# Hardware Demonstration of Starshade Formation Flying

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## Objectives:

 To experimentally validate formation sensing and control algorithms while maintaining high contrast with a flight-like starshade

## Our approach:

- Princeton starshade testbed
- Pupil image sensor of diffraction pattern
- Discrete-time control and estimation

## Formation flying in starshade technology?



In science mode:

- The width of the deep of starshade's shadow depends on:
  - size of the starshade
  - separation distance
- The width can be resized but at a cost

Thus, better formation-keeping performance helps to maximize the scientific yield.

## **Position Sensing**

- Technology development needed in position sensing
  - Need position accuracy < 10 cm
  - Centimeters over 10,000's kilometers separation is sub-mas angular measurement
- We can exploit nature of diffraction to avoid angular measurement
- Starshade's diffraction pattern moves one-to-one with starshade position over large distance
- Out-of-band light is bright and generates distinct Poisson spot – provides good guiding signal
- Pupil image is direct measurement of diffraction pattern

- Lateral Sensing technology gap at TRL 5 (as of Nov 2018)
- SLATE testbed at JPL demonstrated position sensing accuracy < 30 cm and control accuracy < 1 m (flight equivalent)
- See Milestone #4 Report by Flinois, Bottom, et al. (2018)
- Excellent work validating concept and showing robustness of sensing + control scheme
- Optical performance limited by small starshade and collimating optics

## Opportunity with Princeton testbed

- Existing testbed with flight-representative starshade
- ◎ Optical performance validated to 10<sup>-10</sup> contrast level
- Can validate formation sensing and high contrast simultaneously
- Realistic optical performance allows exploration of new sensing techniques
- Starshade alignment with out-of-band light already used in high-contrast experiments
- ◎ Can be used for TRL 6+ work

#### Princeton Starshade Testbed



Starshade diameter: 26 mm Science channel:  $\lambda = 641$  nm Guiding channel:  $\lambda = 405$  nm



## Formation Flying

## The formation flying problem



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## Control and estimation diagram Feedback control loop



## The N-body problem for relative motion The leader spacecraft:

$$\ddot{\mathbf{r}}_{L} = -\sum_{i=1}^{N} \mu_{i} \left( \frac{\mathbf{r}_{Li}}{\|\mathbf{r}_{Li}\|^{3}} \right) + u_{L} \quad \text{for} \quad i = 1, 2, ...N$$
(1)

The follower spacecraft:

$$\ddot{\mathbf{r}}_F = -\sum_{i=1}^N \mu_i \left( \frac{\mathbf{r}_{Fi}}{\|\mathbf{r}_{Fi}\|^3} \right) + u_F \quad \text{for} \quad i = 1, 2, ...N$$
(2)

The term  $u_X$  correspond to control inputs.

## Equations of Motion

The relative motion is  $x = r_F - r_L$ 

$$\ddot{x} = -\sum_{i=1}^{N} \mu_i \left( \frac{\mathbf{r}_{Fi}}{\|\mathbf{r}_{Fi}\|^3} - \frac{\mathbf{r}_{Li}}{\|\mathbf{r}_{Li}\|^3} \right) + \Delta \mathbf{u} + \mathbf{w} \quad \text{for} \quad i = 1, 2, \dots N$$
(3)

 $\odot \boldsymbol{w} \sim \boldsymbol{\mathcal{N}} \left( \mu_{SRP}, \sigma \right)$  adds uncertainty (normal random noise)

- $\mu_{SRP}$  is the average of the differential acceleration caused by the solar radiation pressure
- According to the configuration of our laboratory, we assume:
  - The starshade is the leader in free motion
  - The telescope is the follower in controlled motion
  - Therefore  $\Delta u = u_F u_F = u_F$

Linear quadratic regulator with integral action





## Estimation Strategy

## Unscented Kalman filter



Other relevant features:

Approximates the actual motion as:

$$\ddot{x} = -\sum_{i=1}^{N} \mu_i \left( \frac{\mathbf{r}_{F_i}}{\|\mathbf{r}_{F_i}\|^3} - \frac{\mathbf{r}_{L_i}}{\|\mathbf{r}_{L_i}\|^3} \right) + \Delta u + z \sigma^{-0}$$

Fed by the sensors and the controller

#### **Pupil Sensor**

## Some background



- Deep shadow ~1m larger than telescope (in radius)
- Formation-keeping needs lateral position error ≤ 10 cm
- For 1000's km of separation it means milliarcsec measurement
- Direct sampling the one-to-one diffraction pattern of the starshade

#### **Pupil Sensor**



Starshade's diffraction pattern approximated by a Bessel function:

$$I(x,y) \approx J_0^2 \left( \frac{2\pi R \sqrt{(x-x_s)^2 + (y-y_s)^2}}{\lambda z} \right)$$
(4)

 $\odot$   $x_s$  and  $y_s$  solved via non-linear least squares

## Hardware-in-the-loop simulation features

- Intersatellite separation 26,000km
- ◎ For in-plane readings < 1m use pupil sensor
- ◎ For intersatellite separation and in-plane readings > 1m:
  - Star-tracking sensor
  - Normal distributed random signal with a ±5m error
- Target star is Epsilon Eridani
- Maximum thrust firing of 1N
- Simulation time 2 hour
- ◎ 10 celestial bodies from JPL's ephemeris DE432

### **Experiment Procedure**

- Start camera with initial misalignment
- Begin control loop...
  - Switch to pupil plane camera
  - Switch to out-of-band wavelength channel
  - Take pupil image and extract position
    - Or get position from noisy star tracker if at large offset
  - Generate control signal + move camera
  - Switch to focal plane camera
  - Switch to science-band wavelength channel
  - Take contrast image with focal plane camera

#### Results

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## Position error in the line-of-sight frame

- ◎ Starting offset: 50 m
- ◎ Median pupil sensor error: 16 cm



Results

## Control signals

 $\odot$  Total  $\Delta v = 0.89 \text{ m/s}$ 



- Ombination of an LQR+i and UKF
- High precision position sensing using a pupil image sensor
- ◎ Favorable performance includes:
  - Position error convergence within tolerances
  - Robust steady-state
  - Low values of total  $\Delta v$
- Initial results suggest the validity of formation flying approach in starshade technology

- Implement control scheme that maximizes observing time (minimizes thruster firings)
- Add beacon on starshade to do focal plane "retargeting" control
- Add control in "putting" region and implement proper sensor handoff
- Investigate position sensing in "putting" region
- Investigate other position extraction schemes (e.g., neural net)

## THANK YOU FOR YOUR ATTENTION lmmoreno@princeton.edu