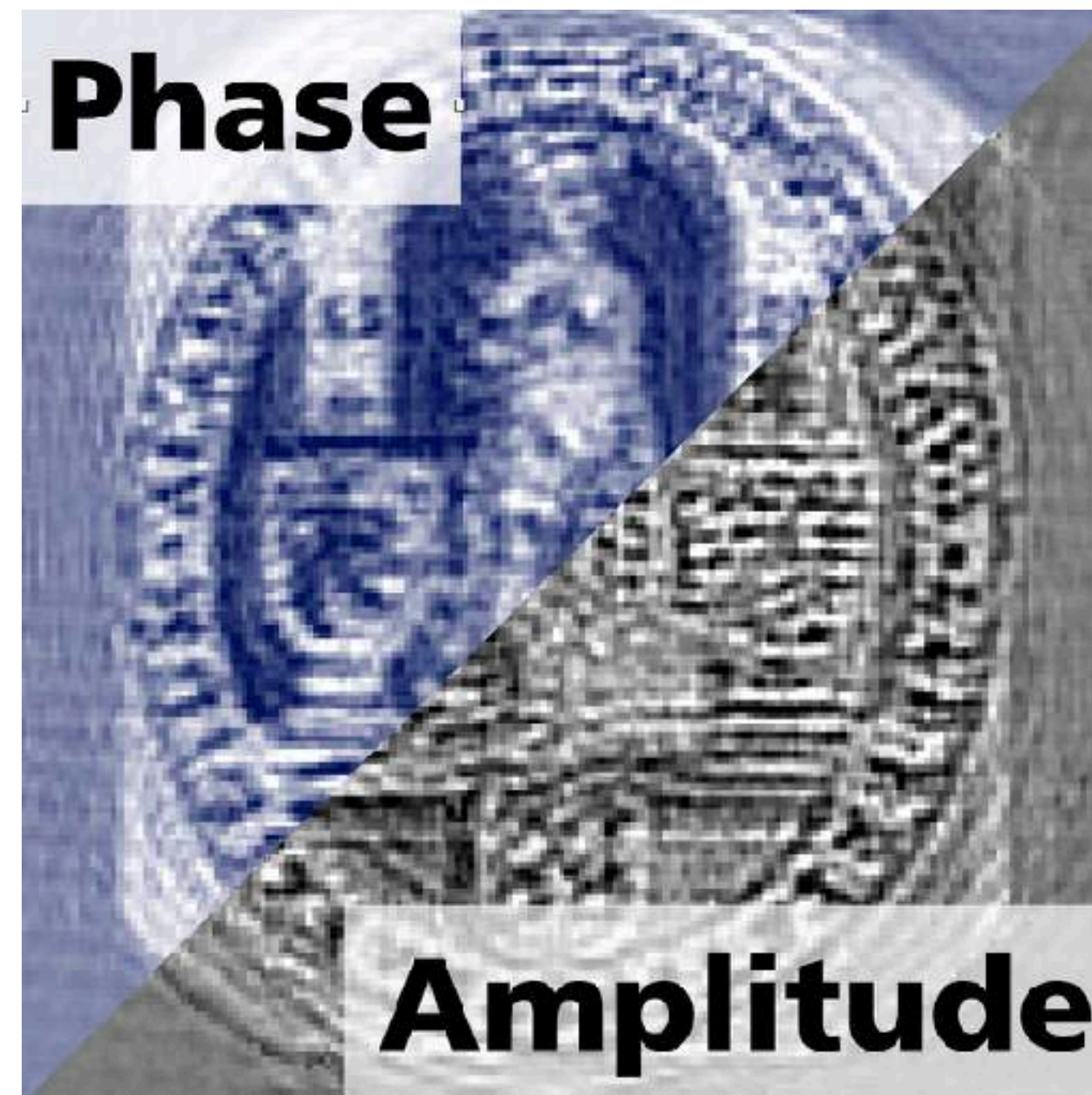


The vector-Zernike wavefront sensor

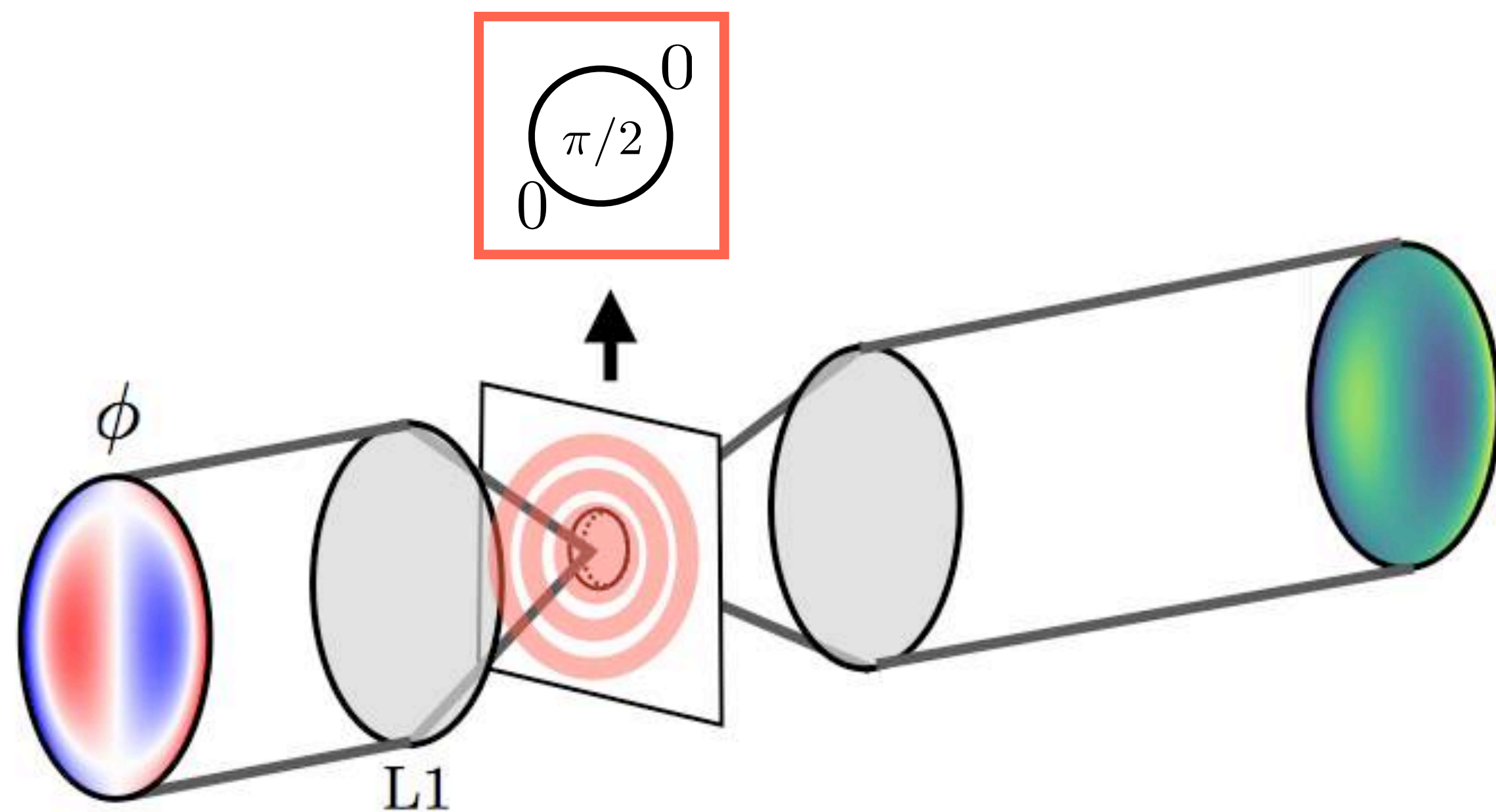


David S. Doelman*, Fedde Fagginger Auer, Emiel Por,
Micheal J. Escuti and Frans Snik

[*doelman@strw.leidenuniv.nl](mailto:doelman@strw.leidenuniv.nl)



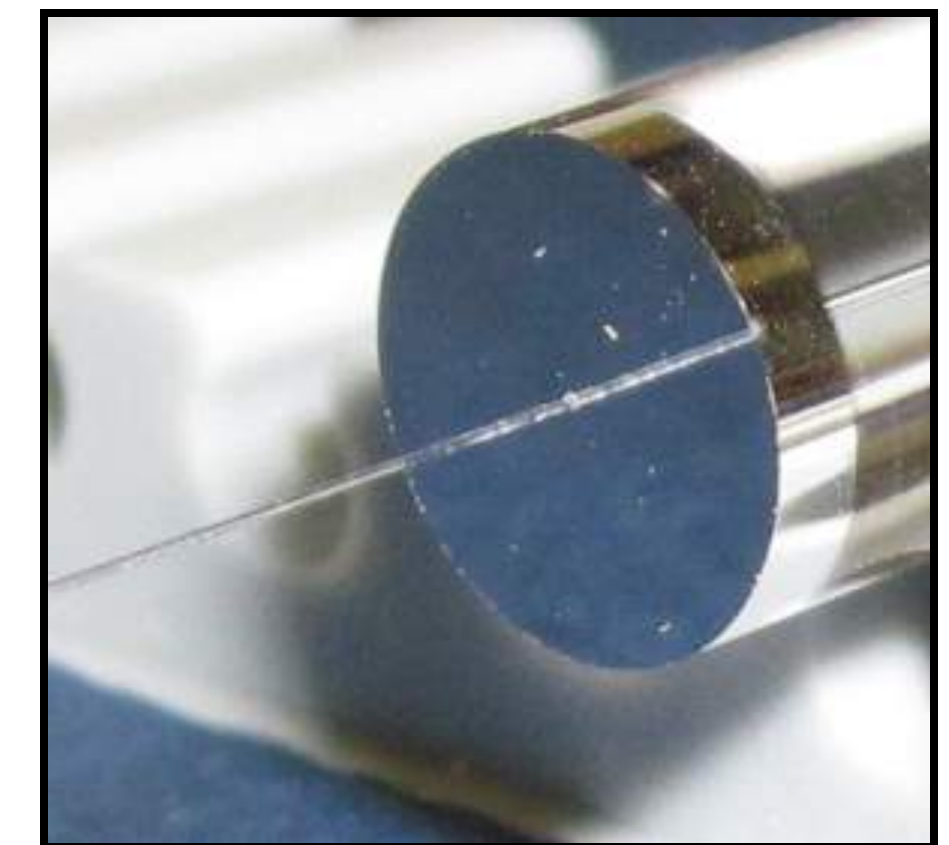
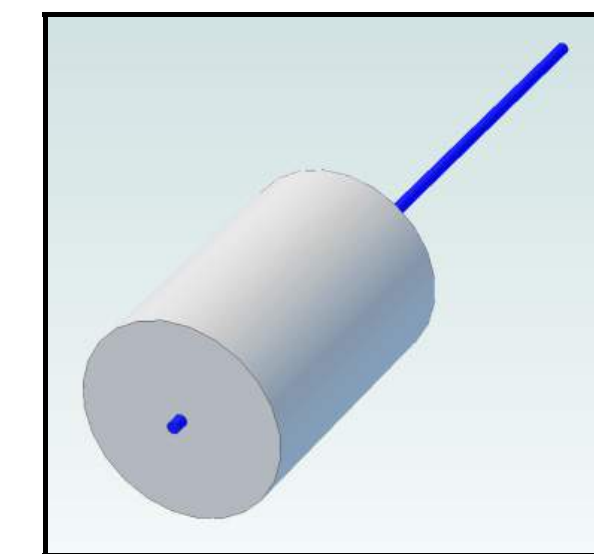
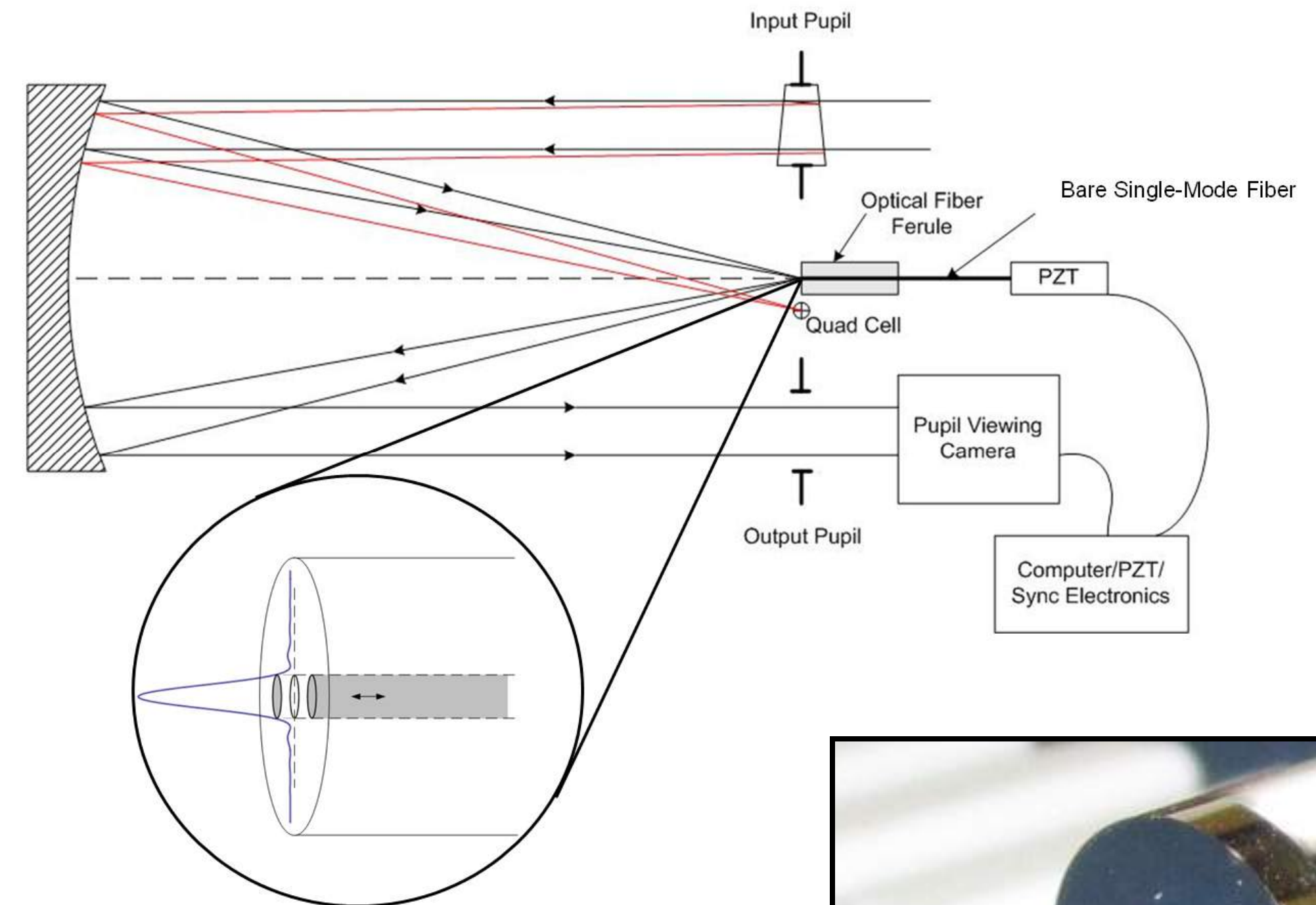
The Zernike wavefront sensor



- **Phase aberrations are converted to intensity variations in the conjugated pupil plane**
- **Most sensitive wavefront sensor (Guyon 2005)**
- **Limited dynamic range**
- **Varying amplitude variations reconstructed as phase aberrations**

Phase-Shifting Zernike Interferometer Wavefront Sensor

- Zernike mask consists of silver-coated single-mode fiber with moving optical capillary tube.
- With four phase steps ($-\pi/2$, 0 , $\pi/2$ and π), both phase and amplitude of the wavefront can be recovered



Wallace et al. 2011

Phase-Shifting Zernike Interferometer Wavefront Sensor

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- With four phase steps ($-\pi/2$, 0 , $\pi/2$ and π), both phase and amplitude of the wavefront can be recovered

$$I_1 = E_1 \cdot E_1^* = A^2(1 + \varepsilon^2 - 2\phi + \phi^2)$$

$$I_2 = E_2 \cdot E_2^* = A^2(1 + \varepsilon^2 + 2\varepsilon + \phi^2)$$

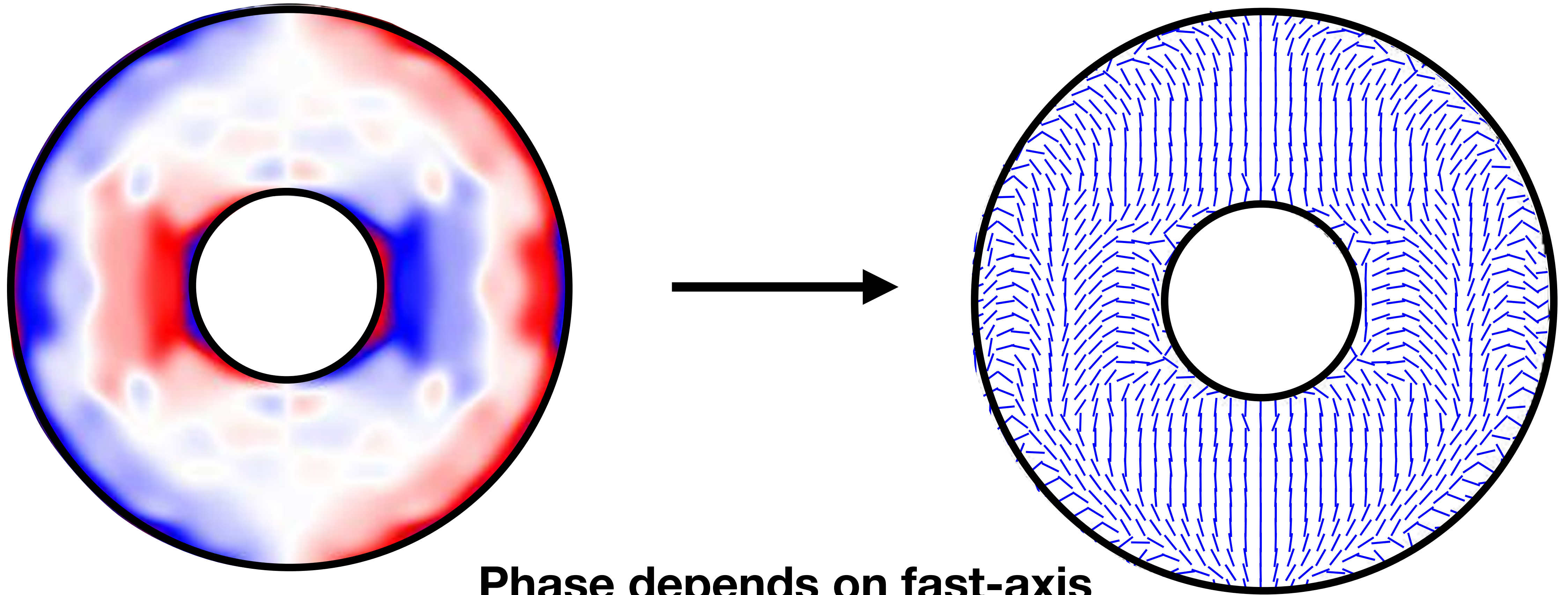
$$I_3 = E_3 \cdot E_3^* = A^2(1 + \varepsilon^2 + 2\phi + \phi^2)$$

$$I_4 = E_4 \cdot E_4^* = A^2(1 + \varepsilon^2 - 2\varepsilon + \phi^2)$$

$$I_0 = (I_1 + I_2 + I_3 + I_4)/4.$$

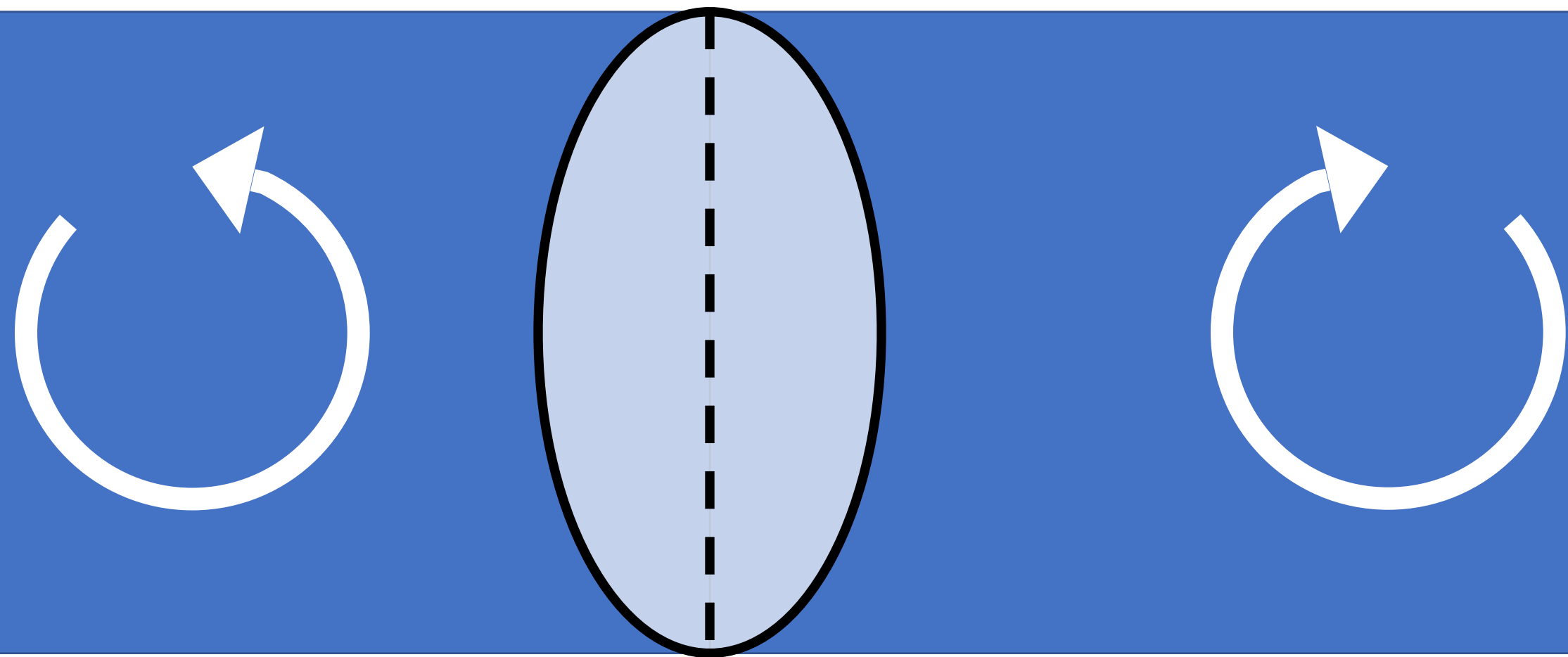
$$\phi = \frac{I_3 - I_1}{4I_0} \quad \varepsilon = \frac{I_2 - I_4}{4I_0}$$

Liquid-crystal technology: the geometric phase



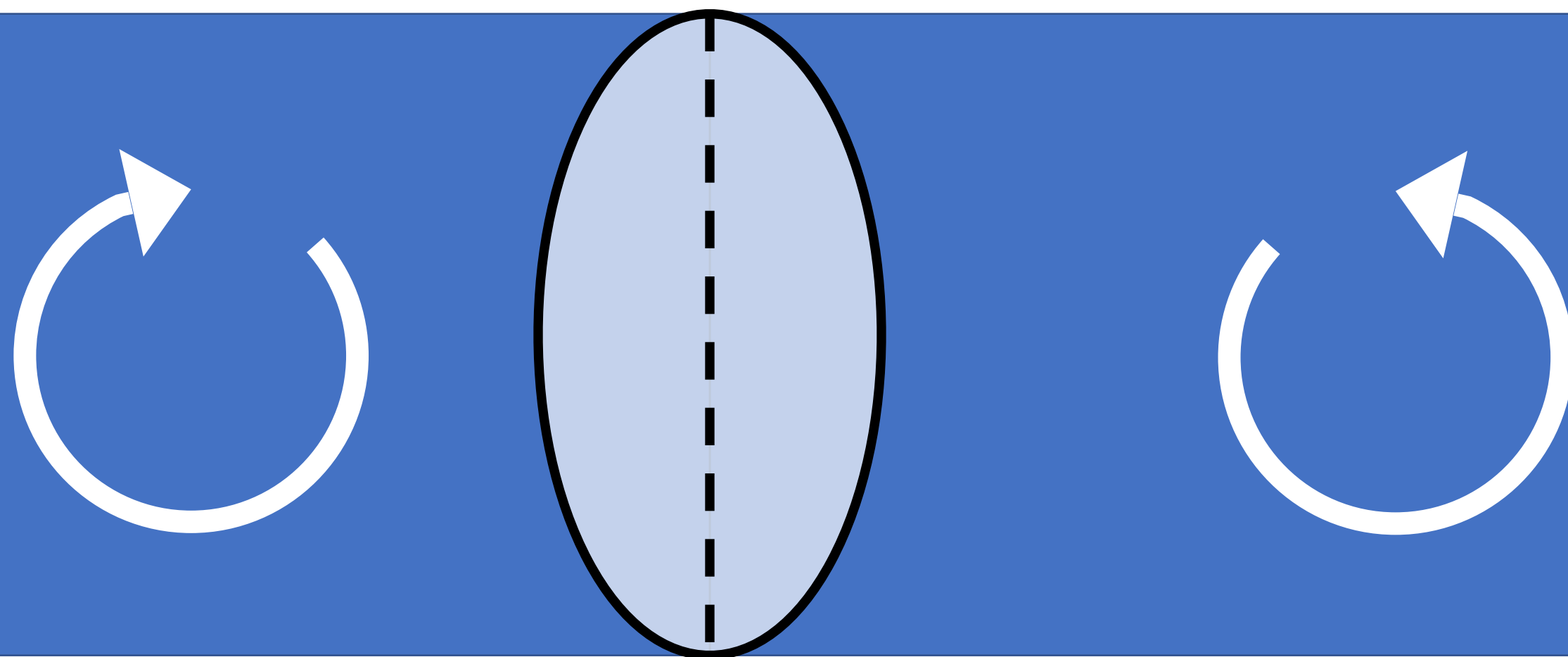
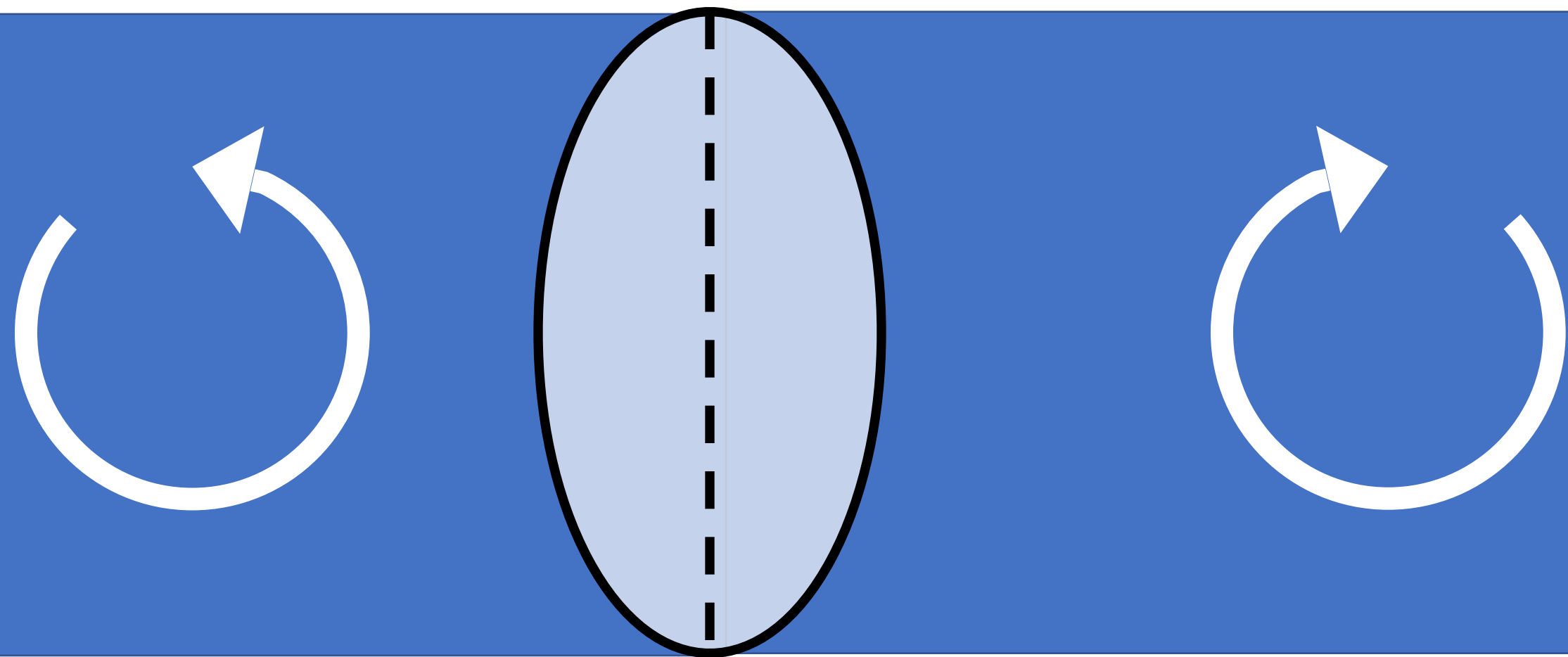
**Phase depends on fast-axis
orientation in a half-wave retarder
and circular polarization state**

Geometric phase

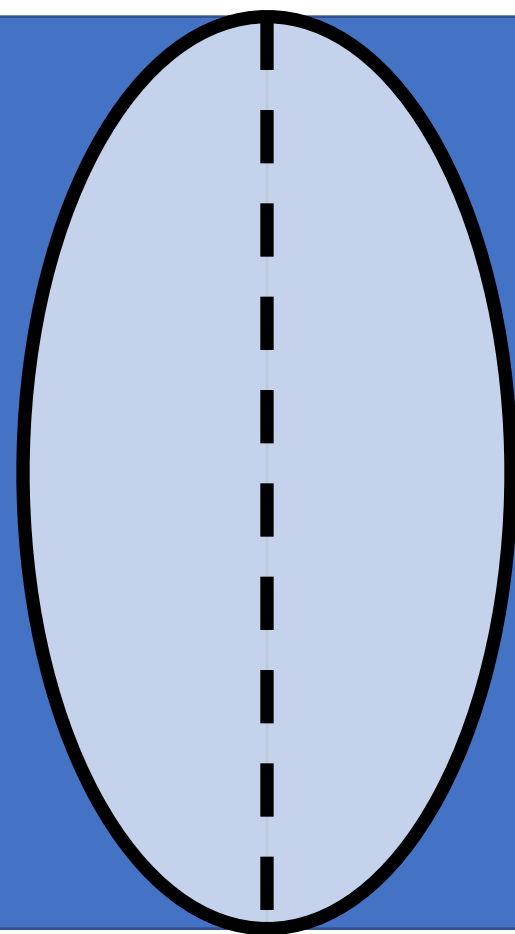
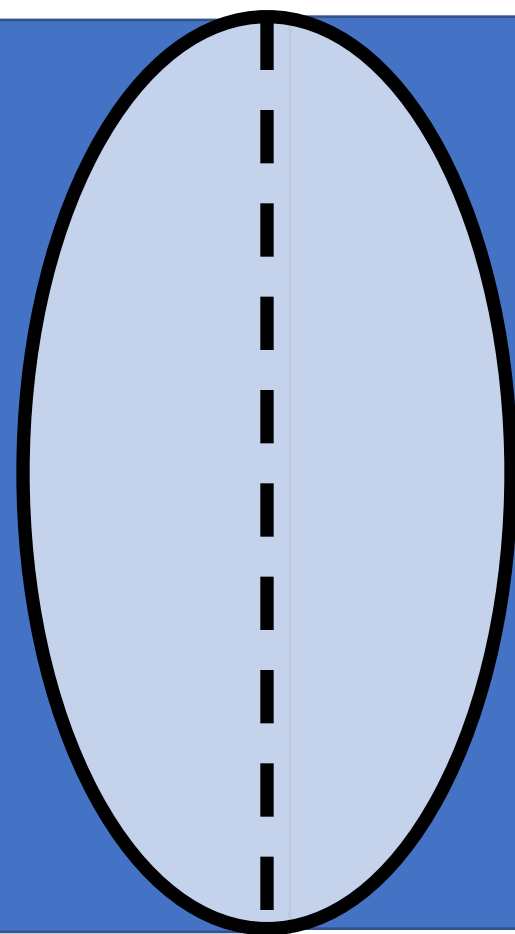


$\frac{\lambda}{2}$ -plate

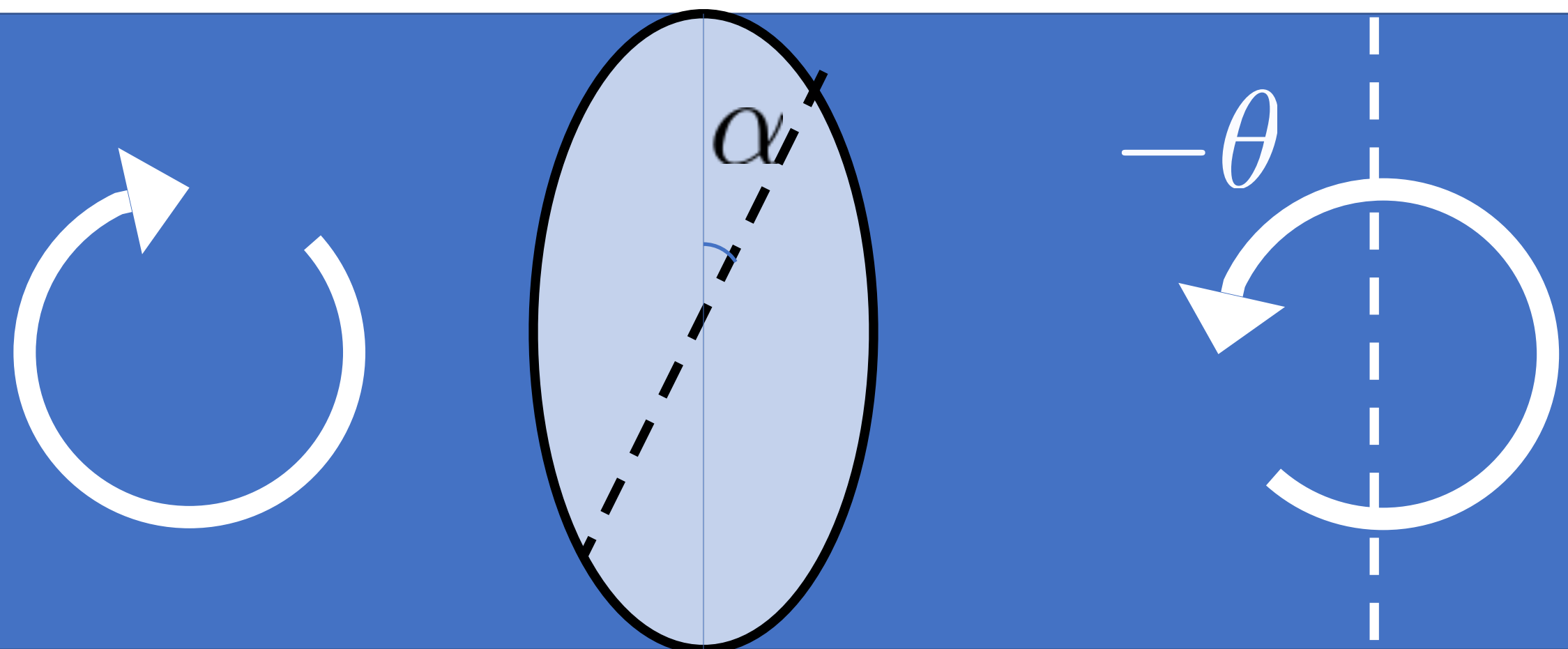
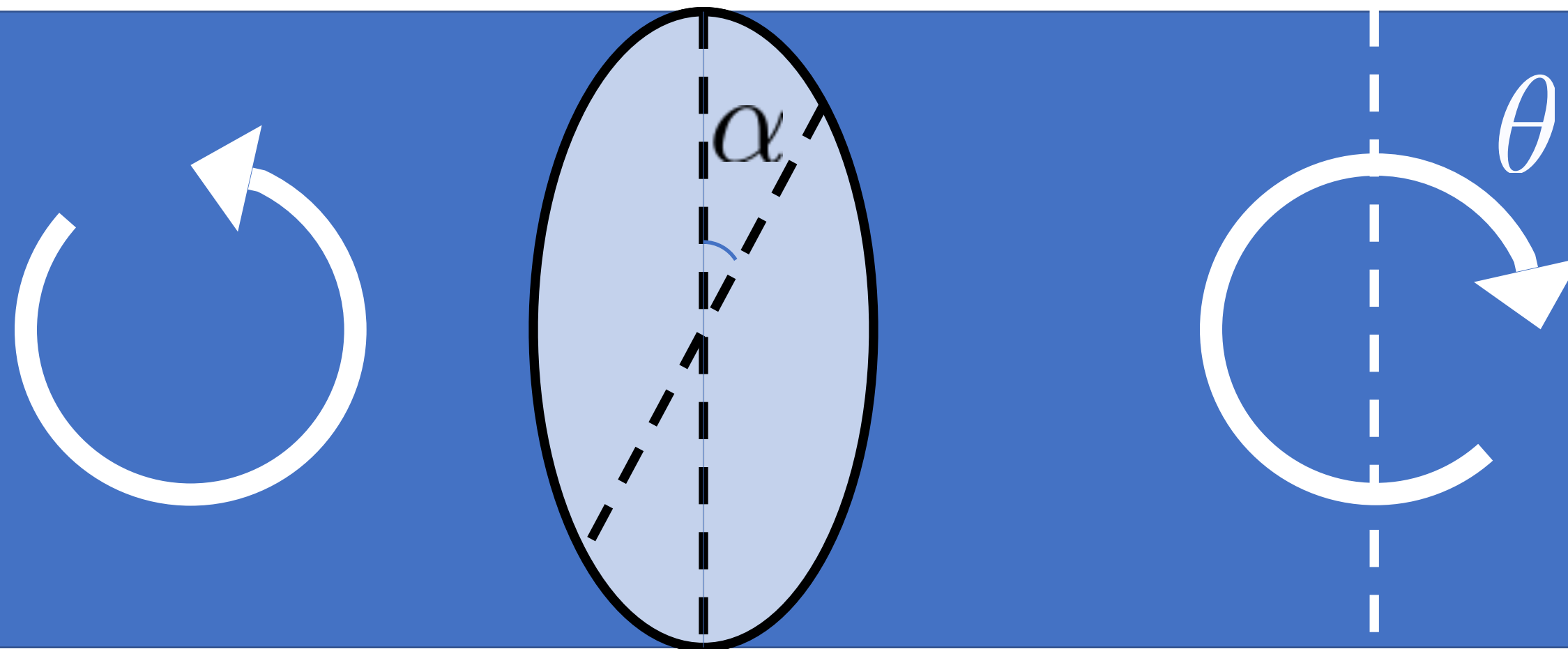
Geometric phase



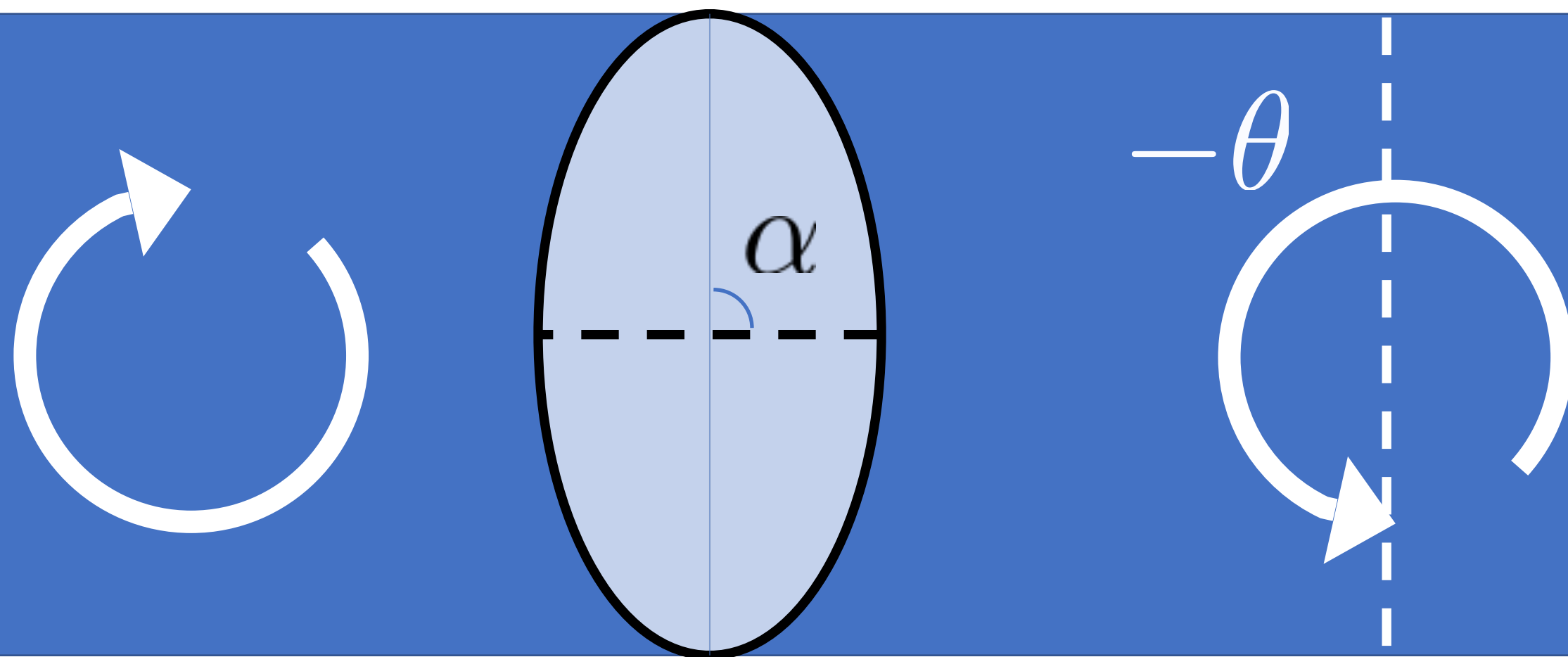
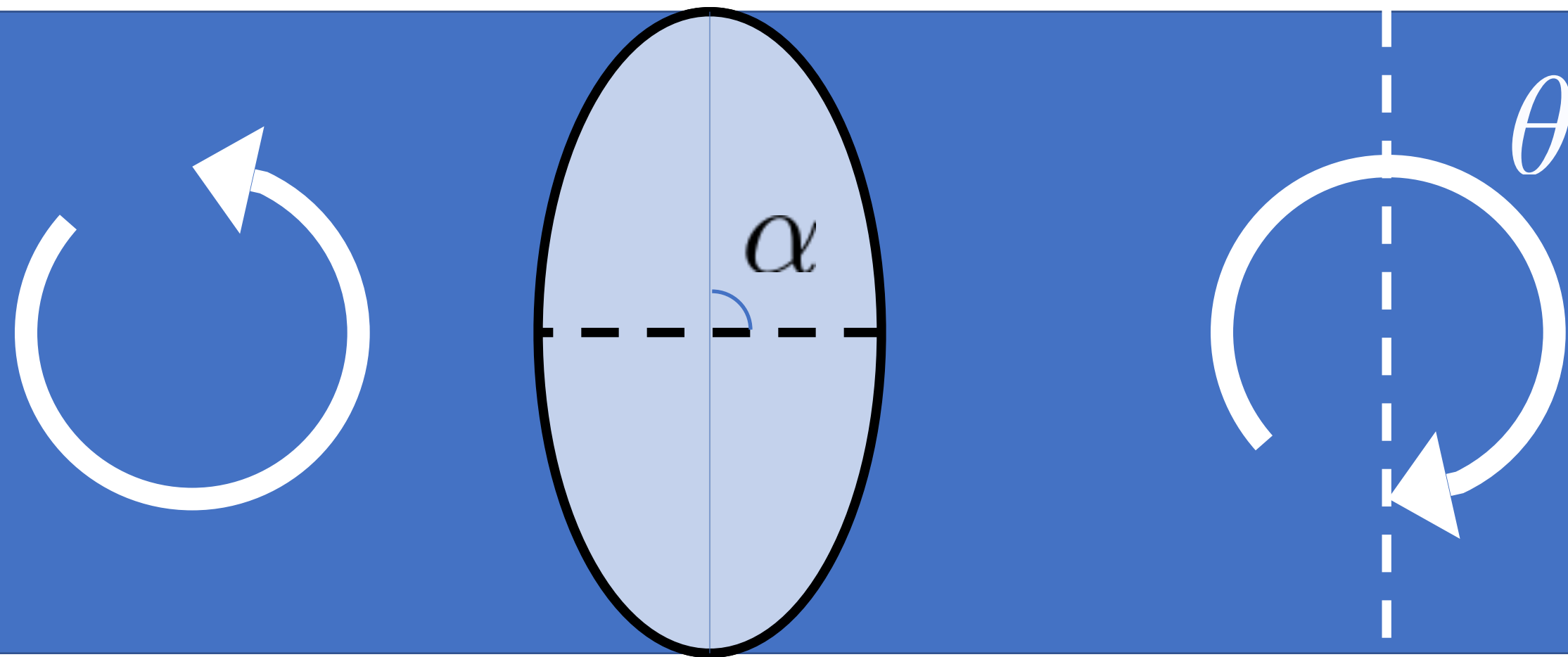
Geometric phase



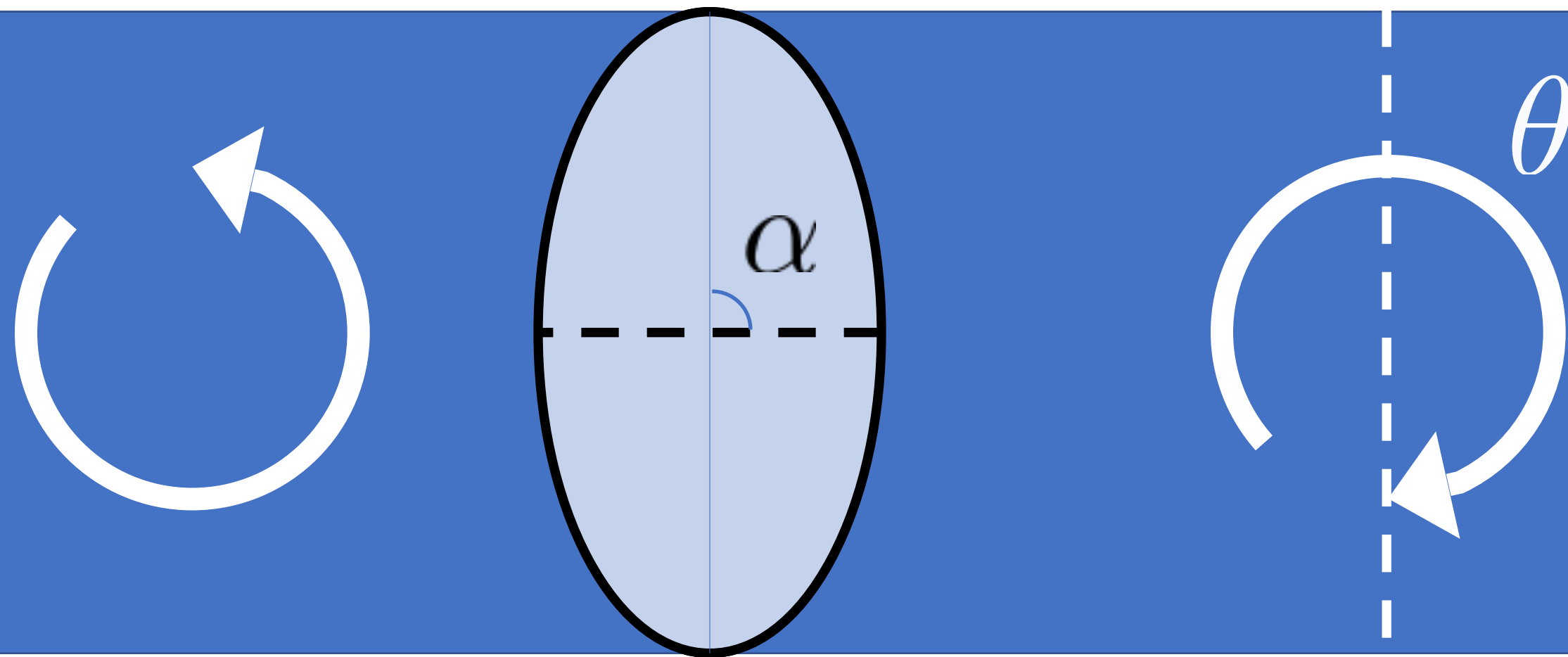
Geometric phase



Geometric phase



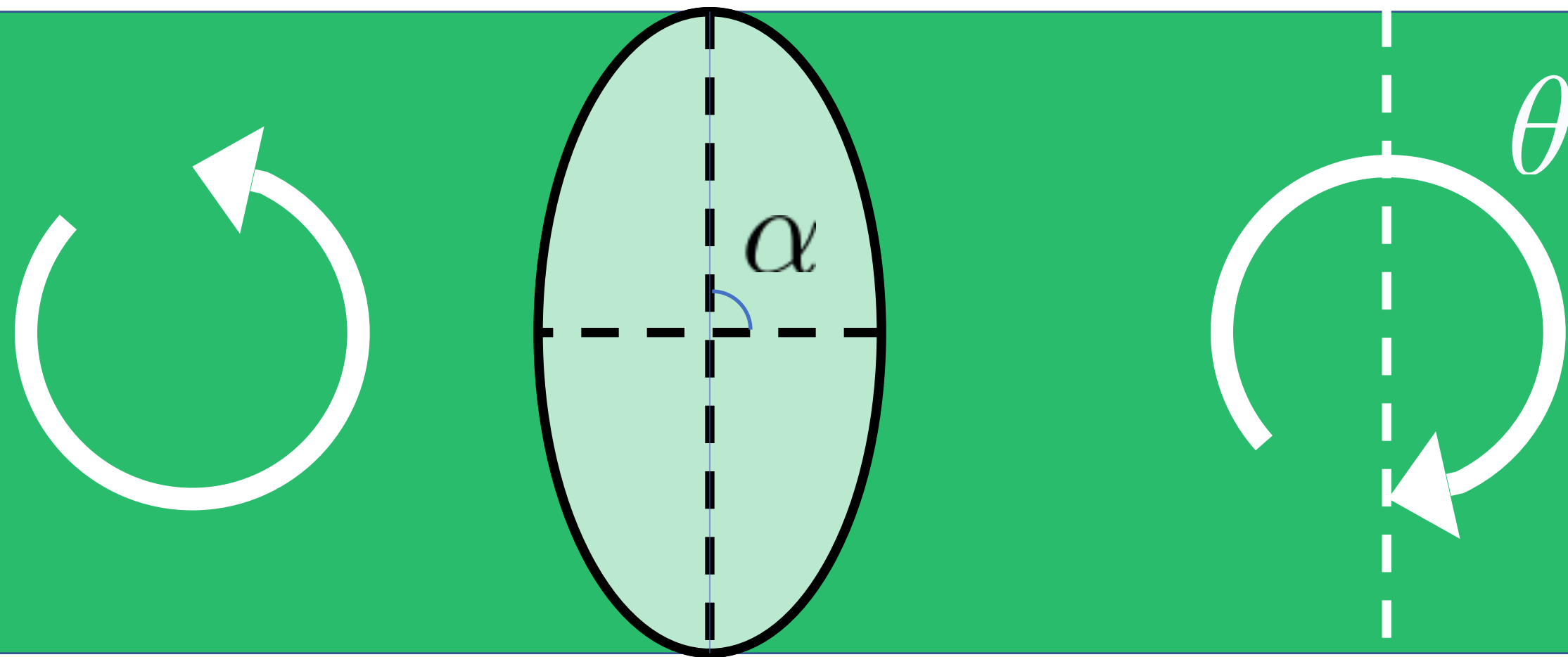
Geometric phase



The diagram illustrates the geometric phase. It consists of three main parts: a circular path with a counter-clockwise arrow on the left, a sphere in the center with a dashed horizontal line and a vertical line, and an angle α marked between the dashed line and the vertical line. To the right, a circular path with a clockwise arrow is shown, with an angle θ marked between the vertical line and the path.

$$\theta = \pm 2\alpha$$

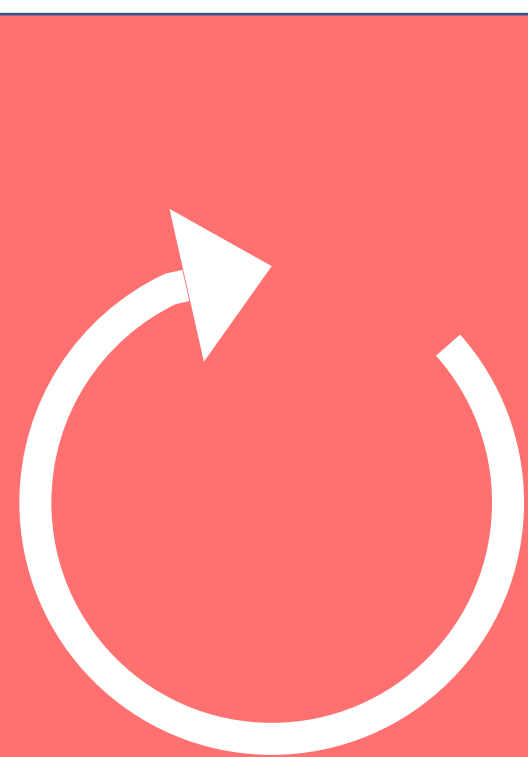
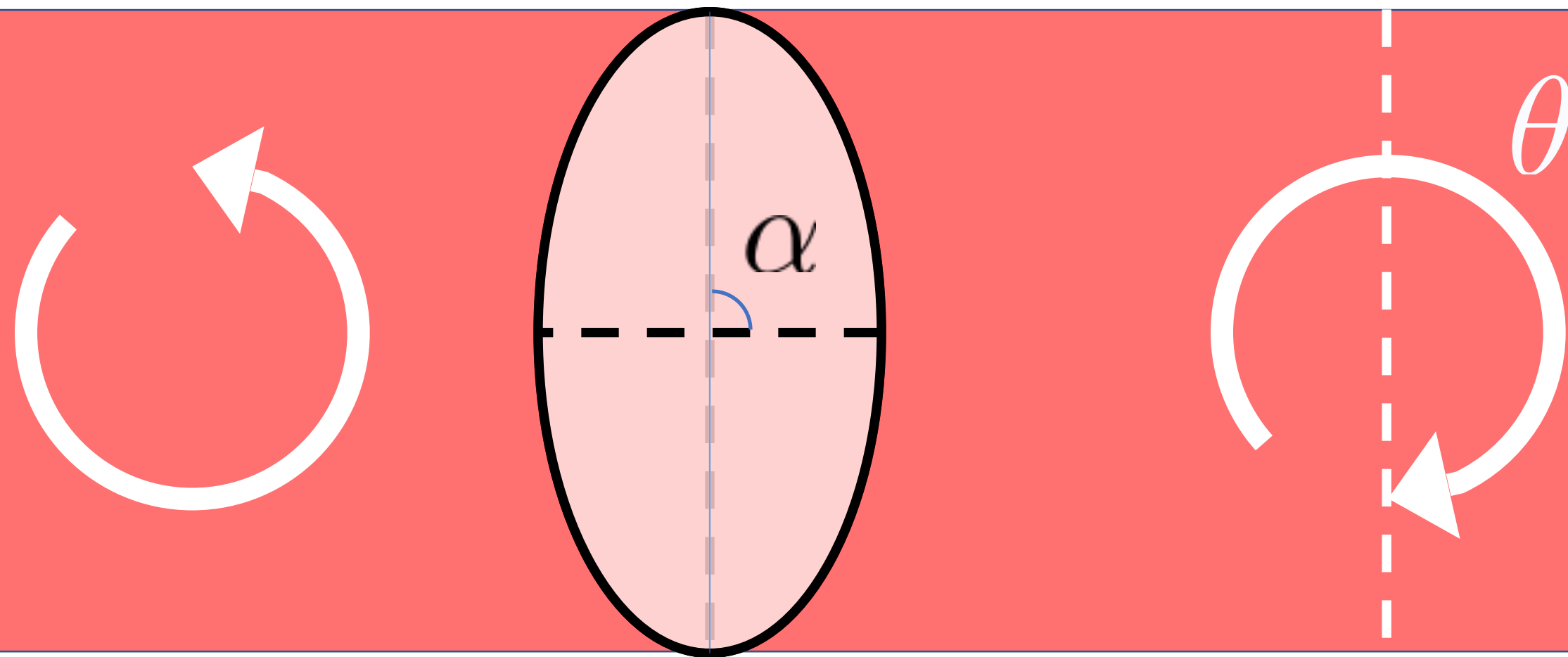
Geometric phase



The diagram illustrates the geometric phase. It consists of three parts: a circular path with a counter-clockwise arrow, a sphere with a dashed vertical axis, and a circular path with a clockwise arrow labeled θ .

$$\theta = \pm 2\alpha$$

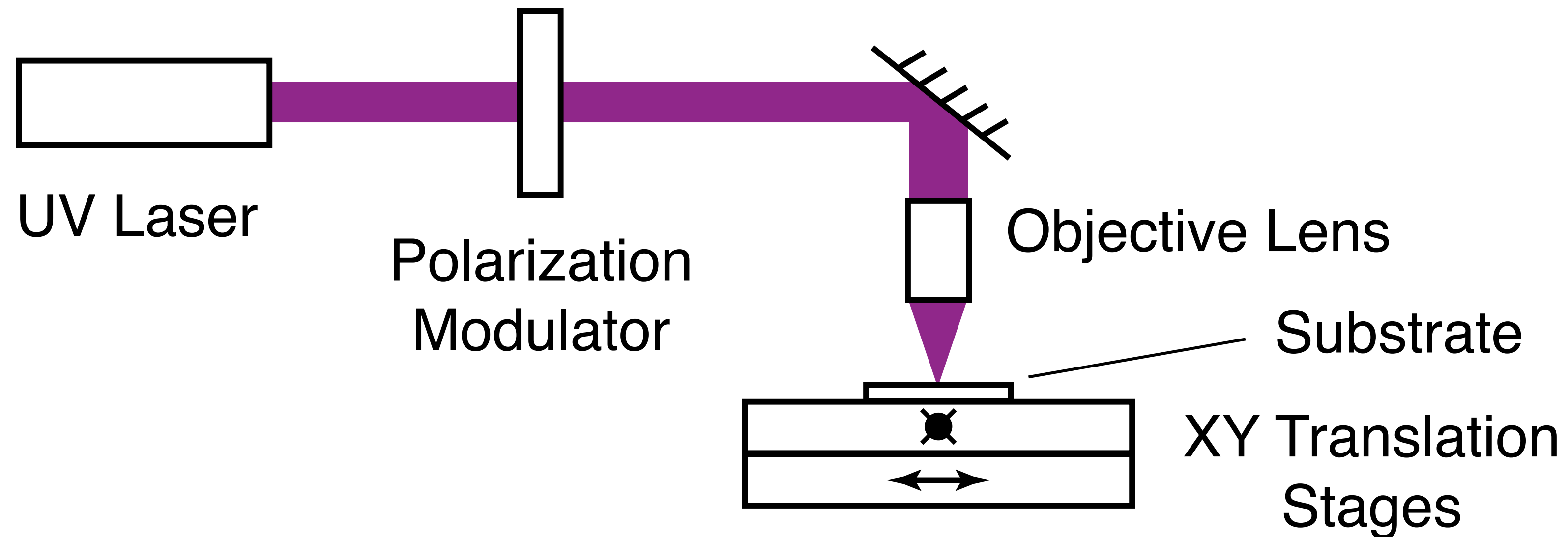
Geometric phase



$$\theta = \pm 2\alpha$$

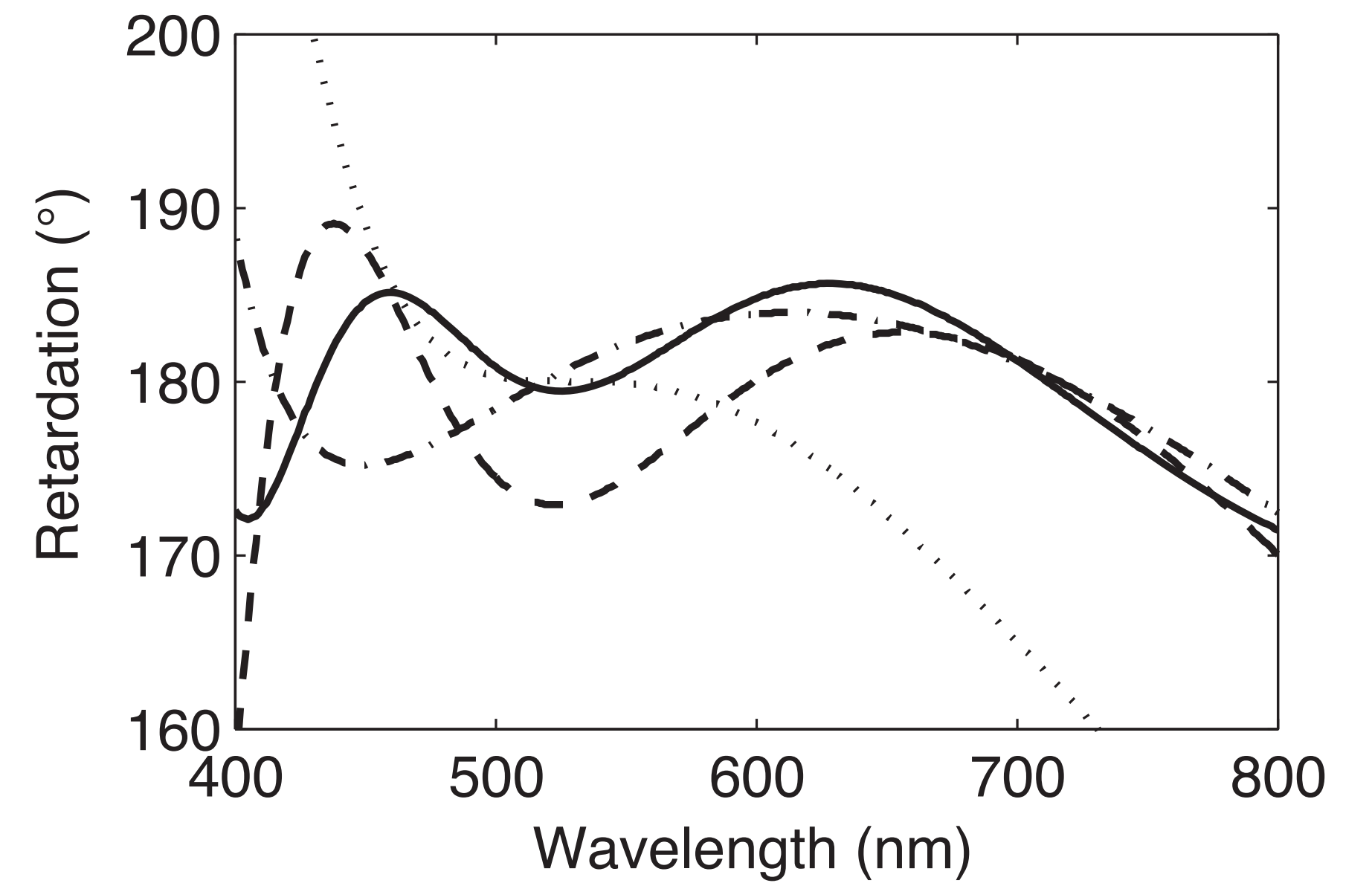
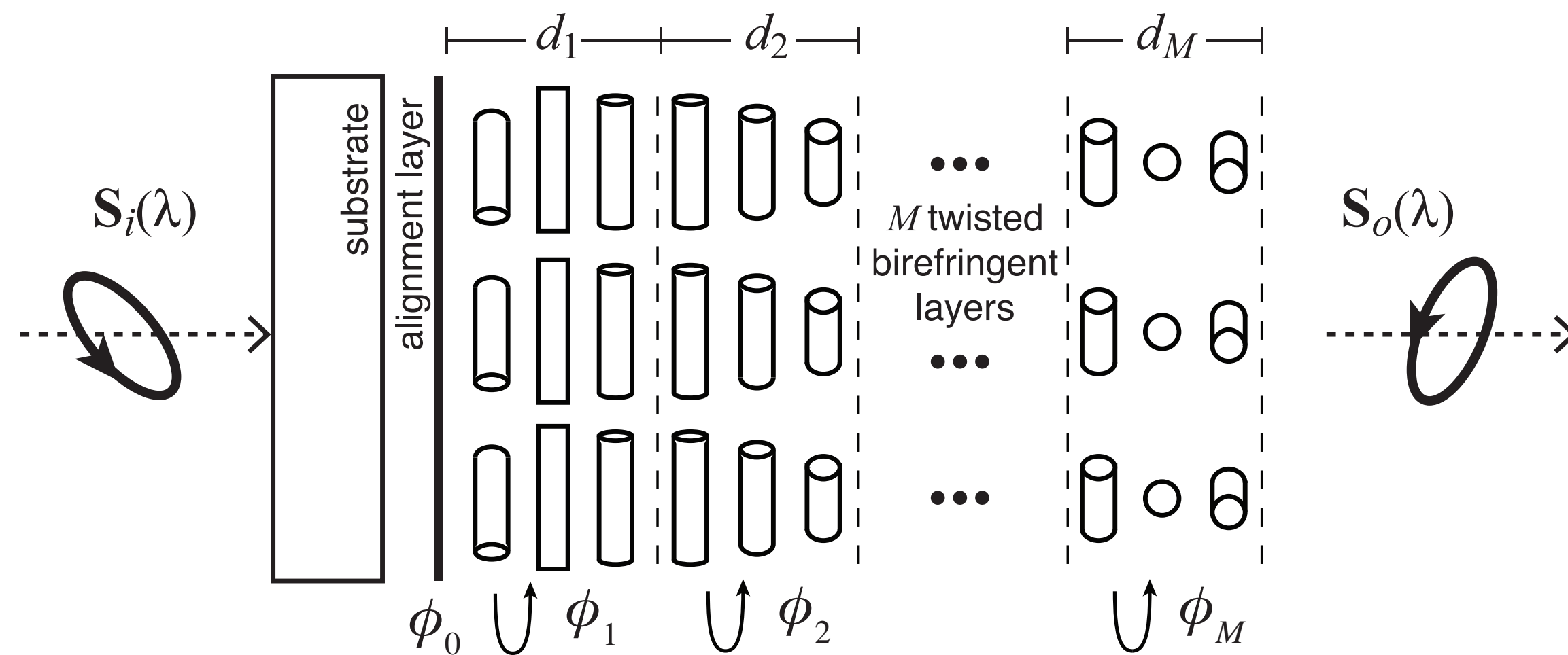
liquid-crystal freeform optics

1. any phase pattern thanks to direct-write technique



liquid-crystal freeform optics

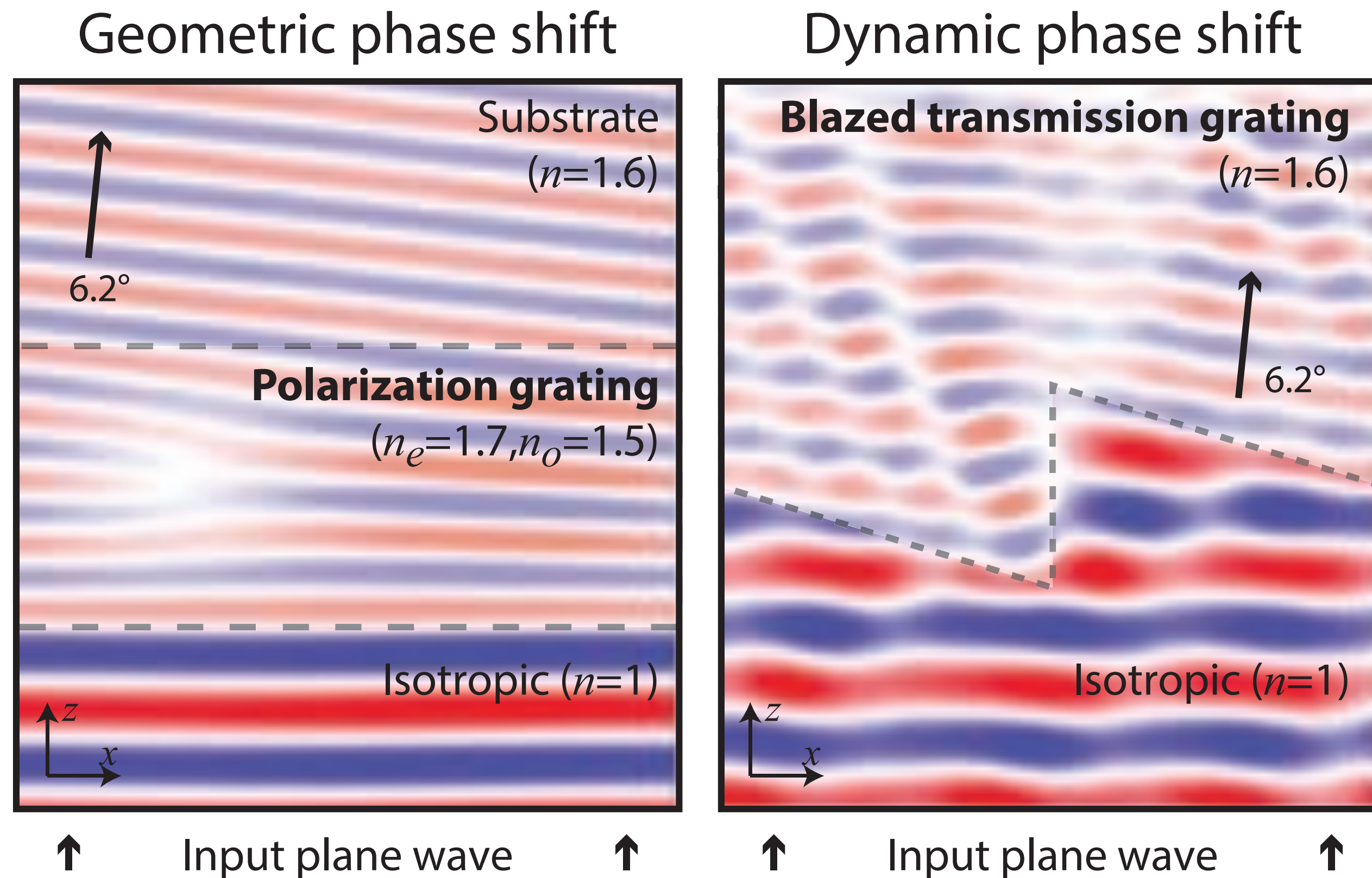
2. achromatization thanks to self-aligning multi-twist liquid crystal retarder



Komanduri et al.
(2013)

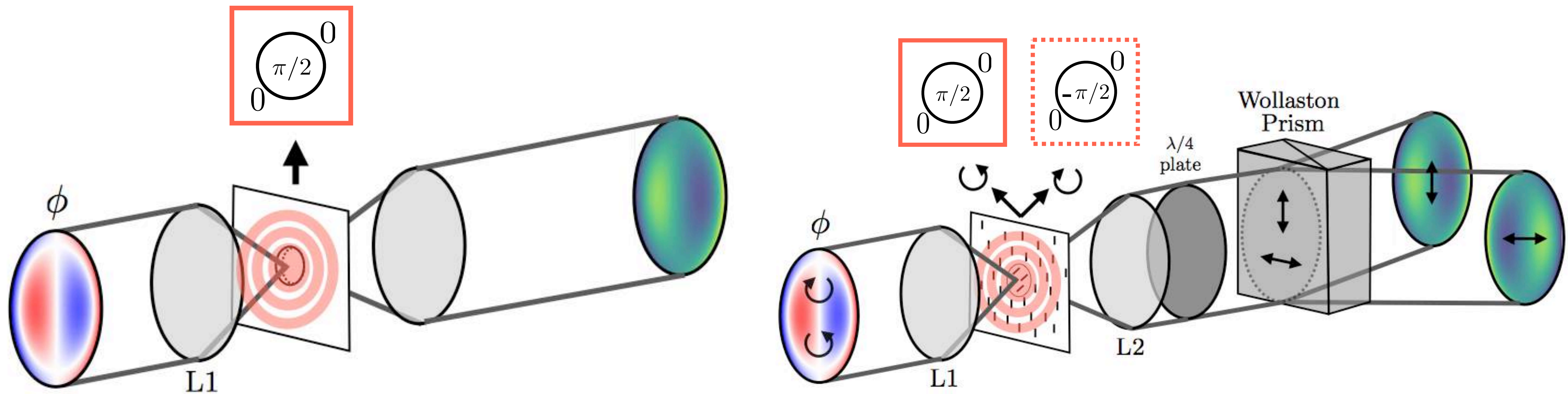
liquid-crystal freeform optics

3. very local and efficient phase ramps

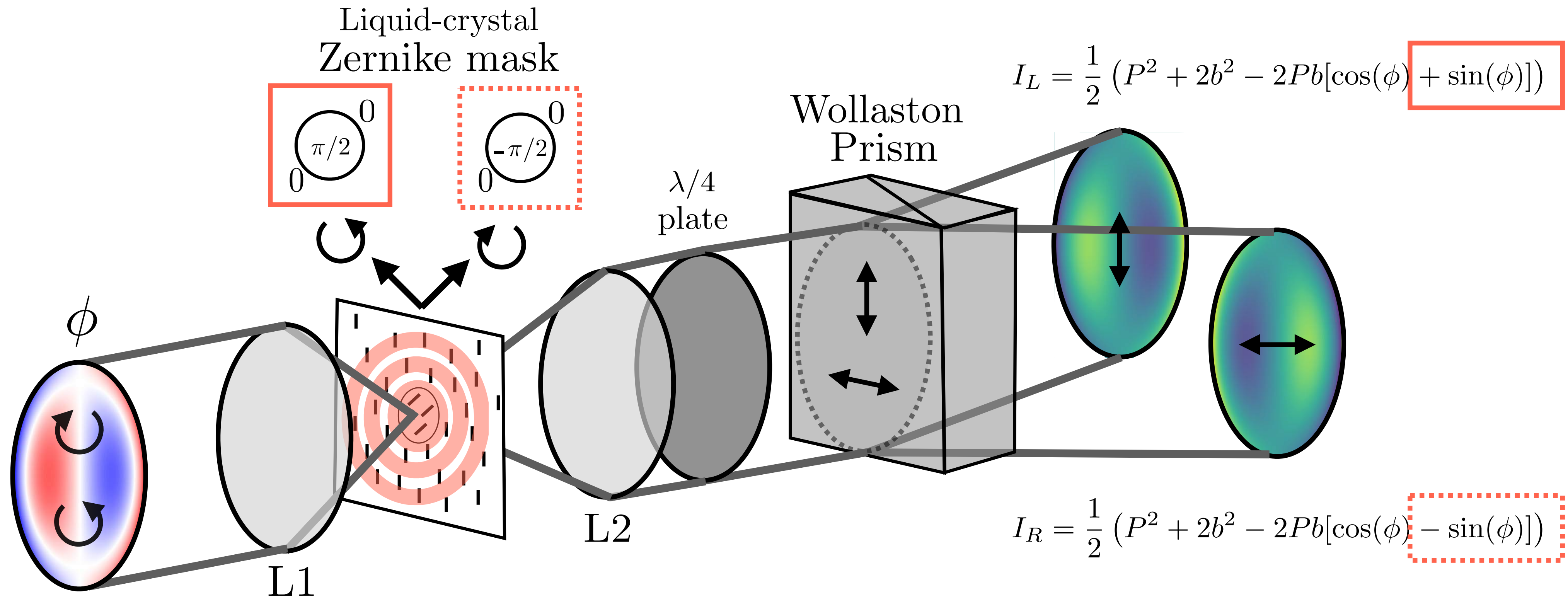


Escuti et al. (2016)

The vector-Zernike wavefront sensor



Wavefront reconstruction theory



Wavefront reconstruction theory

Incoming wavefront

$$\Psi_A = Pe^{i\phi} = P_0(1 - \epsilon)e^{i\phi}$$

Pupil intensities

$$I_L = \frac{1}{2}(P^2 + 2b^2 - 2Pb[\cos(\phi) + \sin(\phi)])$$

$$I_R = \frac{1}{2}(P^2 + 2b^2 - 2Pb[\cos(\phi) - \sin(\phi)])$$

$$b = \widehat{M} \otimes \Psi_A \simeq \sqrt{S}\widehat{M} \otimes P_0 = \sqrt{S}b_0$$

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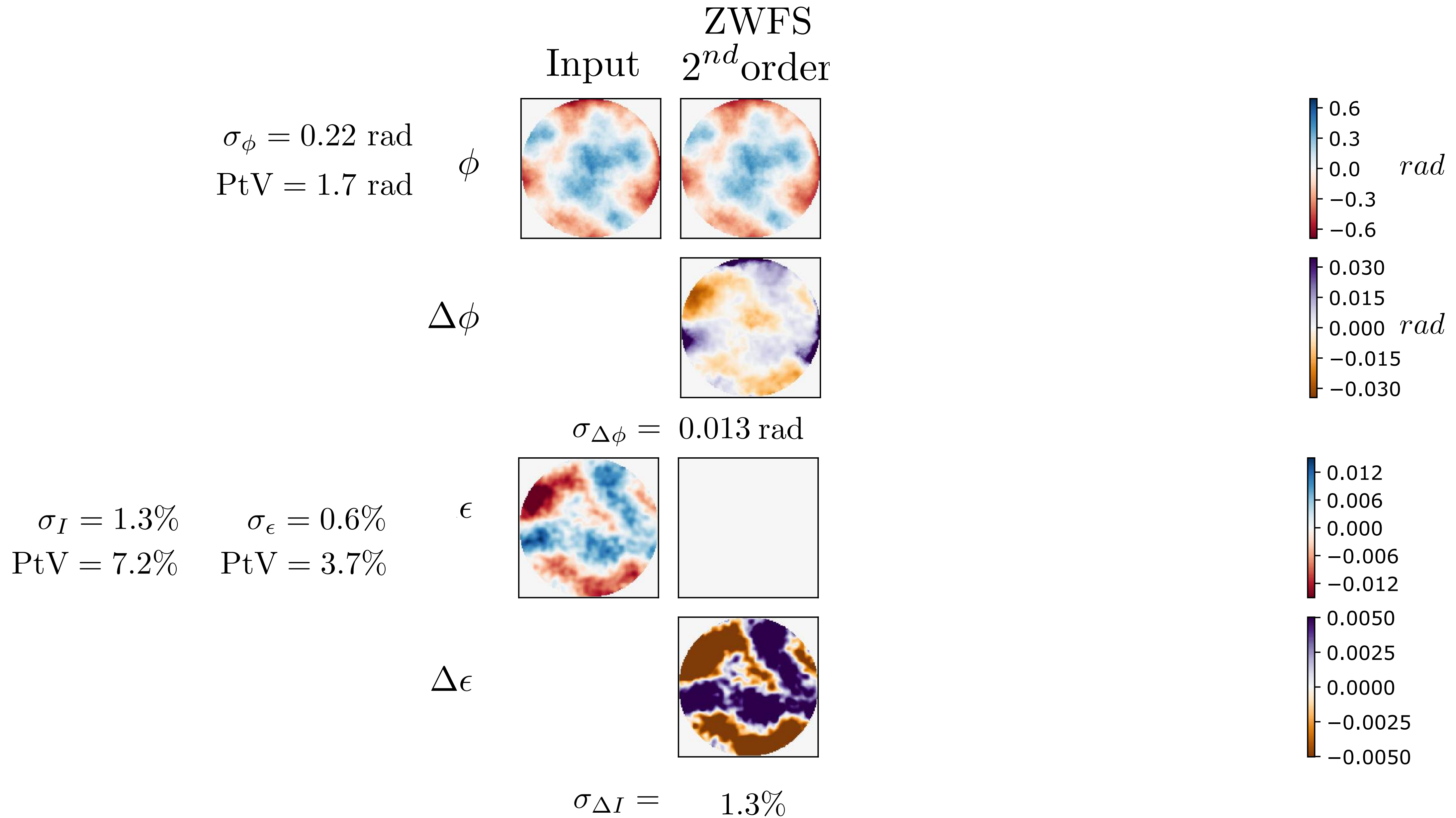
Reconstruction

$$P = \sqrt{I_R + I_L + \sqrt{4b^2(I_R + I_L) - (I_R - I_L)^2 - 4b^4}}$$

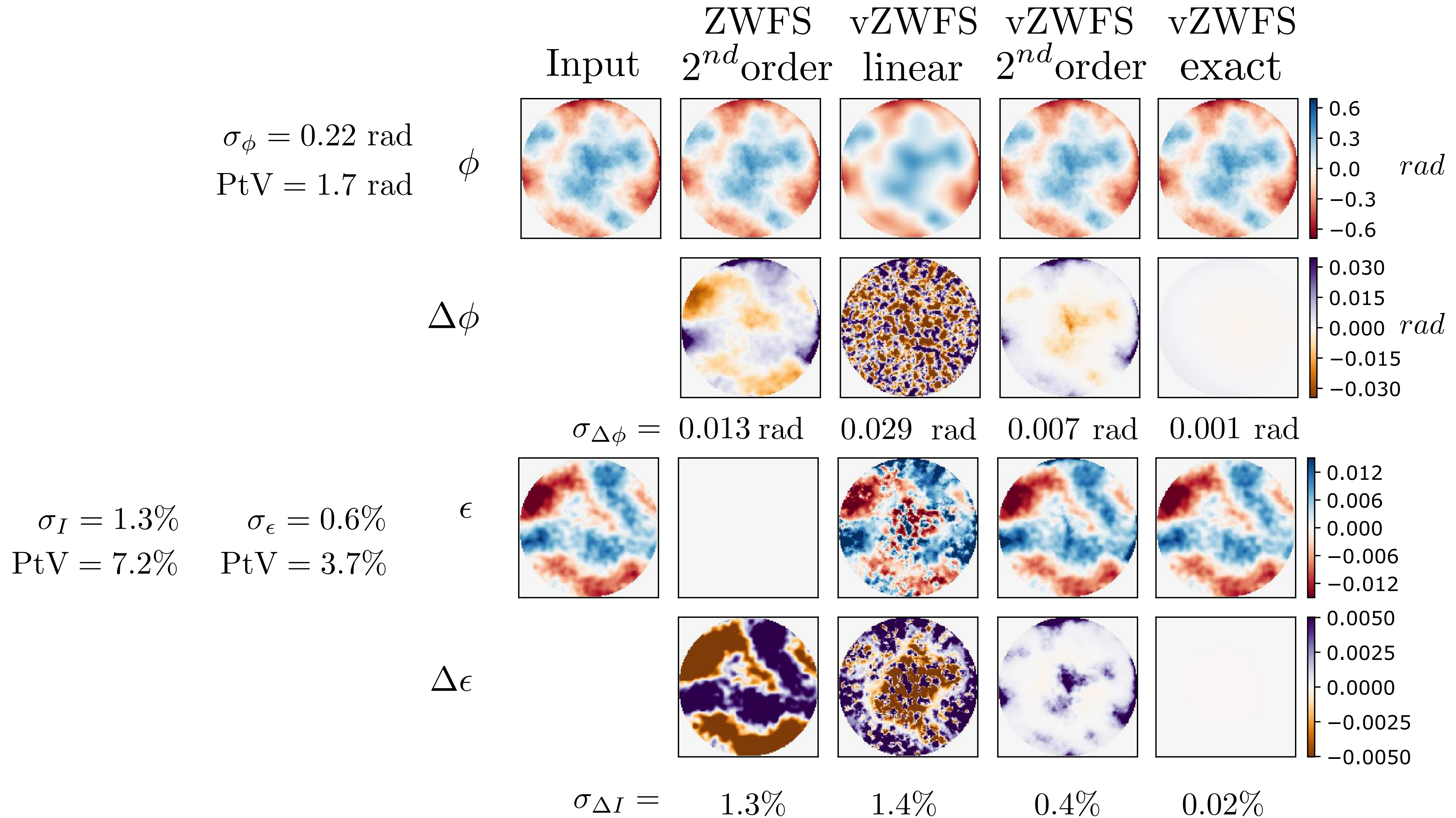
$$\phi = \arcsin\left(\frac{I_R - I_L}{2Pb}\right)$$

Nested solution! -> approximate with b_0 and iterate

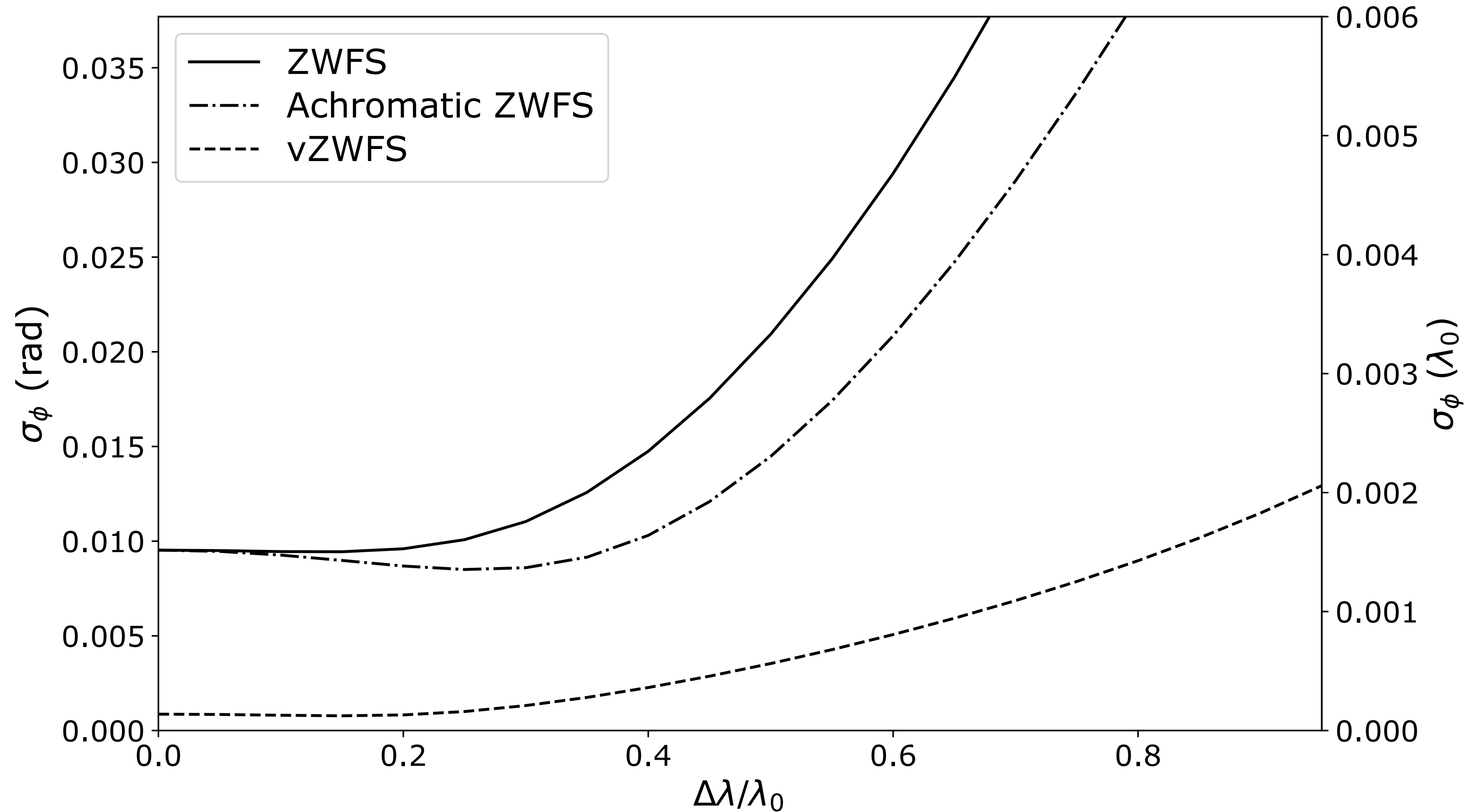
Simultaneous phase and amplitude reconstruction



Simultaneous phase and amplitude reconstruction



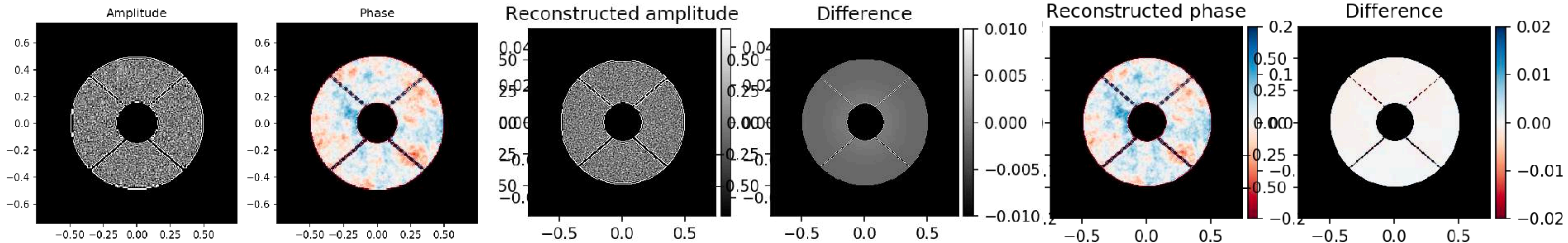
Broadband performance



HCIPy polarization update

```
vZWFS_ideal = VectorZernikeWavefrontSensorOptics(pupil_grid, num_pix=128)
```

```
amp_est, phase_est = reconstructor(vZWFS_ideal(wf_new))
```

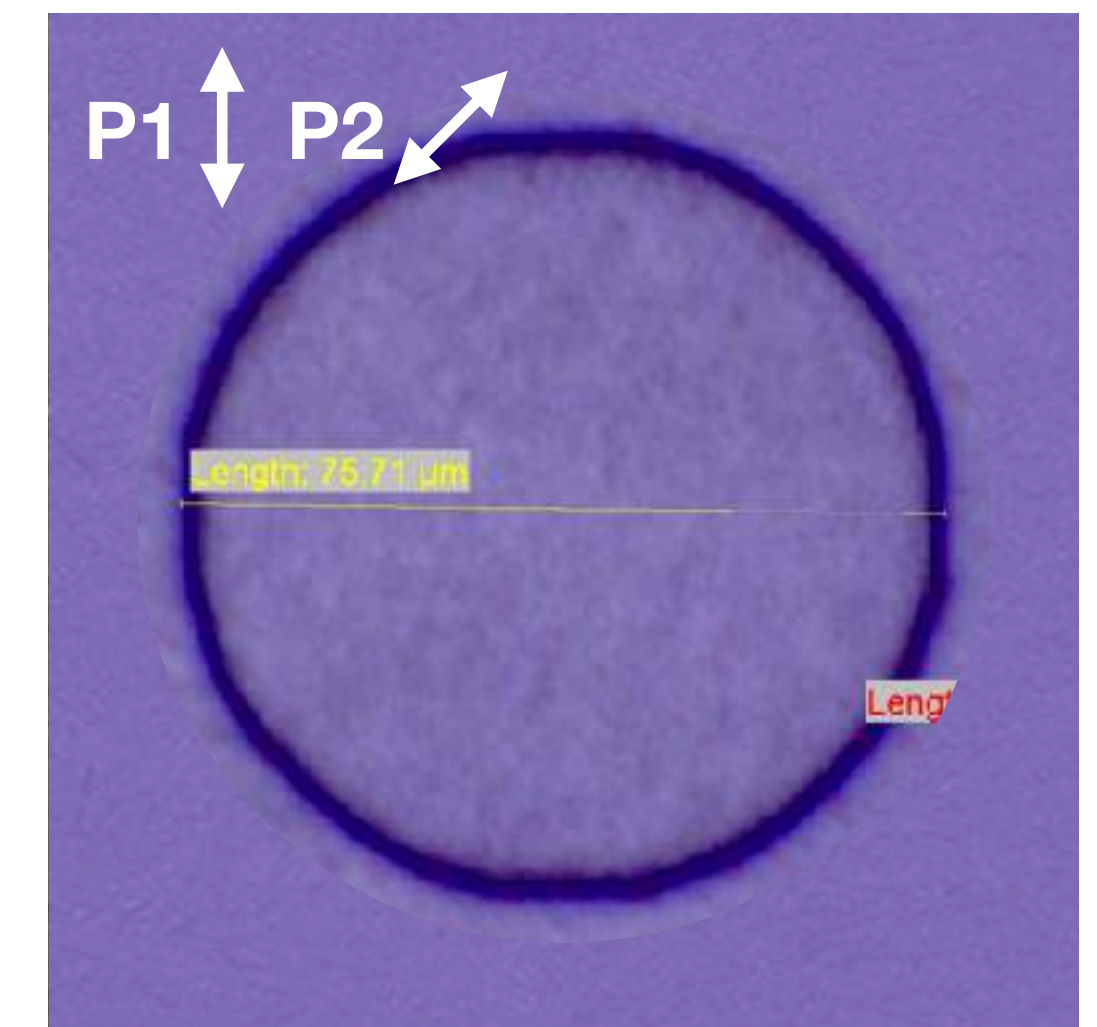
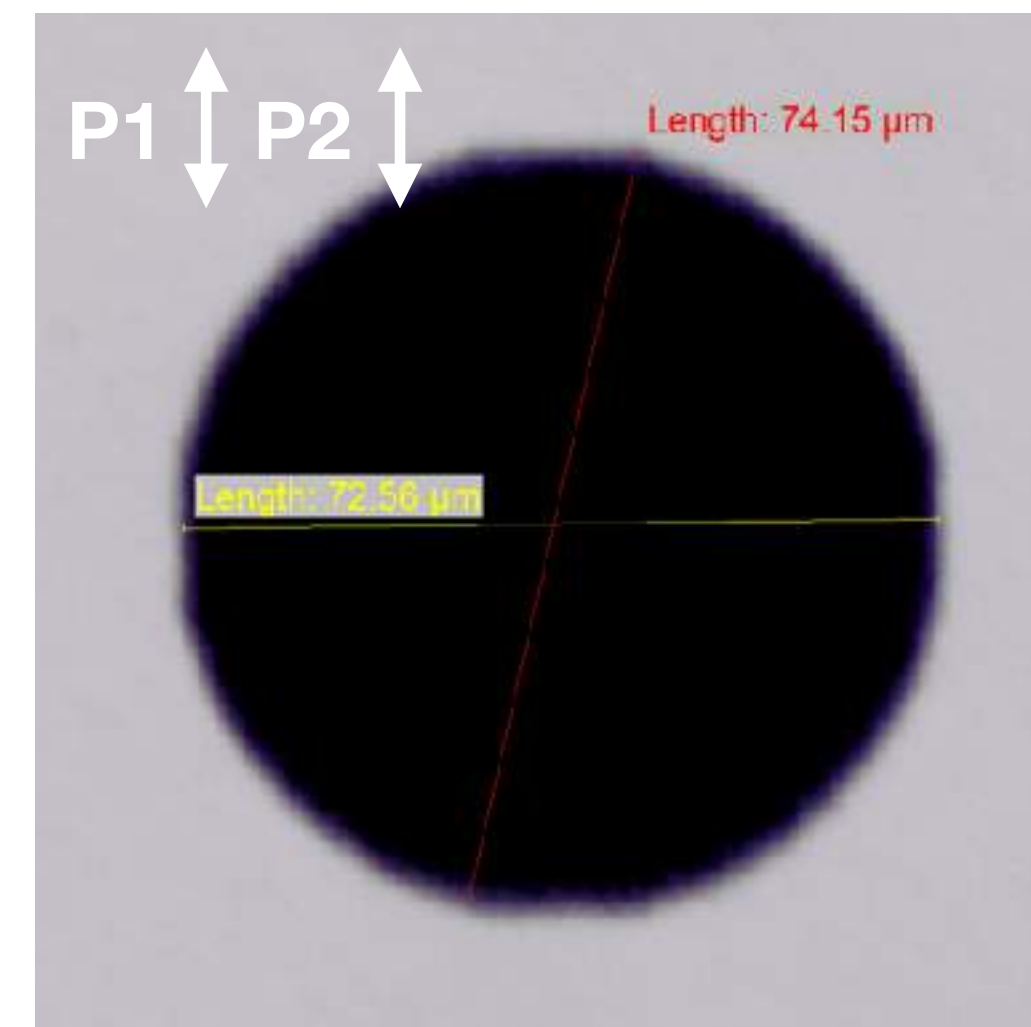
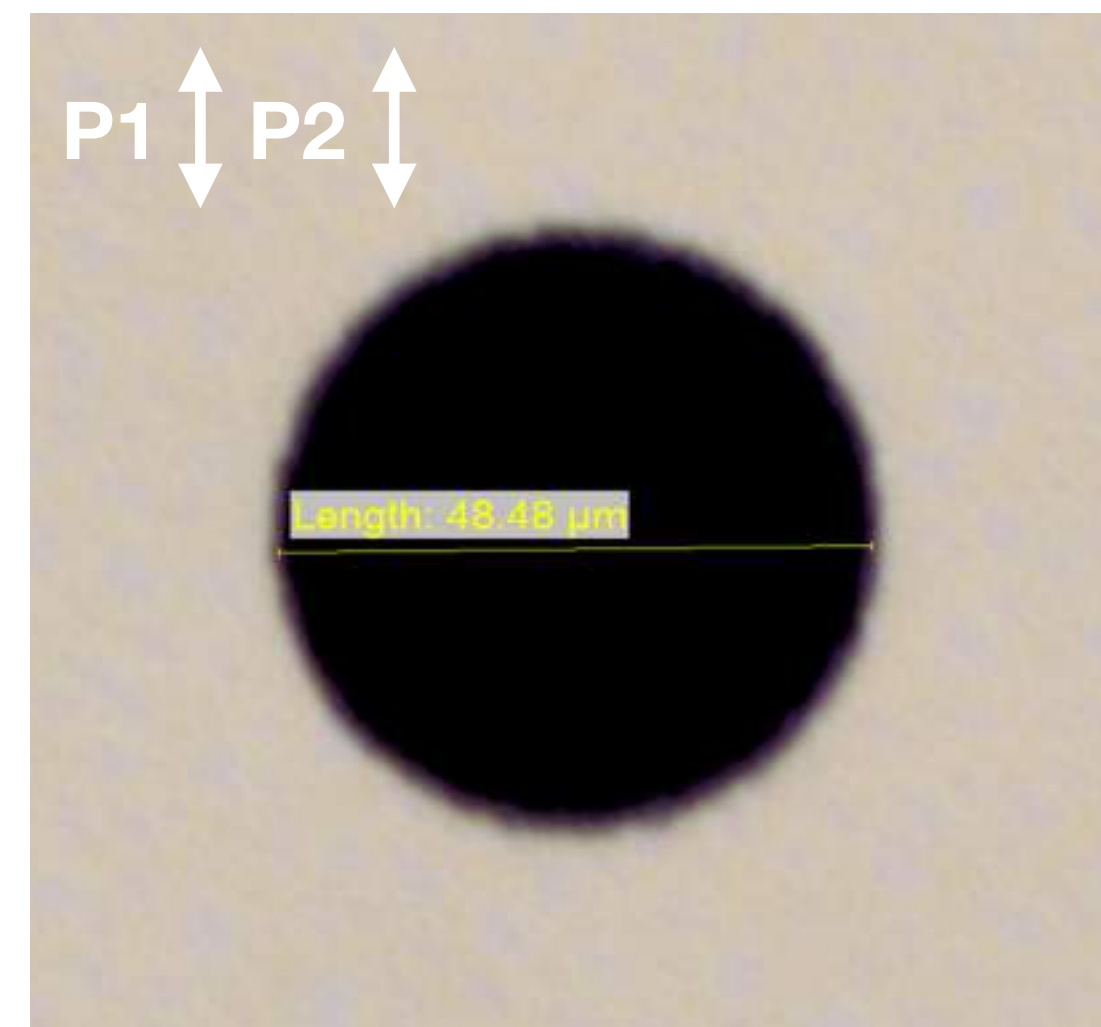
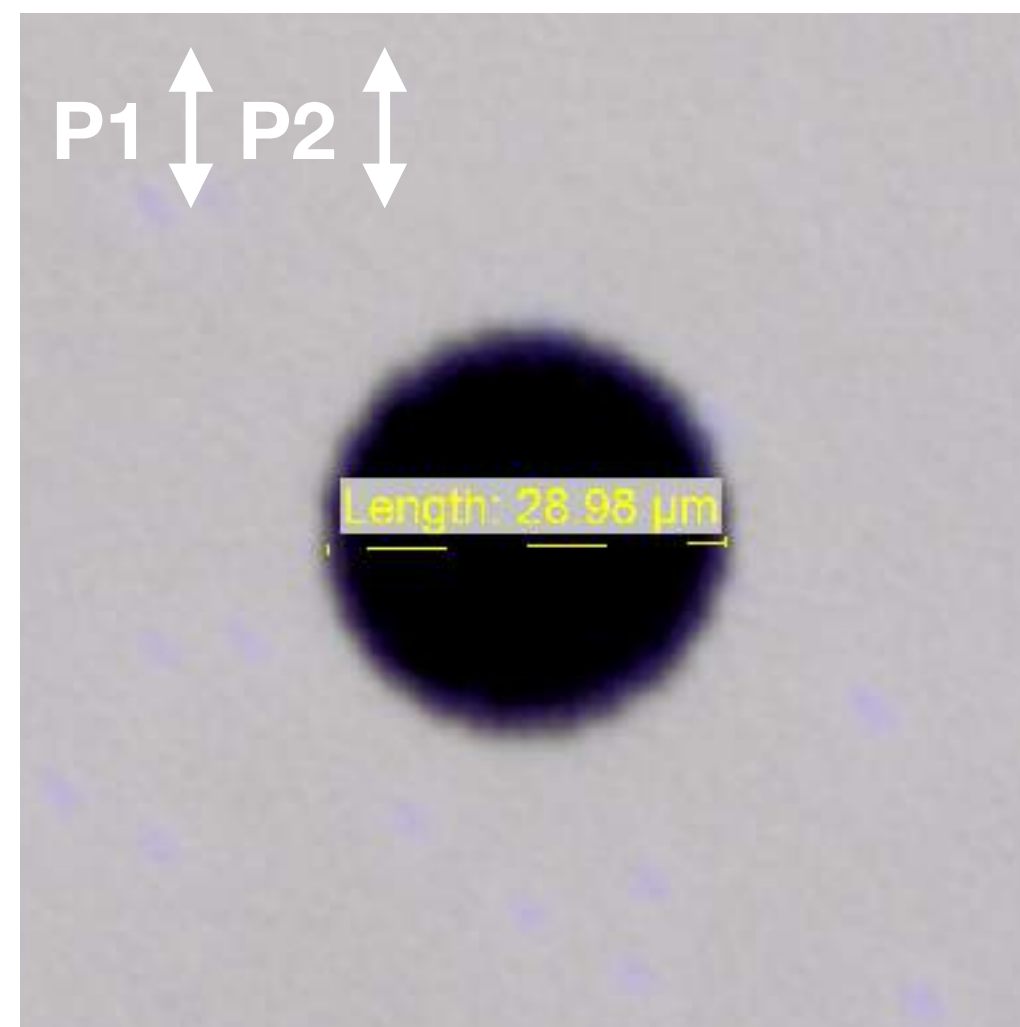


<https://github.com/ehtpor/hcipy>

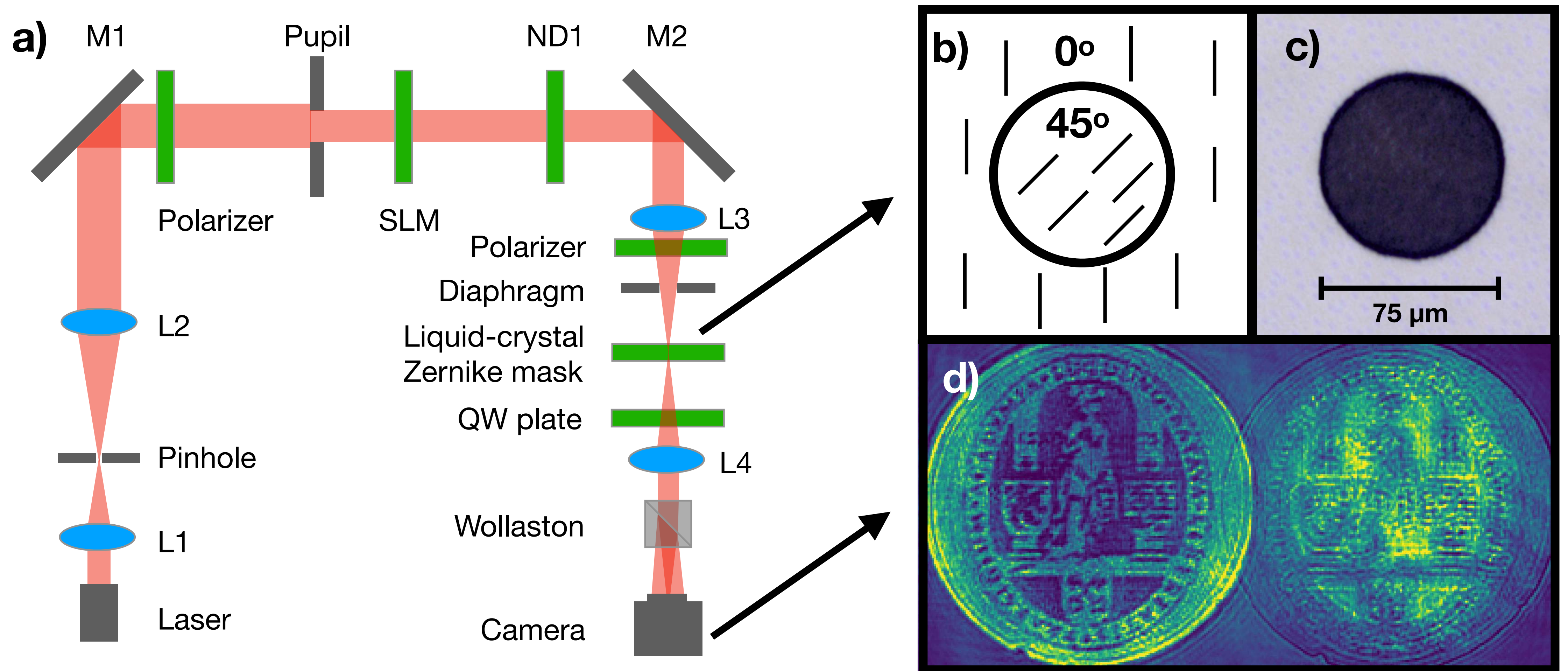
docs.hcipy.org

Manufacturing of the vZWFS

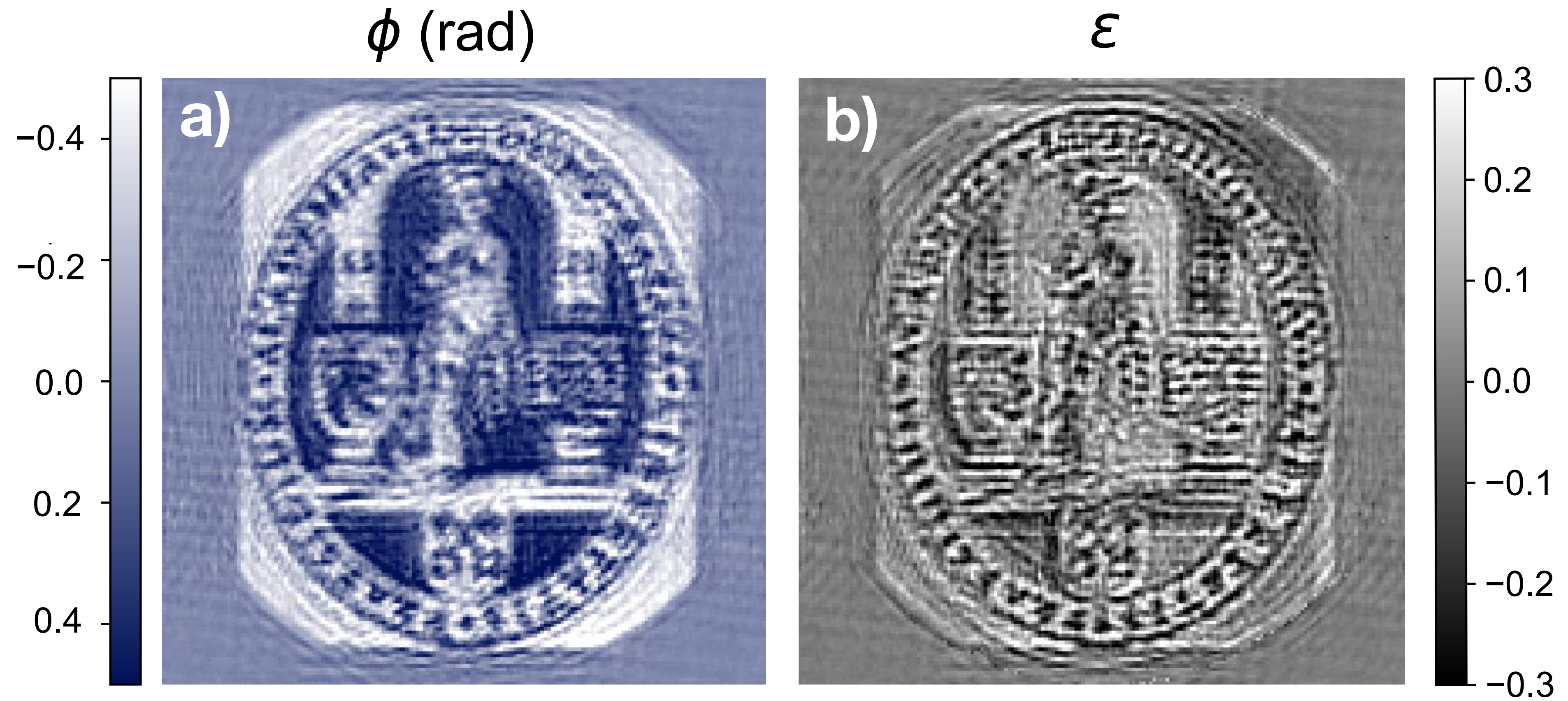
- Manufacturing by the “Geometric Phase Lab” at the North Carolina State University, in collaboration with ImagineOptix
- Manufactured three vZWFS on the same substrate, each with a differently sized dot (30, 50, 70 micron)
- Single non-twisted liquid-crystal layer with a retardance that is half-wave at 633 nm



Lab demonstration

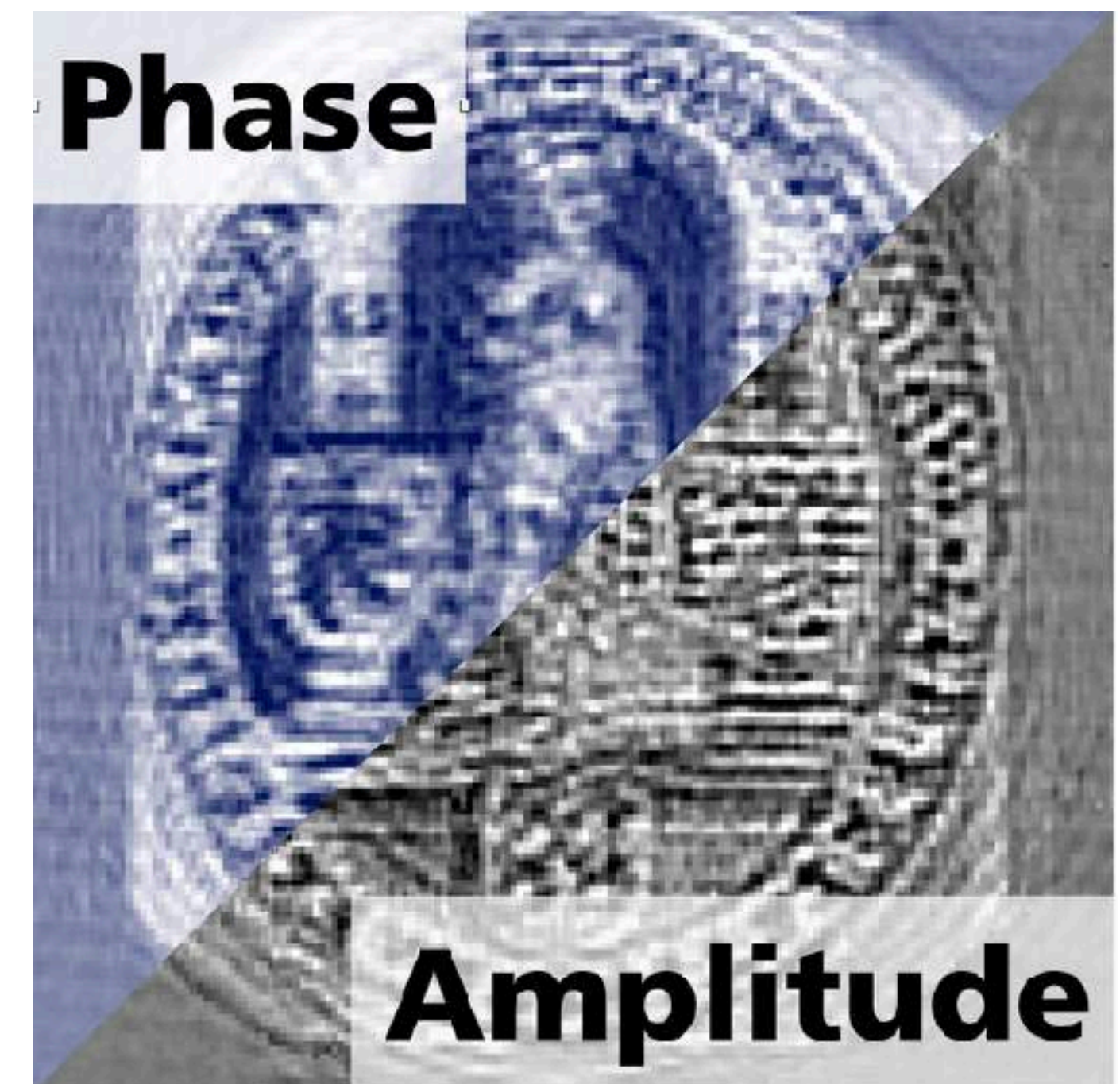


Lab demonstration



Conclusions

- The liquid-crystal vector-Zernike wavefront sensor is a simple yet powerful upgrade of the classical ZWFS
- A liquid-crystal Zernike mask applies a $-\pi/2$ and $\pi/2$ phase offset simultaneously
- By separating circular polarisation states, the vZWFS is capable of measuring phase and amplitude simultaneously
- The vZWFS has accurate reconstruction over a larger bandwidth than the ZWFS
- The vZWFS is included in the new polarization module of HCIPy.



Crazy idea

- Add grating pattern to vZWFS phase
- Splits the beam in a $-\pi/2$, $\pi/2$ and 0 (polarization leakage)
- Polarization leakage could be used as absolute reference for the pupil intensity, and solve for b
- Or, depending on retardance, only small amount of light could be split into separate pupils. Most of the light can go into the leakage term, and be used for science
- Downside: the grating smears out the pupil, only small bandwidths possible.

