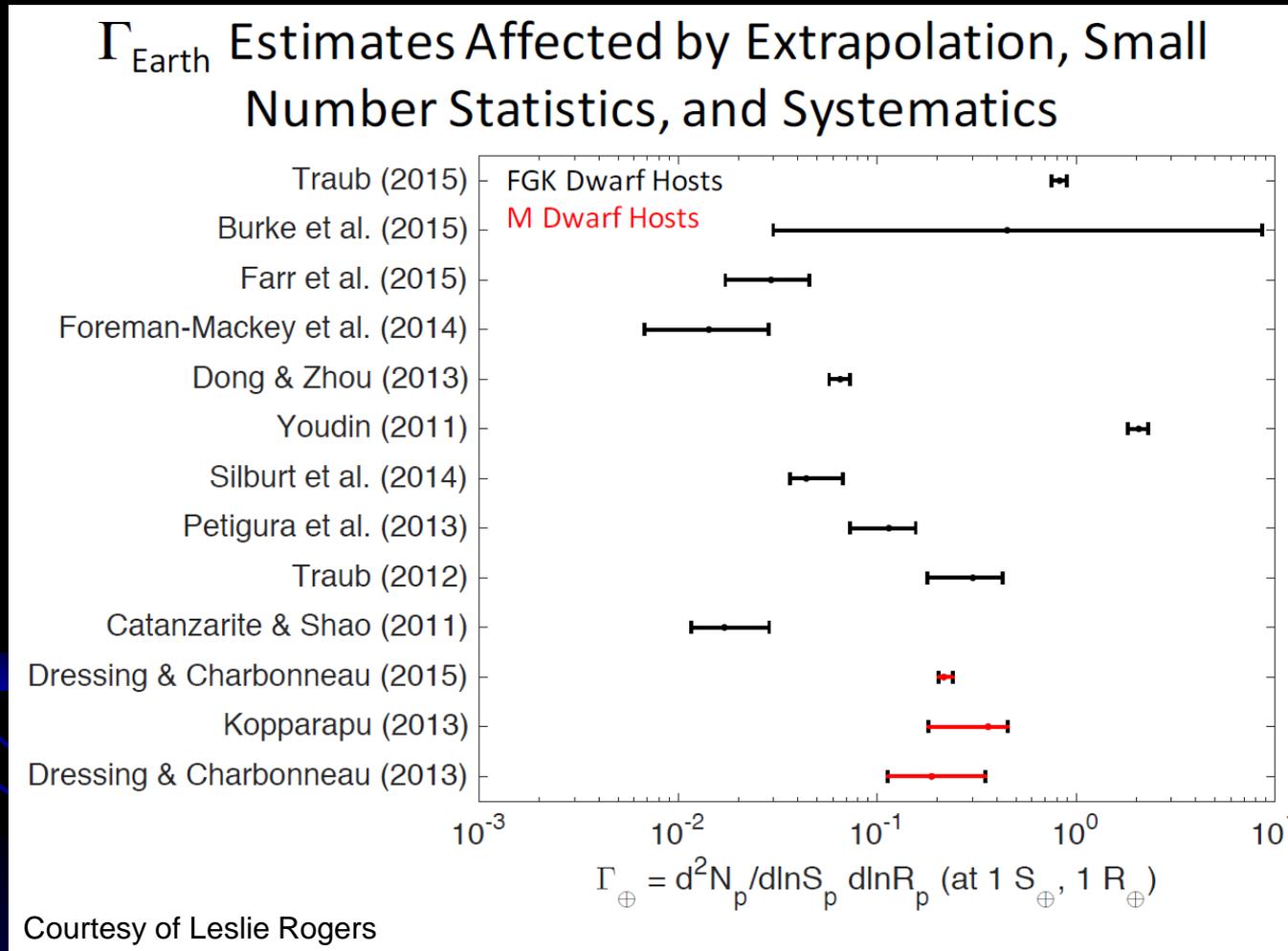
$\Gamma_{\text{earth}}$  is independent of definitions of HZ or habitable size range

For most definitions of  $\eta_{\text{Earth}}$ ,  $\Gamma_{\text{earth}} \sim \eta_{\text{Earth}}$

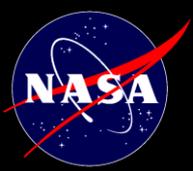
“We generally find higher planet occurrence rates and a steeper increase in planet occurrence rates towards small planets than previous studies of the Kepler GK dwarf sample”



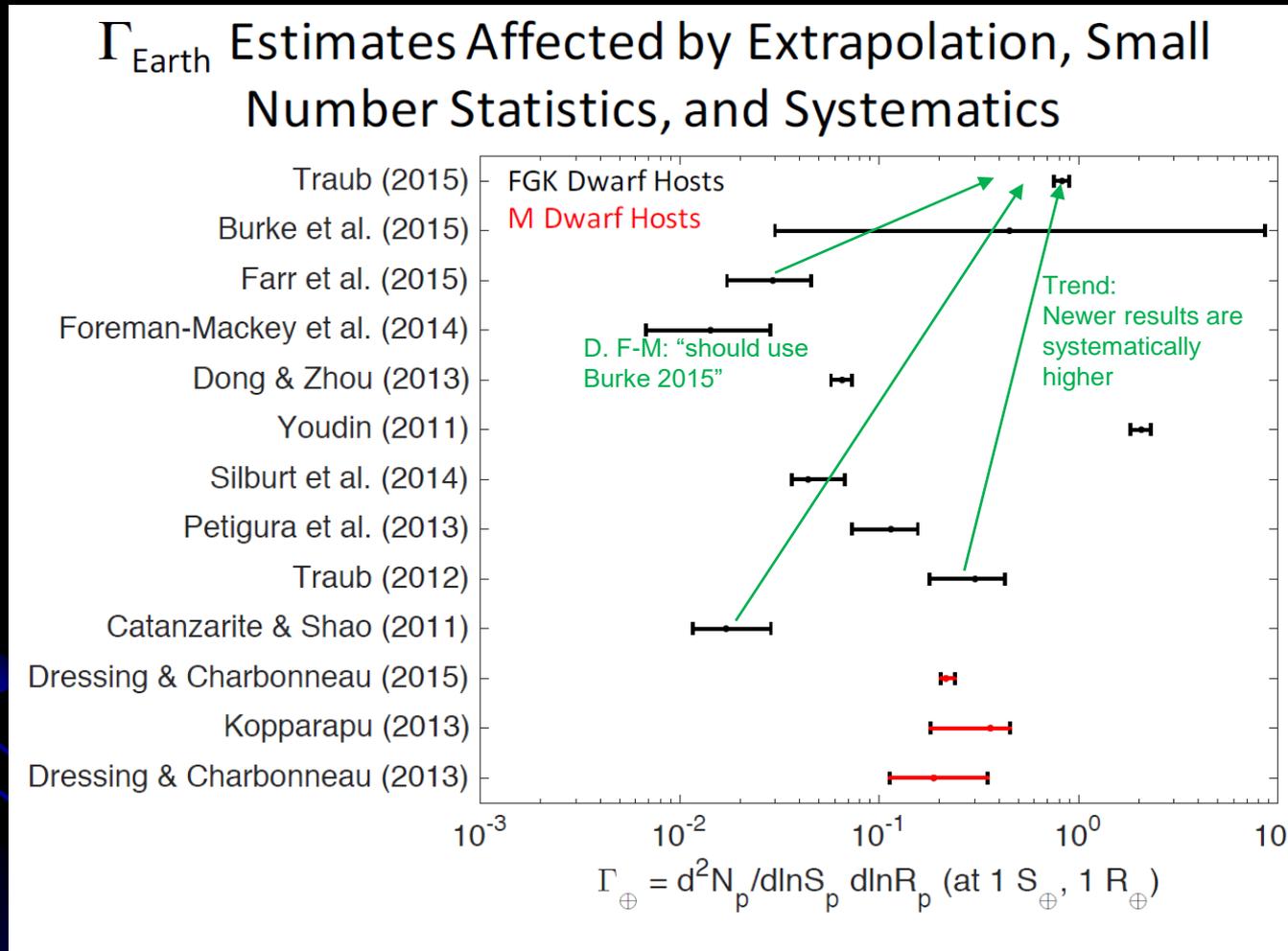
# Comparison of $\Gamma_{\text{earth}}$ from different publications



- Initially, it appears that the possible range of  $\Gamma_{\text{earth}}$  spans 2-3 orders of magnitude
- This is true, but extremely conservative: only the middle ~couple of octaves are “likely”



# Comparison of $\Gamma_{\text{earth}}$ from different publications

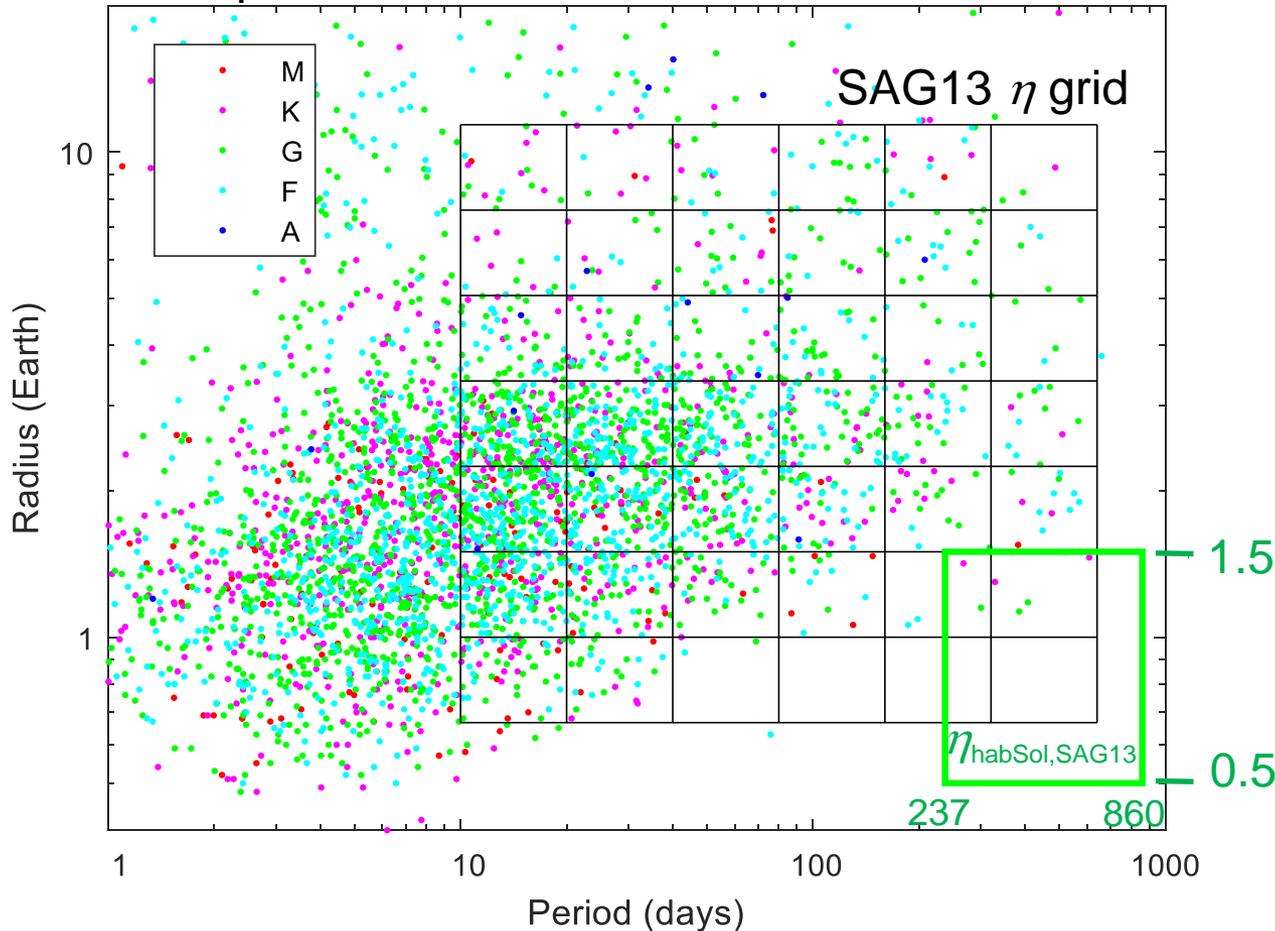


- Initially, it appears that the possible range of  $\Gamma_{\text{earth}}$  spans 2-3 orders of magnitude
- This is true, but extremely conservative: only the middle ~couple of octaves are “likely”



# Standardized eta grid

Kepler candidates from Q1-Q17, dr24



12 community sourced occurrence tables

Batalha, Natalie (2)

Belikov, Rus

Burke, Chris

Catanzarite, Joe

Dressing, Courtney\*

Farr, Will

Foreman-Mackey, Daniel\*

Kopparapu, Ravi

Mulders, Gijs

Petigura, Erik\*

Traub, Wes\*

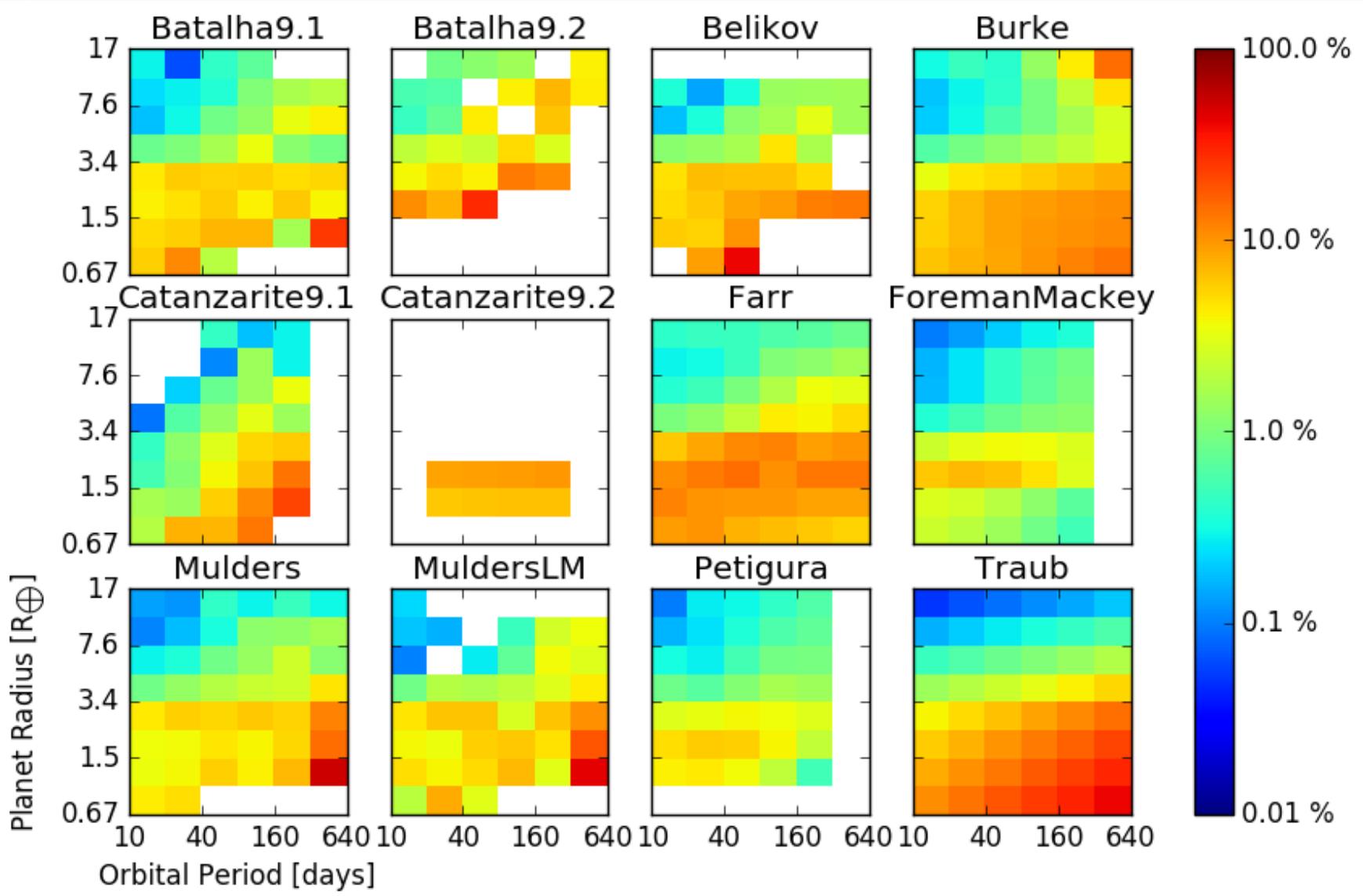
\*dataset was based on prior publications and re-integrated across SAG13 bins by Burke

All datasets and documents can be found on SAG13 repository:  
<https://drive.google.com/drive/folders/0B520NCfkP4aOQUJYdmUzQTJkdkE>

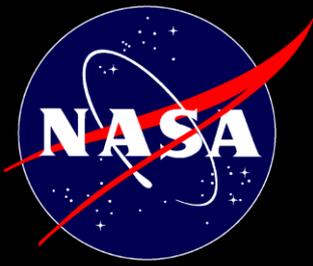
## • $\eta_{\text{habSol,SAG13}}$

- $R = [0.5 - 1.5]$ ,  $P = [237 - 860]$  (Kopparapu optimistic HZ for Sol twin)
- This is not exactly  $\eta_{\text{Earth}}$ , just a tentative rough representation of a potentially habitable region

# NASA Example: submitted occurrence rates for G-dwarfs



Plots and analysis are generated with the make\_plots.py script in the SAG13 Google drive, code by Gijs Mulders.

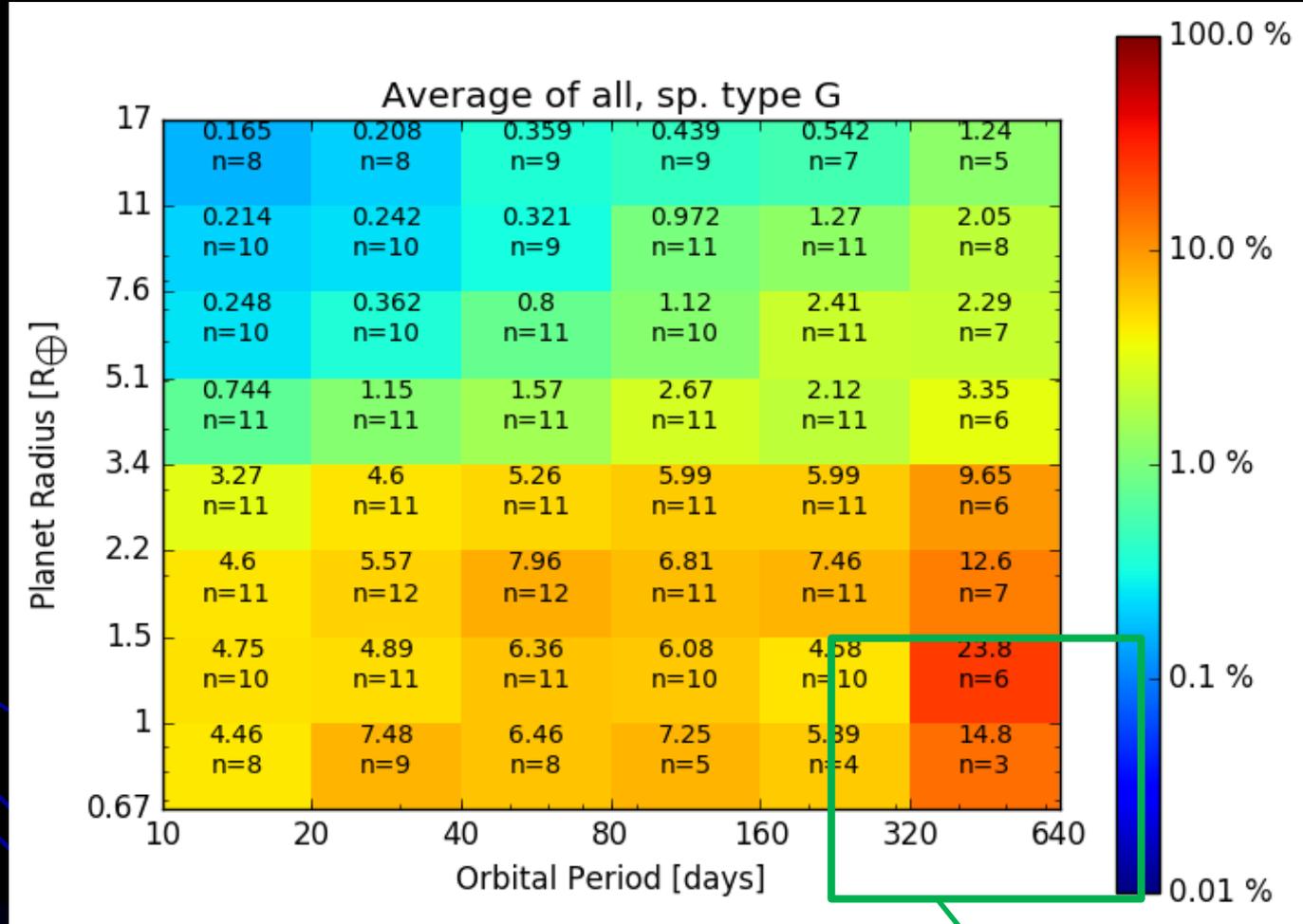


# Closer look at G-dwarf average

## legend

% occurrence

# of submissions



Note: this is a simple average across submissions  
 More sophisticated combination methods are being explored, such as weighting by quoted uncertainties and/or accounting for dependencies

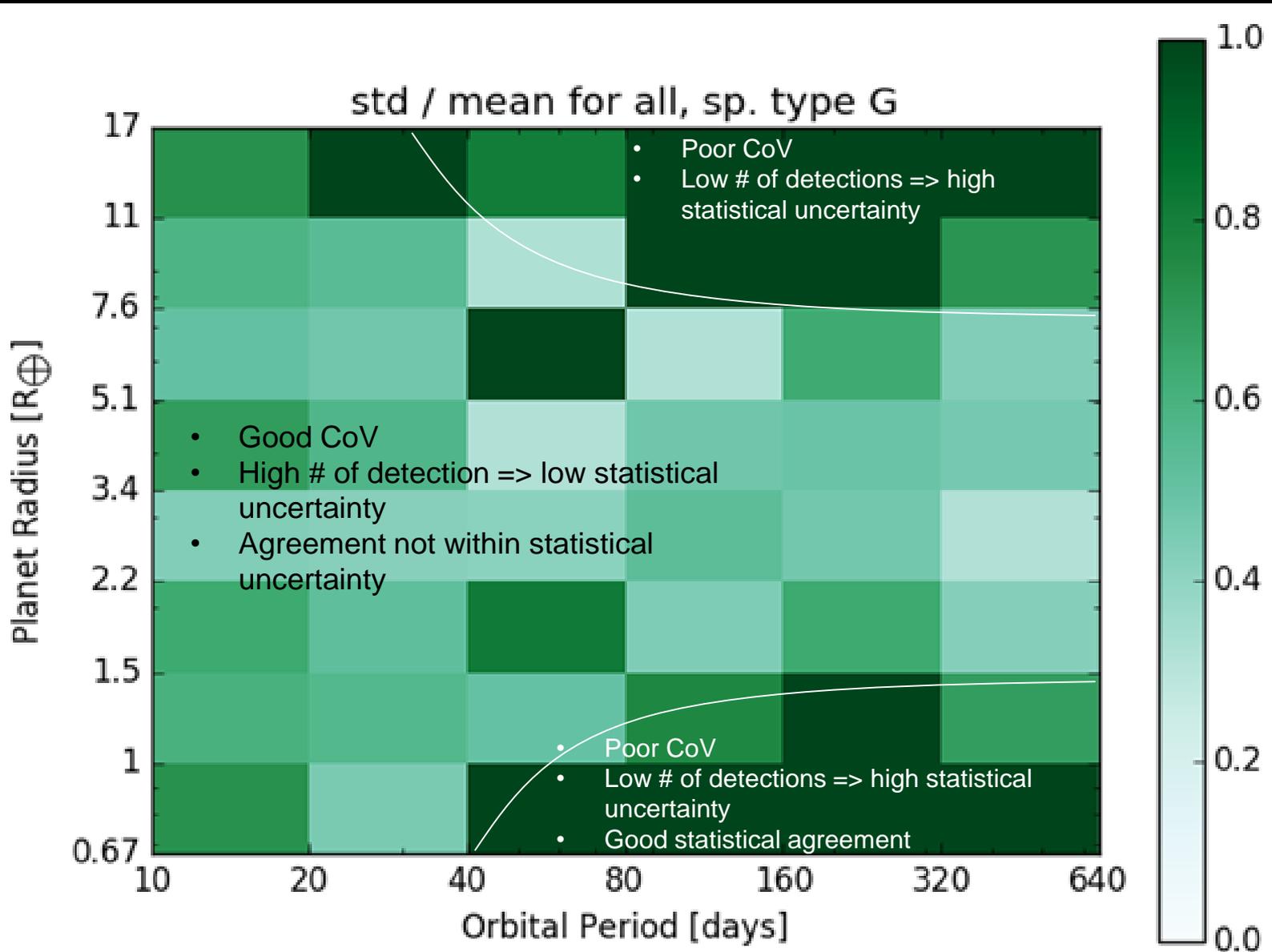
$\eta_{\text{habSol,SAG13}} \sim 0.58$   
 (based on best power law fit)

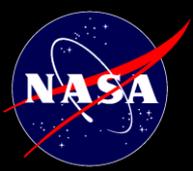
Plots and analysis are generated with the make\_plots.py script  
 in the SAG13 Google drive, code by Gijs Mulders.



# Coefficient of Variation

(aka relative standard deviation =  $\text{std} / \text{mean}$ )

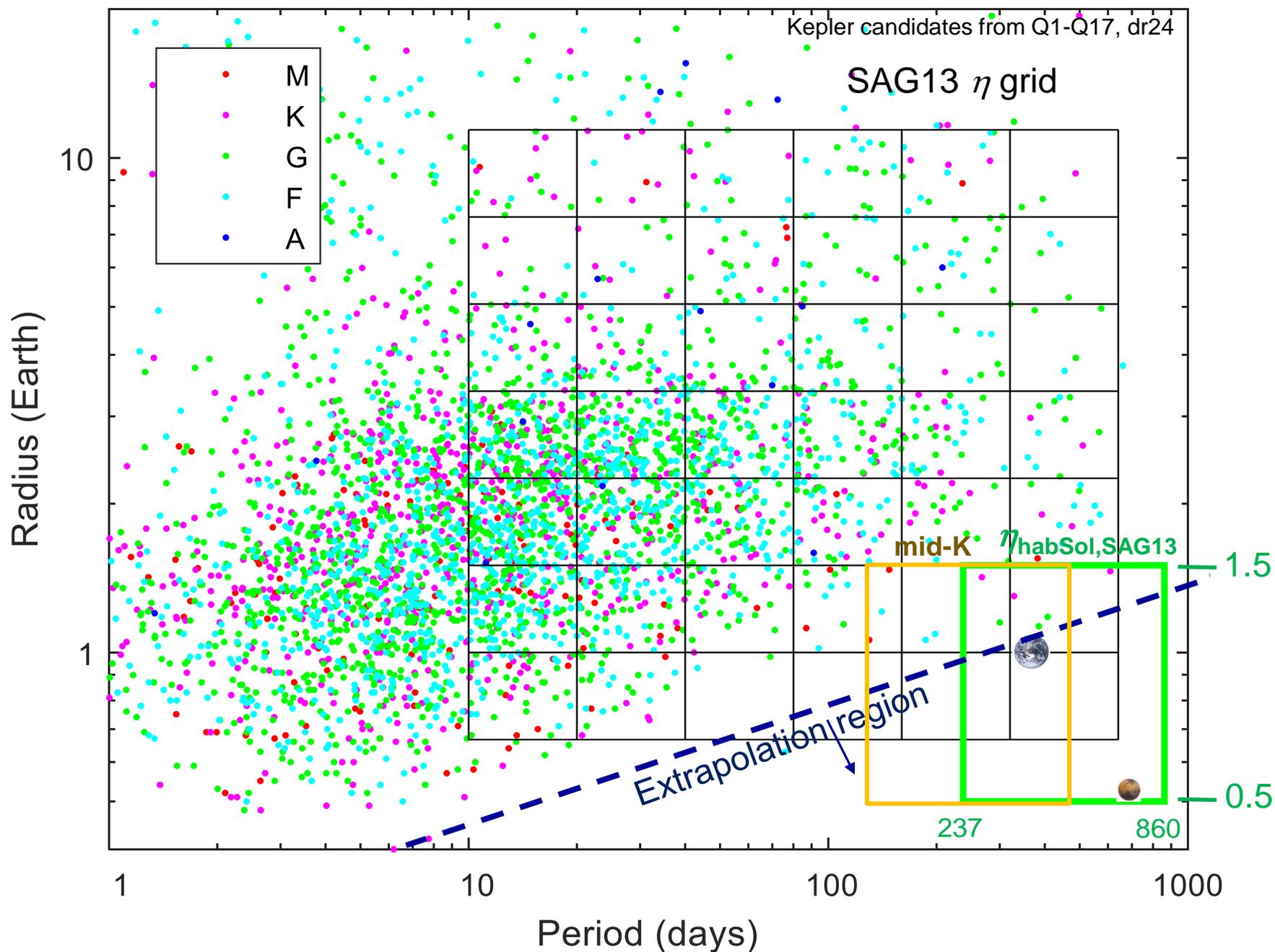




# Sensitivity of occurrence rates to methodologies and assumptions

- Completeness curves and catalog seem to make the largest systematic differences
  - More recent completeness curves and catalogs seem to lead to systematically higher numbers
- Other things (estimation method, details of the code, extrapolation) usually result in occurrence rates that are consistent to better than a factor of 2, usually much better

# Extrapolation and importance of 0.5-1.0 $R_{\text{Earth}}$ bin





# Parametric fit (for G-dwarfs)

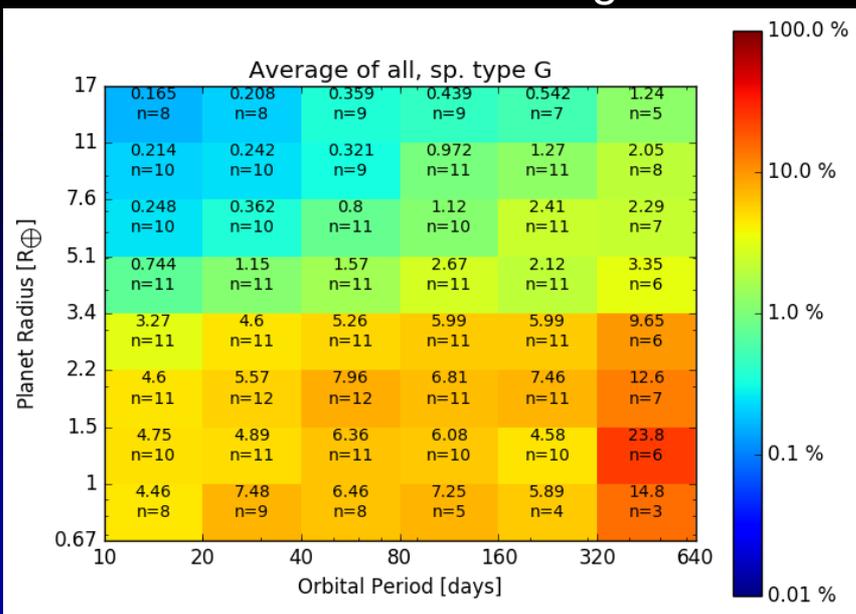
$$\frac{\partial^2 N(R,P)}{\partial \ln R \partial \ln P} = \Gamma_i R^{\alpha_i} P^{\beta_i} \quad \text{in region } R_{i-1} \leq R < R_i$$

(R in Earth radius, P in years)

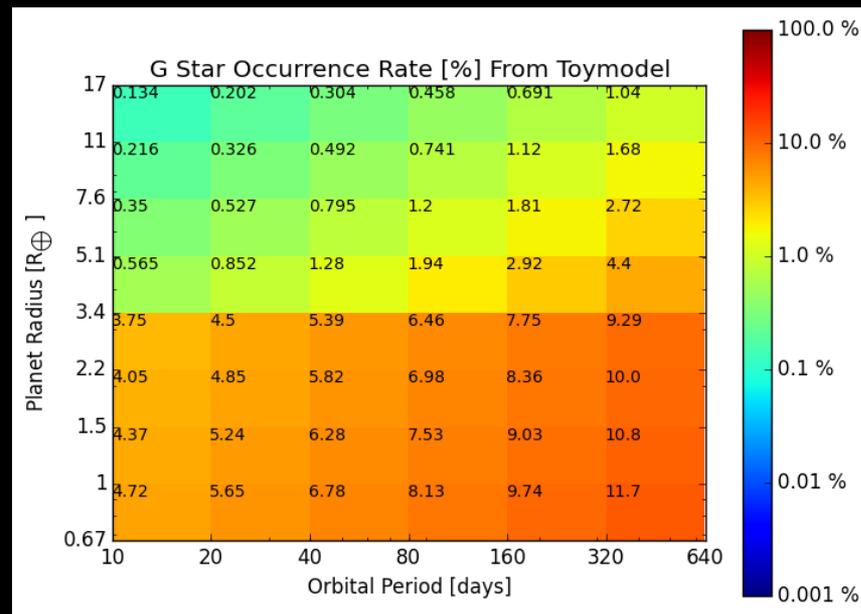
Two-piece  
broken  
power law →

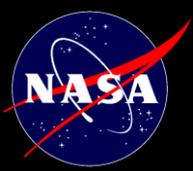
| $i$ | $\Gamma_i$ | $\alpha_i$ | $\beta_i$ | $R_i$ |
|-----|------------|------------|-----------|-------|
| 1   | 0.38       | -0.19      | 0.26      | 3.4   |
| 2   | 0.73       | -1.18      | 0.59      | Inf   |

Submission average



Parameteric fit (integrated across bins)





# Calculations of habitable occurrence rates

Integrating SAG13 parametric fit

|                     |         | HZ (from Kopparapu 2013) |             |
|---------------------|---------|--------------------------|-------------|
|                     |         | Conservative             | Optimistic  |
| Planet radius range | 1.0-1.5 | <b>0.14</b>              | <b>0.20</b> |
|                     | 0.5-1.5 | <b>0.40</b>              | <b>0.58</b> |

Using Burke et al. 2015 posterior tool  
<https://github.com/christopherburke/KeplerPORTs>

|                     |         | HZ (from Kopparapu 2013)                    |   |
|---------------------|---------|---|---|
|                     |         | Conservative                                | Optimistic                                |
| Planet radius range | 1.0-1.5 | <b>0.21<sup>+0.08</sup><sub>-0.08</sub></b> | <b>0.31<sup>+0.1</sup><sub>-0.1</sub></b> |
|                     | 0.5-1.5 | <b>0.5<sup>+0.4</sup><sub>-0.2</sub></b>    | <b>0.73<sup>+0.6</sup><sub>-0.3</sub></b> |

$\eta_{\text{habSol,SAG13}}$

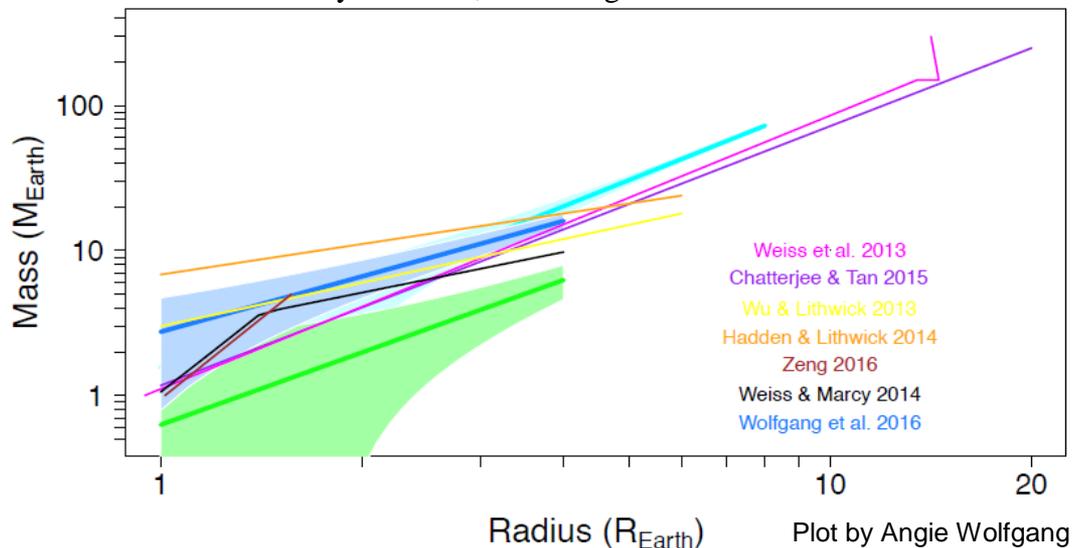


# Converting between Mass and Radius

(focus group led by Angie Wolfgang and Lauren Weiss)

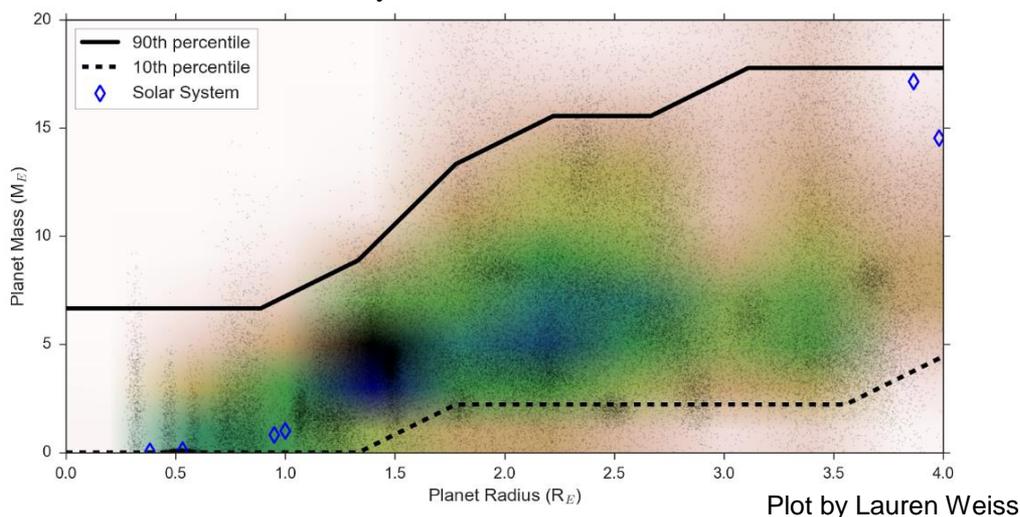
Previous M-R relations in the literature:

wide variety of radius, mass ranges and datasets used

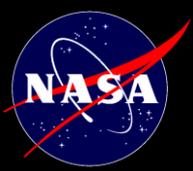


- Purpose: enable SAG13 occurrence rate submissions based on RV planets
- M-R relationship is fundamentally not a 1-1 map (e.g.  $M = f(R)$ ), but a correlation (e.g. density function  $C(M,R)$ )
- M-R focus group deliverables
  - an estimate of this correlation based on open community input
  - analysis of uncertainties and dependency on period and other parameters

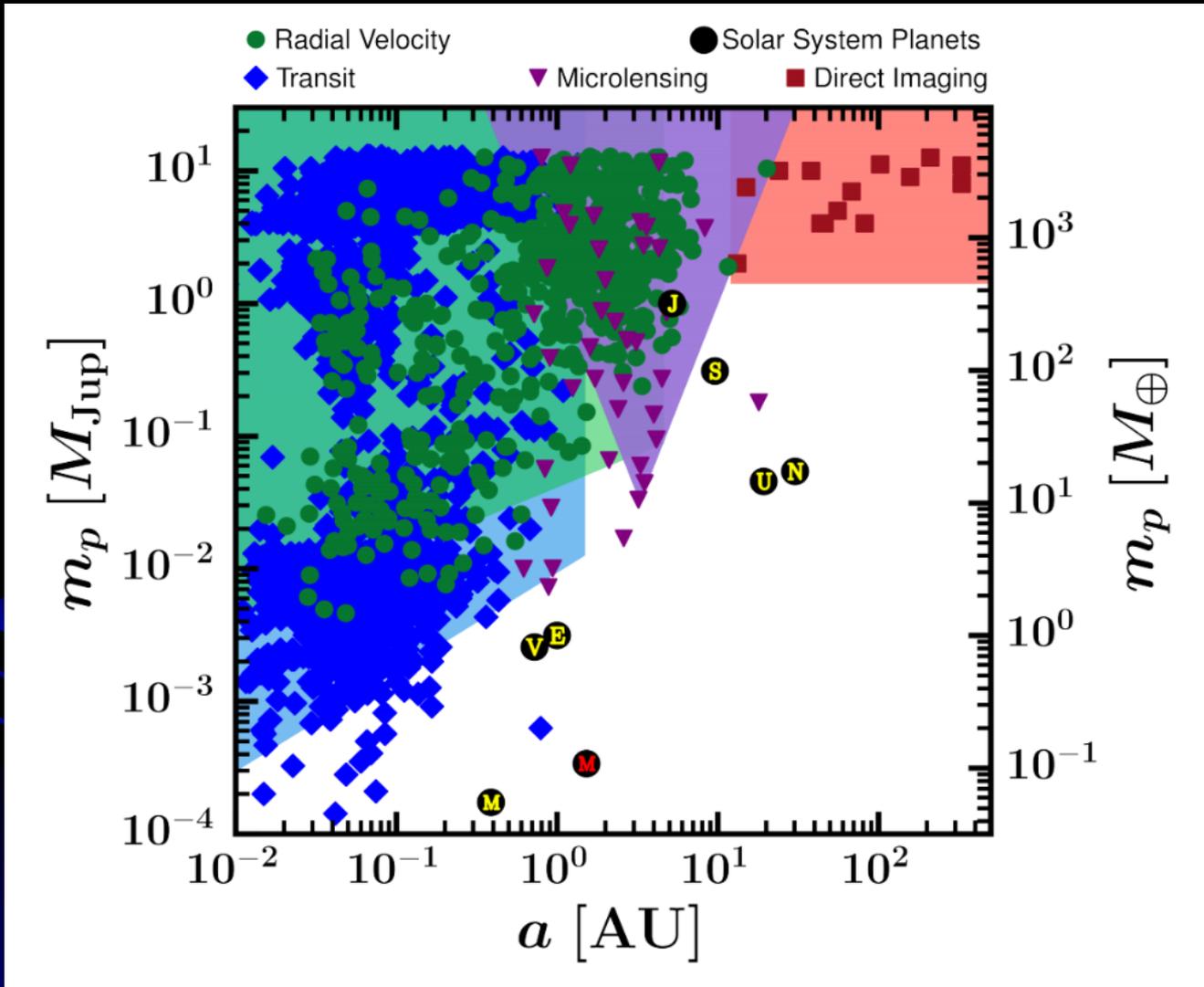
Preliminary estimate of M-R correlation



- Notes about plots / methods
  - TTV data is included
  - Black dots: MC posterior simulation accounting for uncertainties on currently known M-R planets
  - Color map: estimate of the 2D correlation density function (using Gaussian kernel density estimator)



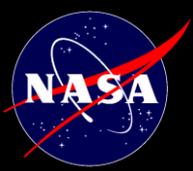
# Linking to results from non-Transit techniques (Christian Clanton)



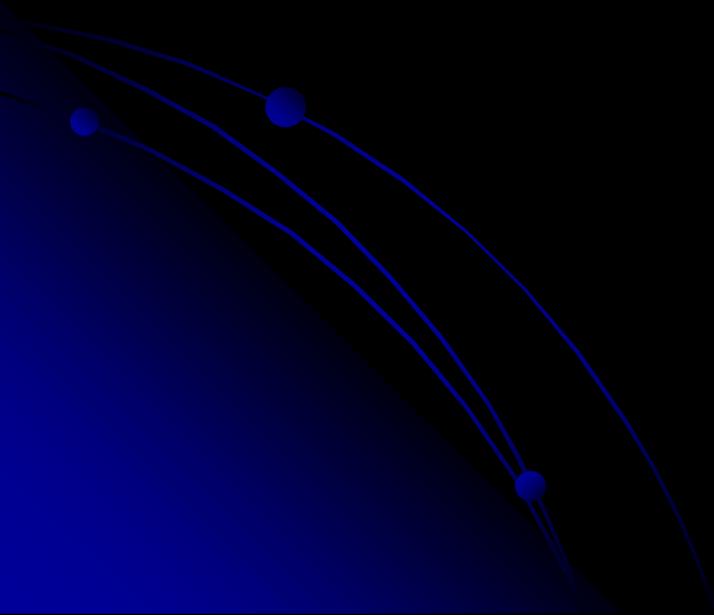


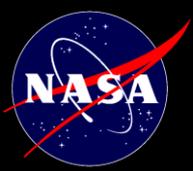
# Conclusions

- $\eta_{\text{Earth}}$  may be significantly higher than many older estimates, especially if going down to 0.5 Earth size ( $\eta_{\text{habSol, SAG13}} \sim 0.6$ )
  - Cannot yet rule out lower values (e.g.  $< \sim 0.3$ ), but values  $> 1$  appear to be more likely than  $< 0.3$
  - Burke 2015  $\eta_{\text{Earth}}$  is even higher
  - Caveat: SAG13 products are not formal scientific results, but rather a meta-analysis to achieve consensus on “most likely” assumptions for mission studies. The upcoming Kepler closeout will yield a formal scientific result.
- Although many orders of magnitude of  $\Gamma_{\text{Earth}}$  (or  $\eta_{\text{Earth}}$ ) are possible, only a small range ( $\sim 1$ -2 octaves) within that is “likely”
- Tentative parametrized distributions are available from SAG13 to use with mission yield calculation codes (or any other purpose)
  - Based on input from the entire exoplanet community
  - See slide 14



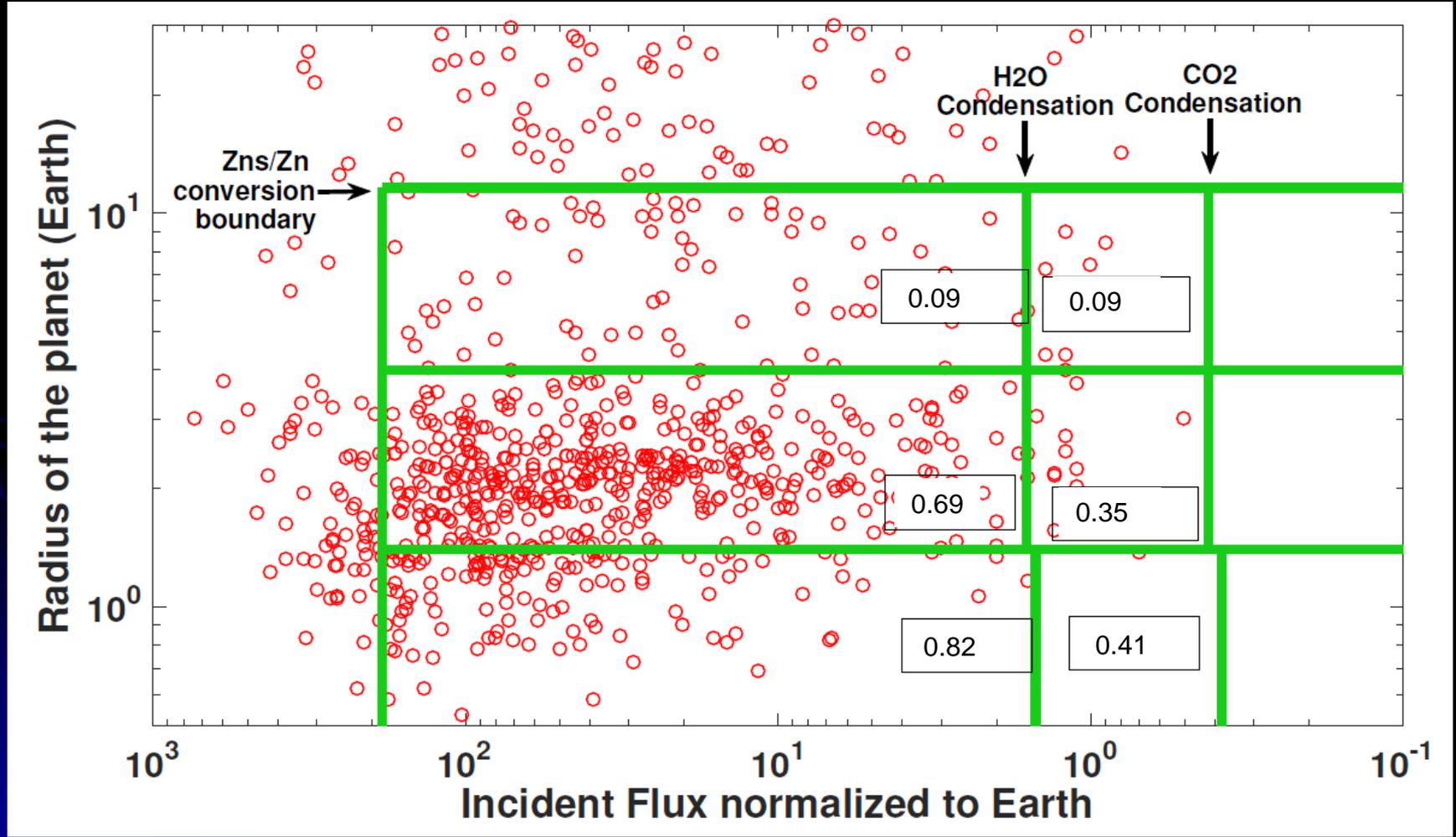
# Backup slides





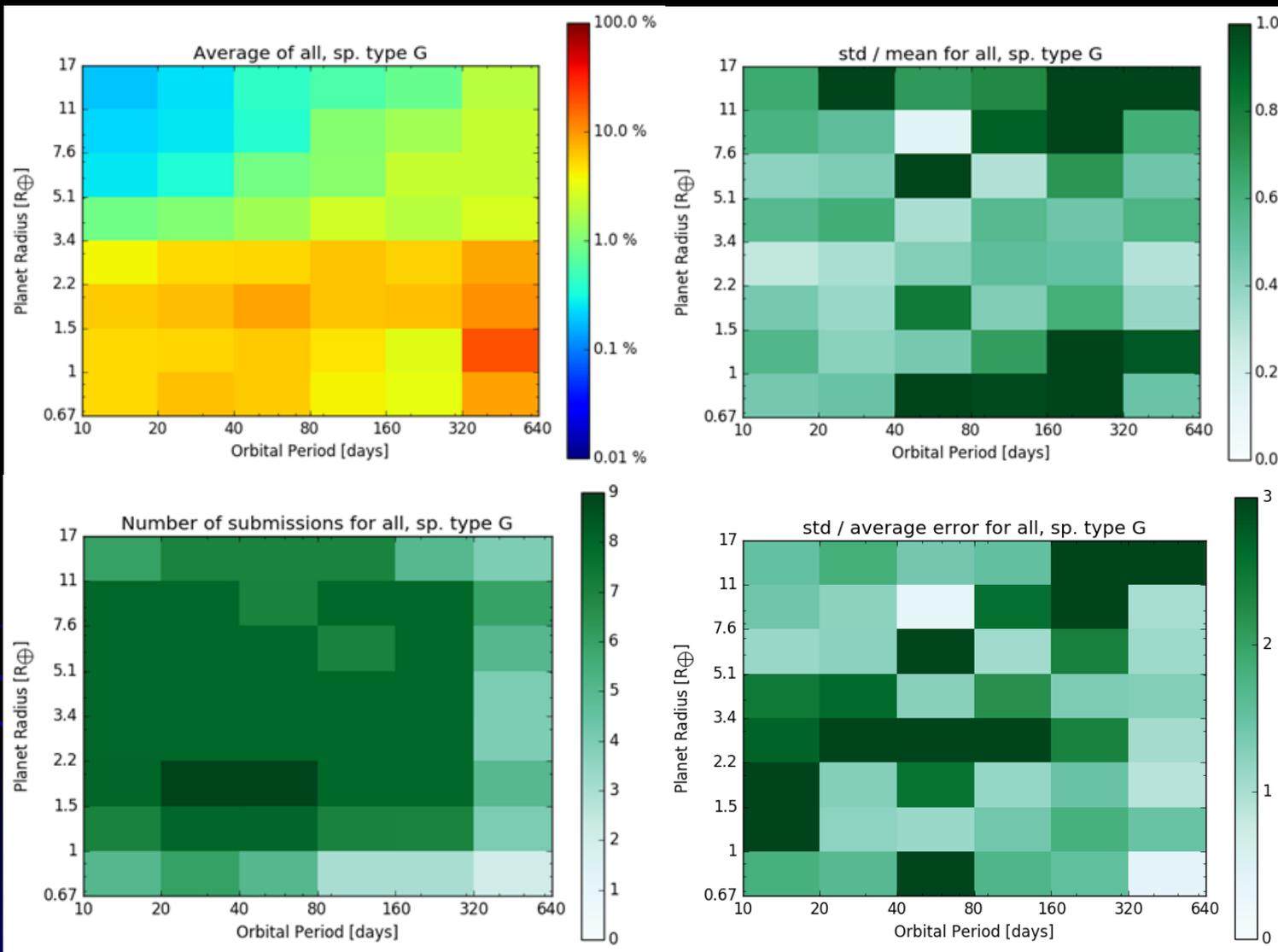
# Occurrence rates for new proposed planet classification

(from Kopparapu, Domagal-Goldman, et al., in prep)  
Numbers based on integrating SAG13 parametric fit





# Analysis of variations in submissions (for G-dwarfs)

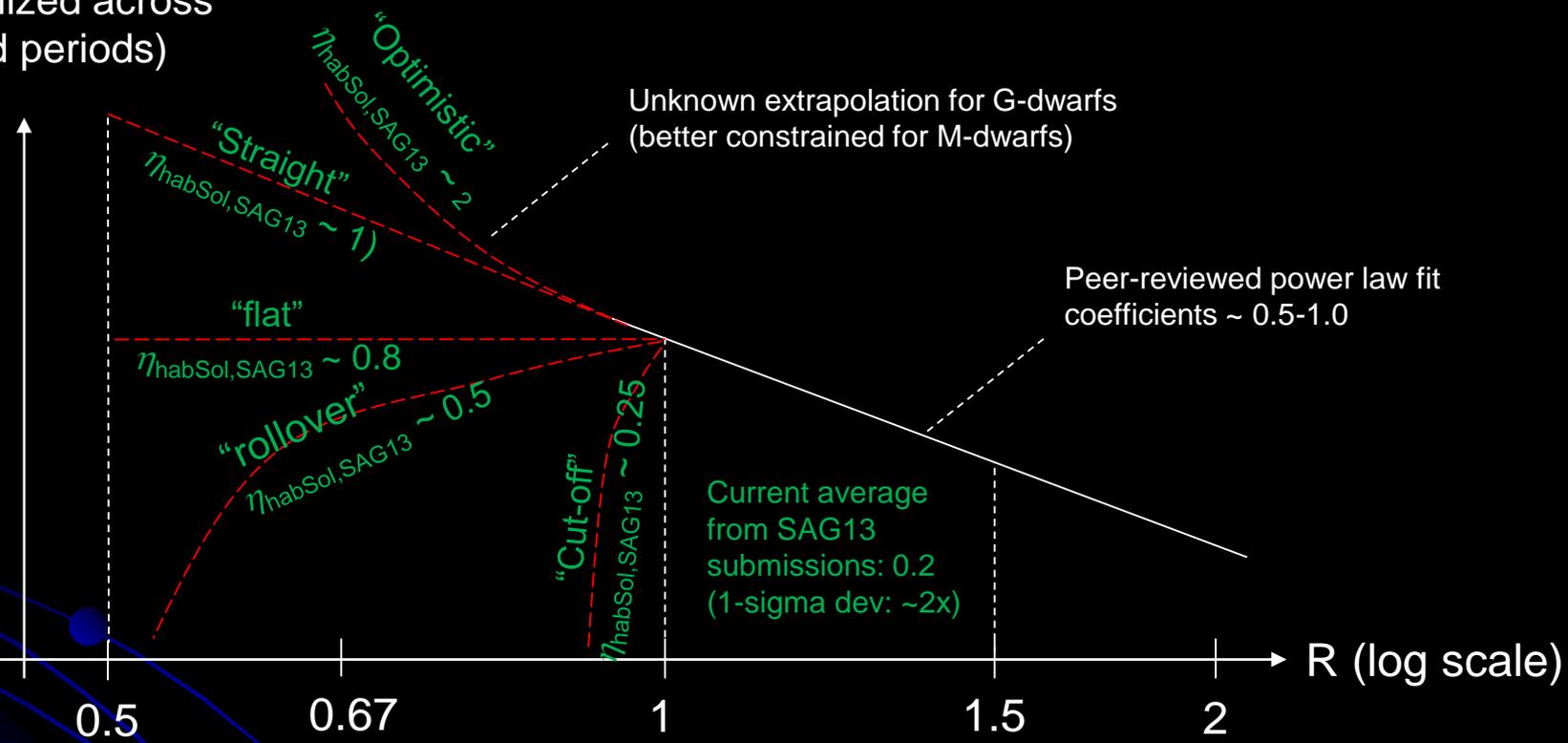


by Gijs Mulders



# Importance of 0.5-1.0 Earth size bin

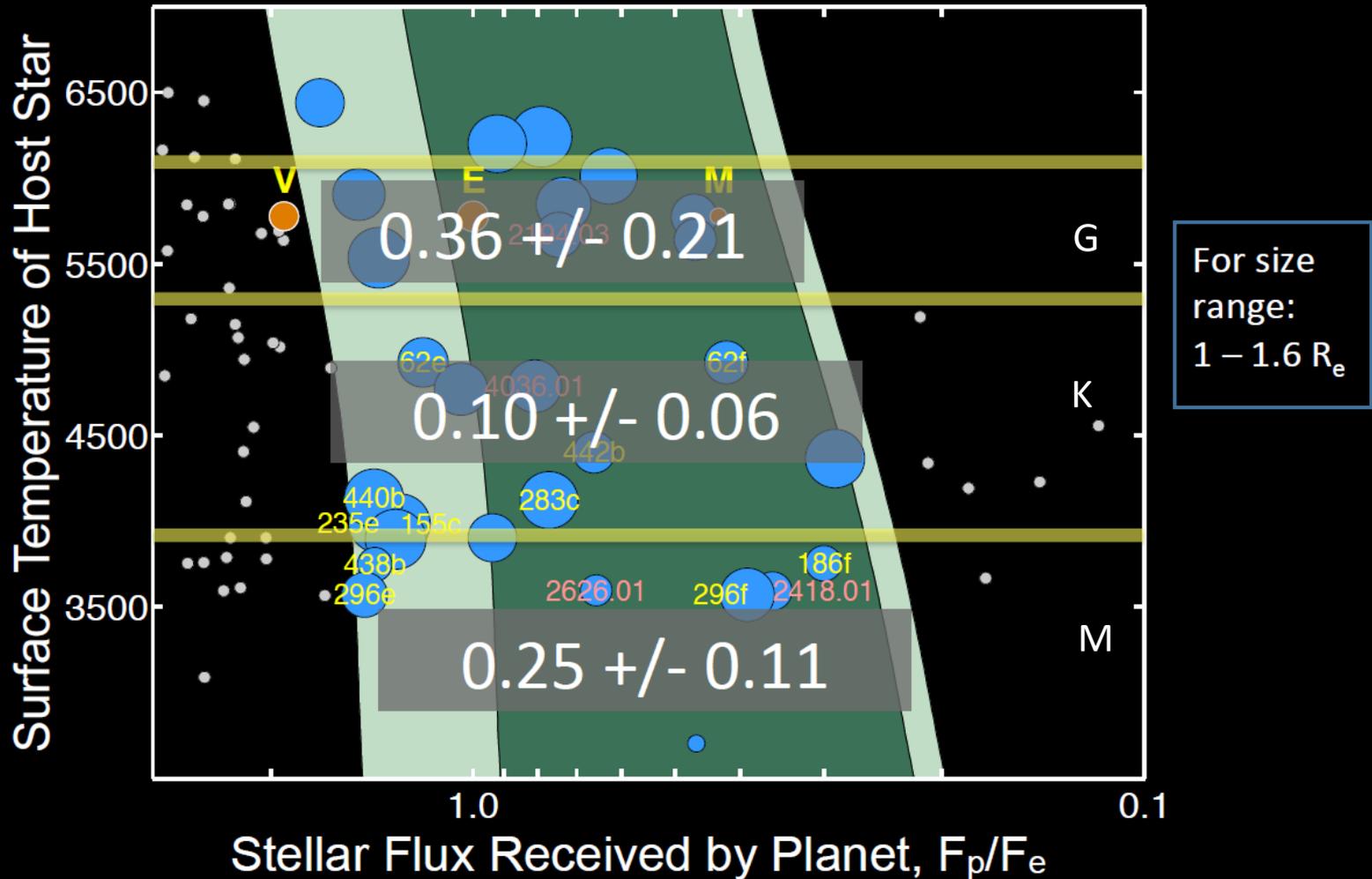
$dN / d\ln(R)$   
(marginalized across  
237-860d periods)



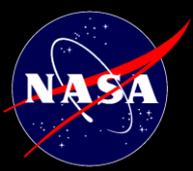
- Any estimate of  $\eta_{Earth}$  should always very clearly specify:
  - Whether 0.5-1.0 bin is included or not
  - What extrapolation assumption was made
- Many discrepancies in  $\eta_{Earth}$  estimates can be traced to inclusion or exclusion of 0.5-1.0 bin
- Mission study teams may want to consider the possibility of a large number of potentially habitable planets in the 0.5-1.0 bin

# Small (< 2 R<sub>e</sub>) Planets in the HZ: 4 yr

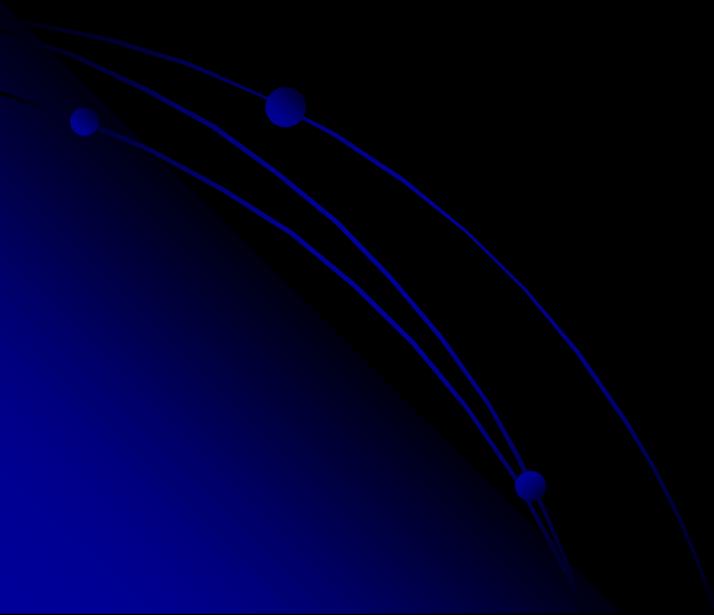
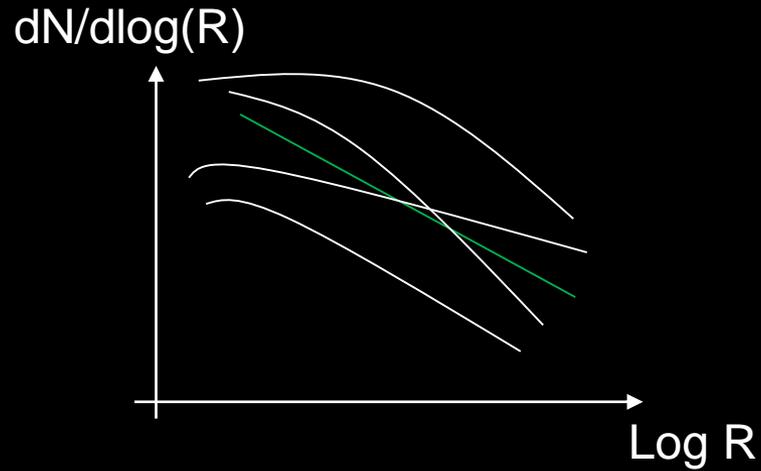
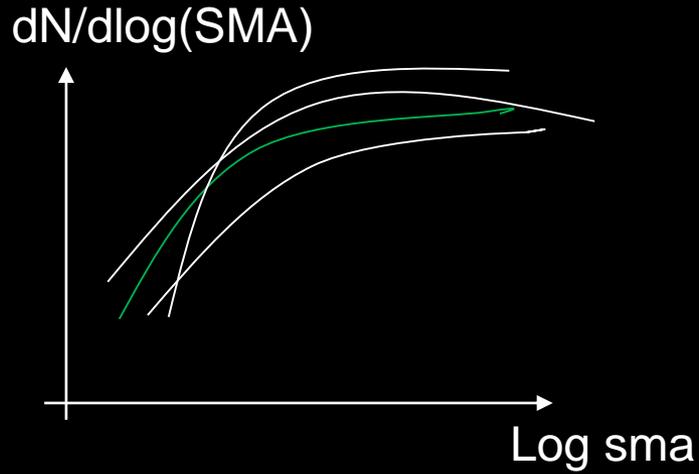
Empirical HZ
  Narrow HZ
  In HZ, symbol scaled to size of Earth



Note: for planet size range of 0.5 – 1.6 R<sub>e</sub>, expected # of planets may be a factor of ~2-3 higher (based on extrapolation)



# Variations between individual parameterized distributions



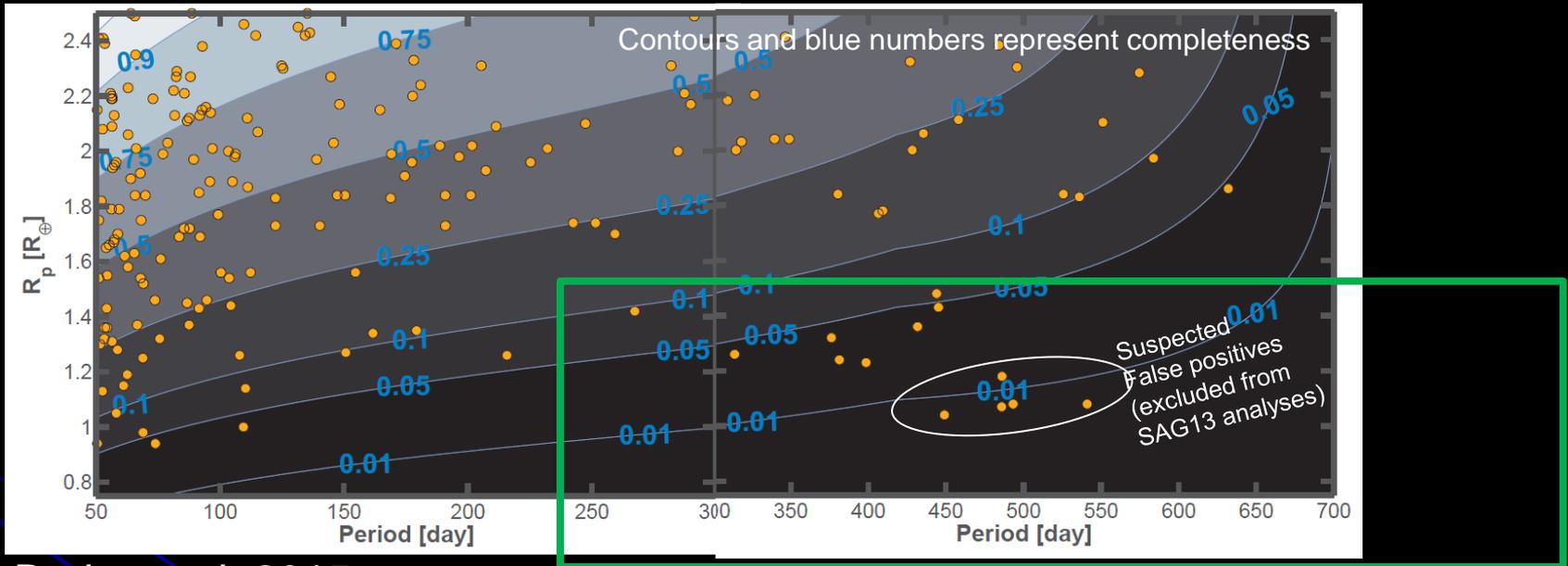


# Current edge of planet candidates

[potential slide, meant to show actual planets and thus better visualize Poisson uncertainty]

Shorter periods, more reliable

Longer periods, less reliable

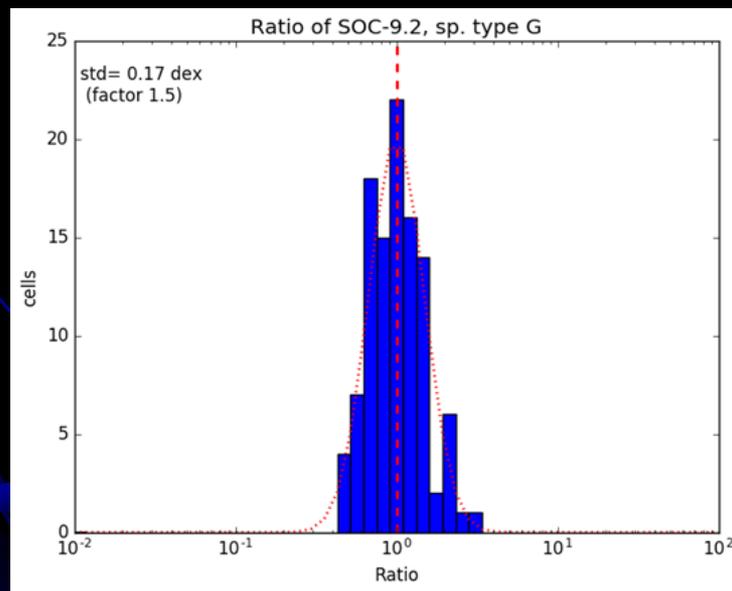
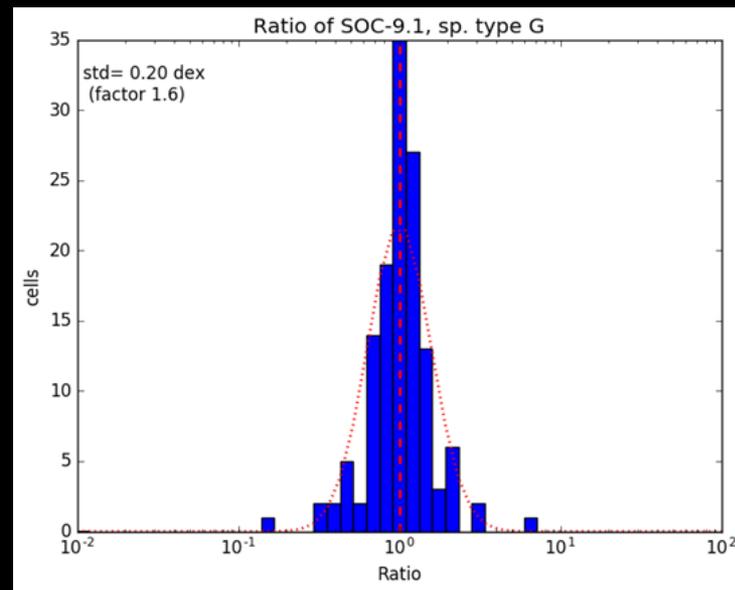
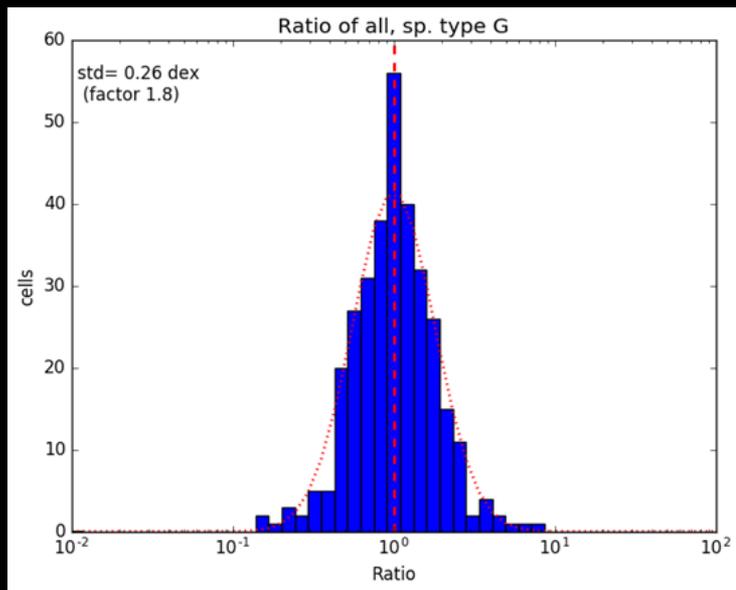


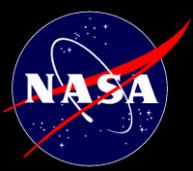
Burke et al. 2015

0.5-1.5 Earth size  
237-860 days (Kopparapu extended HZ for Sun)



# Variance in submissions

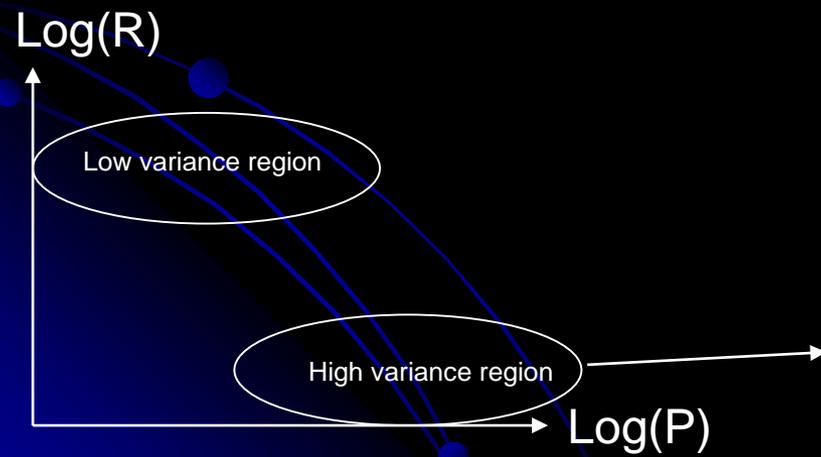




Slide which shows any key correlations we found between variances / outliers and submission parameters (catalog, method, etc.)

[Goal is to show status and any key preliminary patterns we found in the most clear and concise way but emphasize that this is still a work in progress]

Rough idea for visualization:



| Value of $\Gamma_{\text{earth}}$ | catalog               | Completeness ? | Methodology ? |
|----------------------------------|-----------------------|----------------|---------------|
| Lowest value                     | Early catalog ?       |                |               |
|                                  |                       |                |               |
|                                  |                       |                |               |
|                                  |                       |                |               |
|                                  |                       |                |               |
| Highest value                    | More recent catalog ? |                |               |

ROUGH DRAFT

[Note – for now, table entries are purely illustrative, not necessarily ones that we will have in the final slide]



# Details of submitted rates

|                         | Catalog | Filters | Completeness model | Vetting efficiency | Reliability | Methodology | Value of $\Gamma_{\text{earth}}$ |
|-------------------------|---------|---------|--------------------|--------------------|-------------|-------------|----------------------------------|
| Batalha, Natalie (2)    |         |         |                    |                    |             |             |                                  |
| Belikov, Rus            |         |         |                    |                    |             |             |                                  |
| Burke, Chris            |         |         |                    |                    |             |             |                                  |
| Catanzarite, Joe        |         |         |                    |                    |             |             |                                  |
| Dressing, Courtney*     |         |         |                    |                    |             |             |                                  |
| Farr, Will              |         |         |                    |                    |             |             |                                  |
| Foreman-Mackey, Daniel* |         |         |                    |                    |             |             |                                  |
| Kopparapu, Ravi         |         |         |                    |                    |             |             |                                  |
| Mulders, Gijs           |         |         |                    |                    |             |             |                                  |
| Petigura, Erik*         |         |         |                    |                    |             |             |                                  |
| Traub, Wes**            |         |         |                    |                    |             |             |                                  |

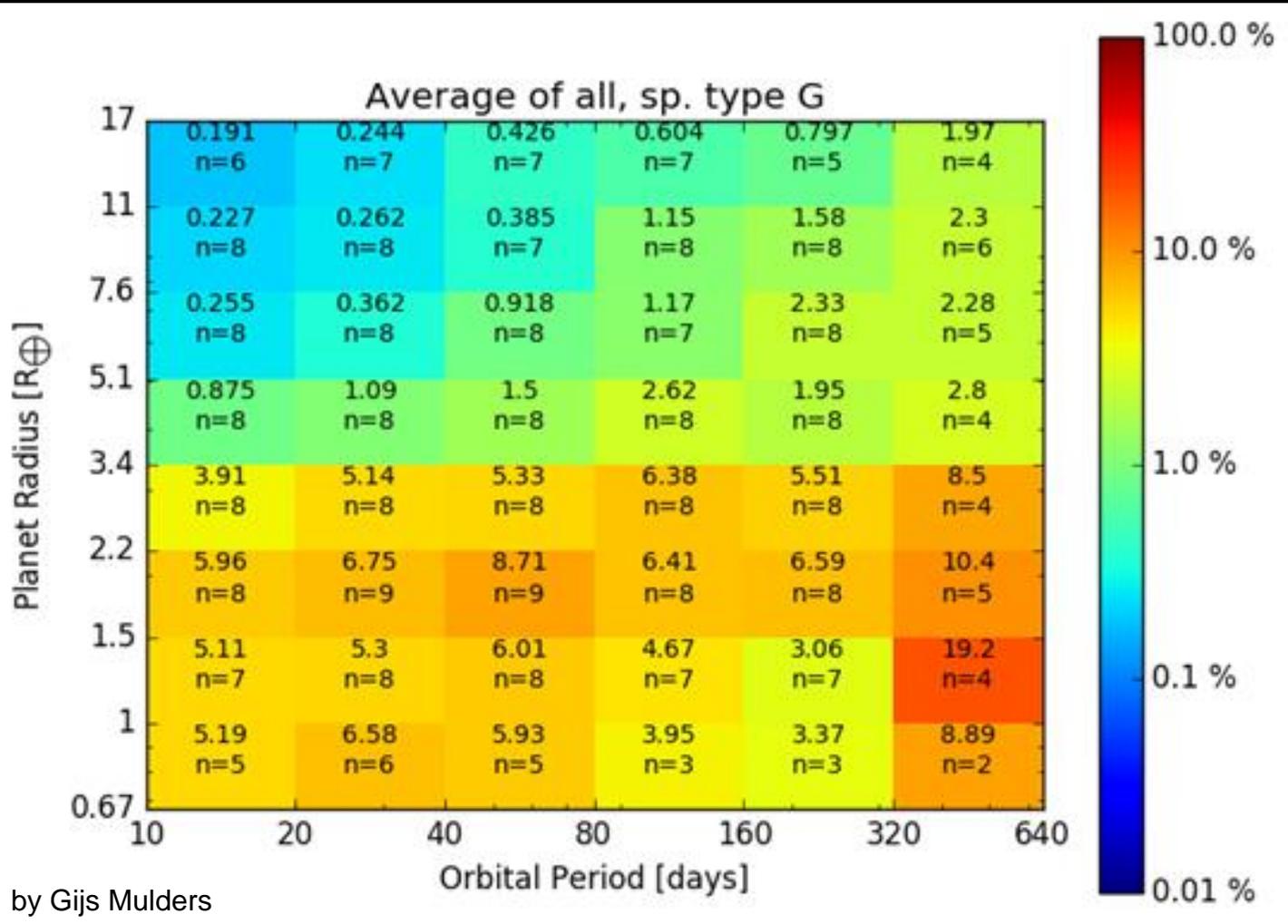


# Closer look at G-dwarf average

## legend

% occurrence

# of submissions





# How do we combine different submissions into one occurrence table?

Full accounting:  
Only “independent” submissions  
are averaged

Accounting for “dependency”  
between submissions

No accounting:  
Simply average all  
submissions



- Best for producing an actual scientific measurement
- Measuring “dependency” is not trivial (and may be impossible in principle)
- Consensus on method can be challenging
- Psychological biases are challenging to identify and control

- Will not generate a scientific measurement, but possibly best for predictions?
- Simple method
- Easier consensus: all submissions are automatically fairly represented
- Crowdsourcing / Prediction market philosophy: psychological biases are in theory averaged out

The question of which method is “correct” is possibly philosophical  
Will probably do both, explicitly describe the process, and leave interpretation to the reader  
Feedback on our strategy is welcome and encouraged