

Vortex coronagraphs for segmented aperture space telescopes

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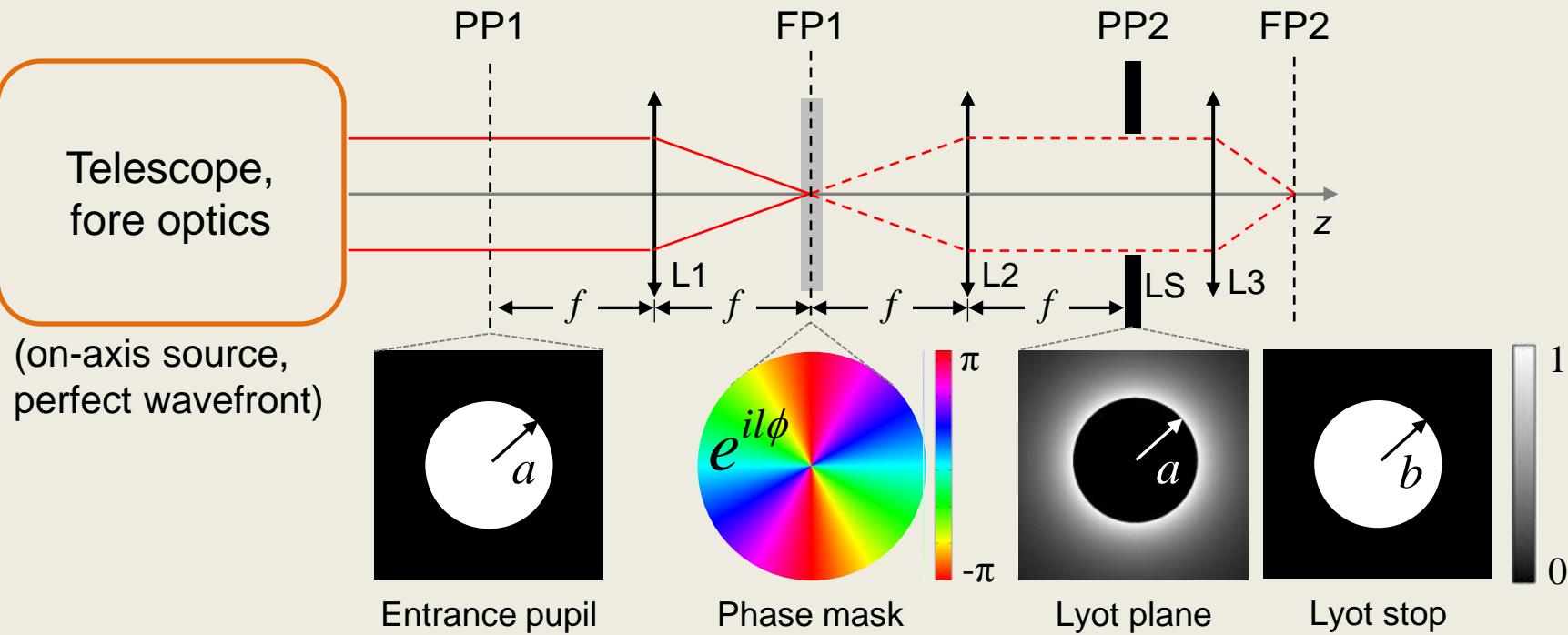
³Space Telescope Science Institute

Outline of talk

- 1. Background on vortex coronagraphs**
- 2. Optimization of coronagraphic masks**
- 3. Wavefront control with aperture discontinuities**
- 4. Outlook for future work**

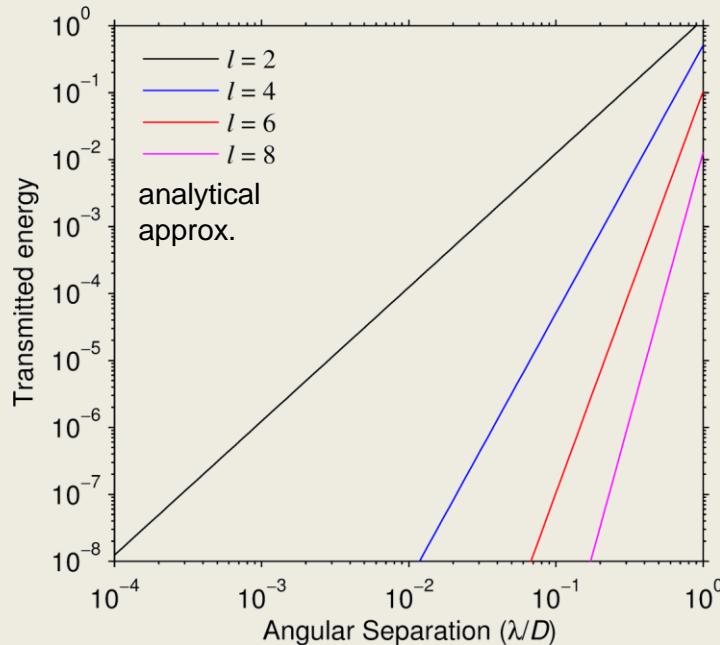
1. Background

The vortex coronagraph

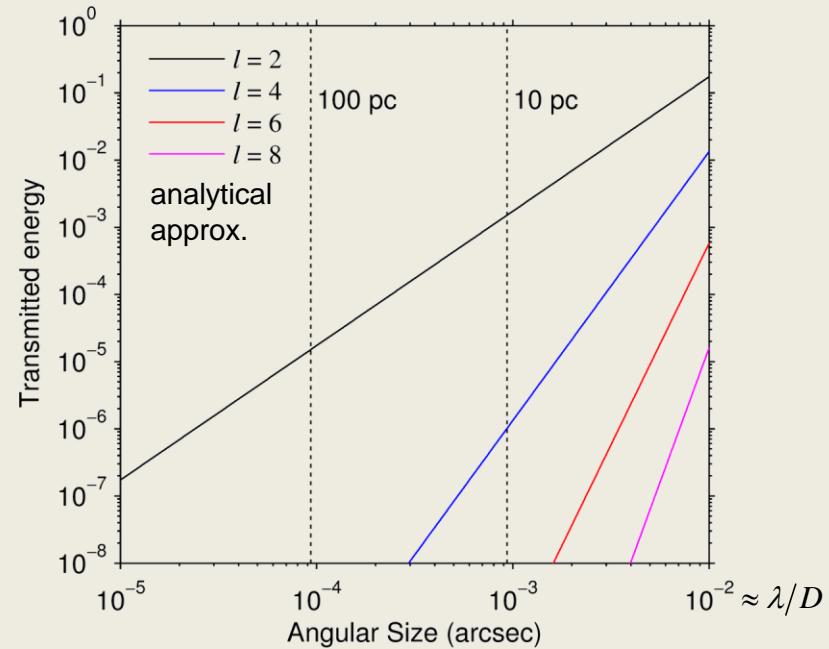


Focal plane vortex phase mask provides theoretically perfect starlight cancellation for an unobstructed, circular pupil and $l = 2, 4, 6, \dots$

Sensitivity to tip-tilt and finite sources



Fraction of energy transmitted through the Lyot stop for an off-axis point source.



Fraction of energy transmitted through the Lyot stop assuming a 12 m diameter aperture and $\lambda = 550$ nm.

Dashed lines indicate the size of a sun-like star at 10 and 100 pc.

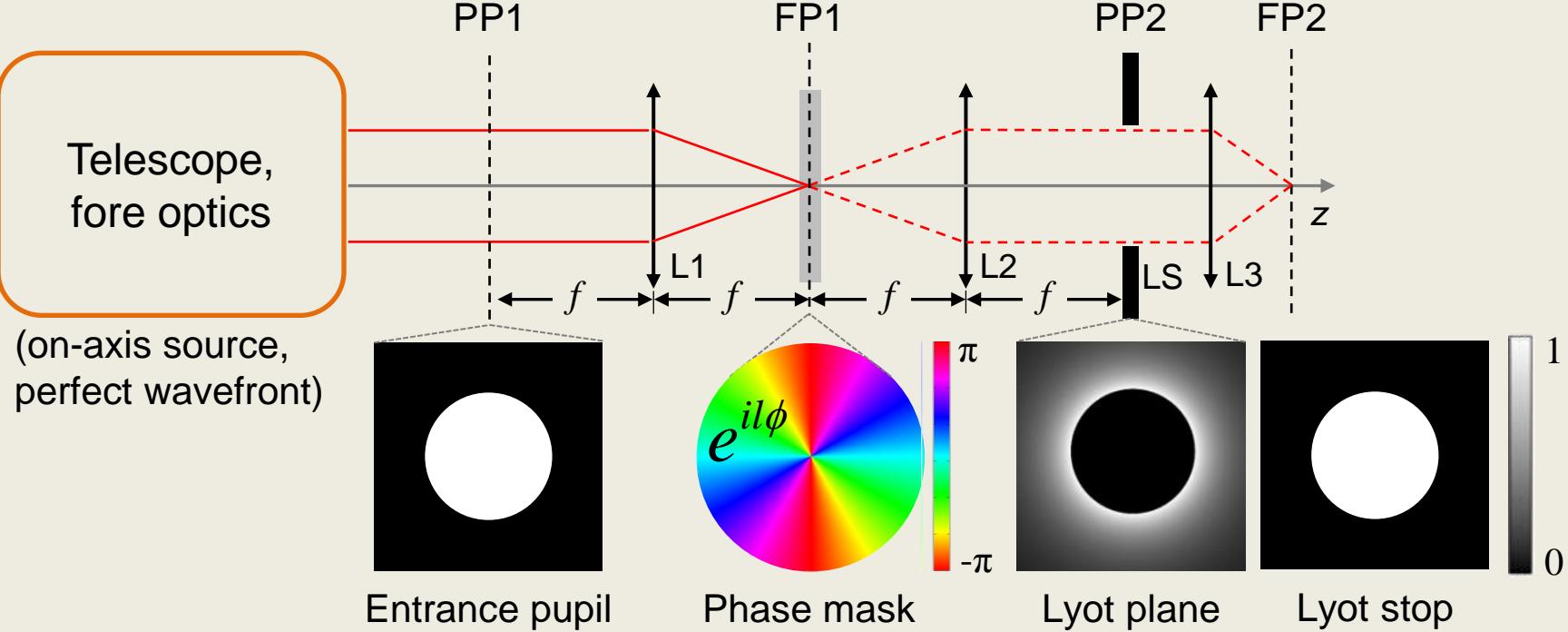
Need at least charge 4 for a 12 m space telescope

Guyon et al., *ApJS* **161** 81 (2006)

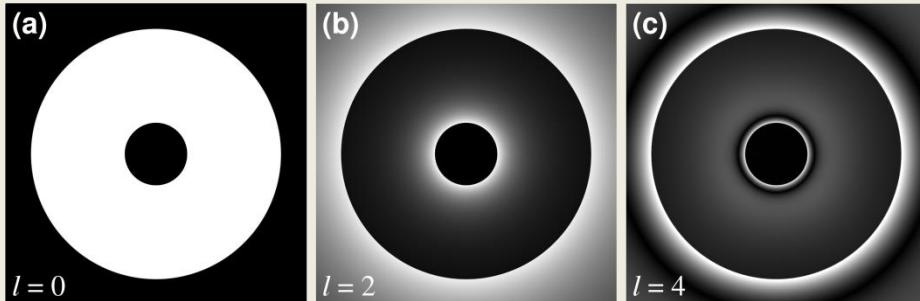
Jenkins, *MNRAS* **384** 515 (2008)

Mawet et al., *Proc. SPIE* 773914 (2010)

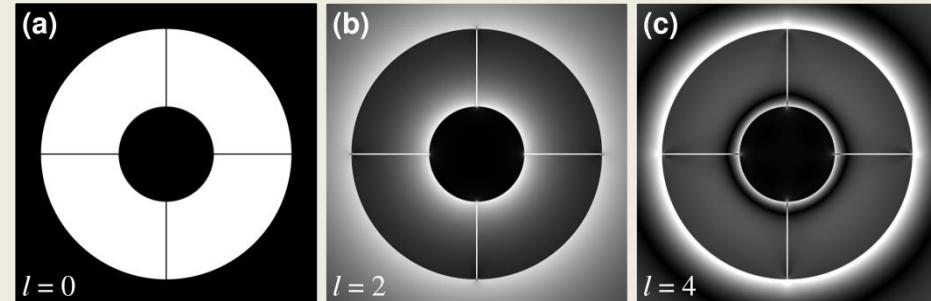
Sensitivity to aperture shape



Annular aperture

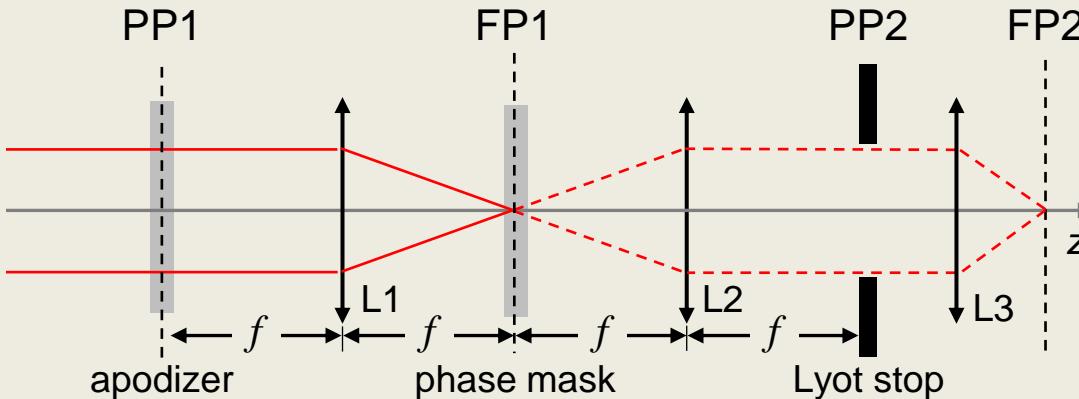


Annular aperture + spiders (Palomar)

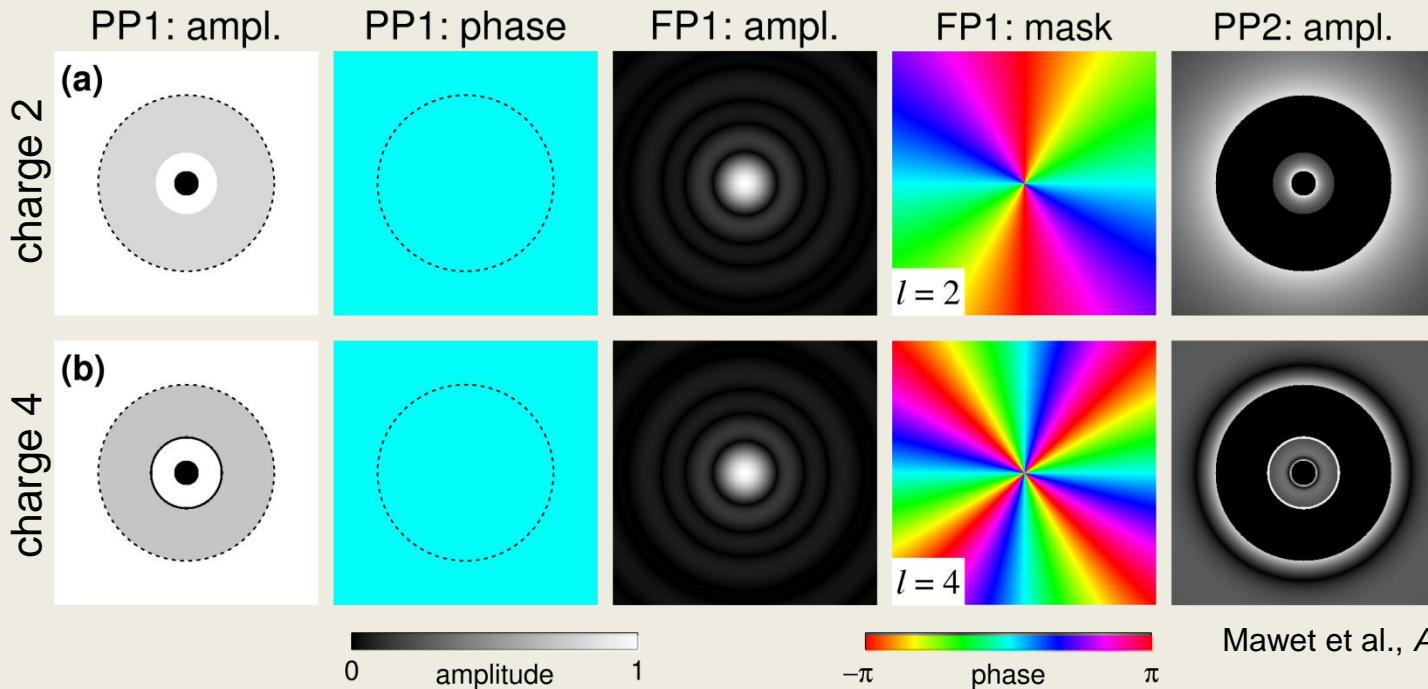


Need advanced designs for segmented aperture space telescopes

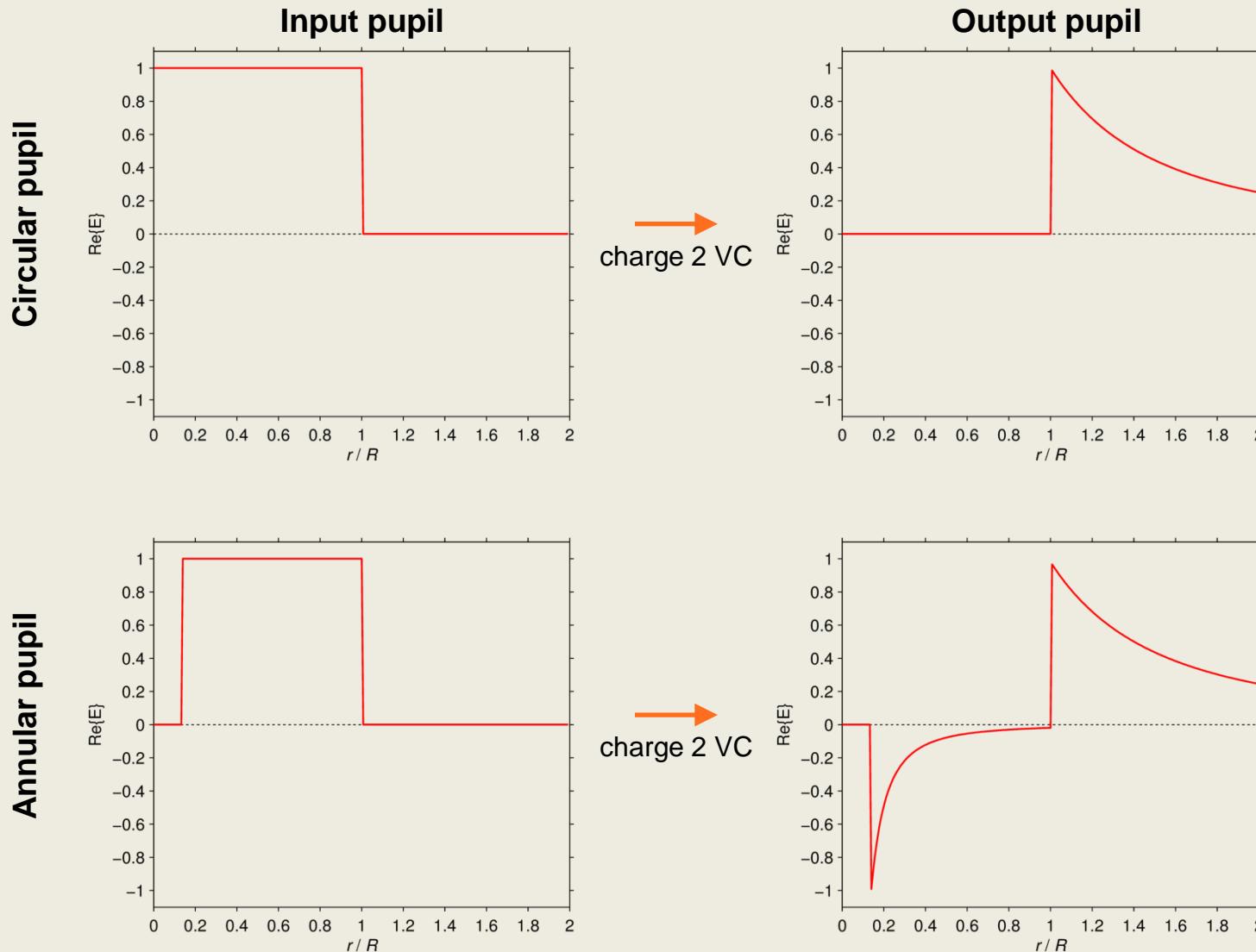
Apodized vortex coronagraphs



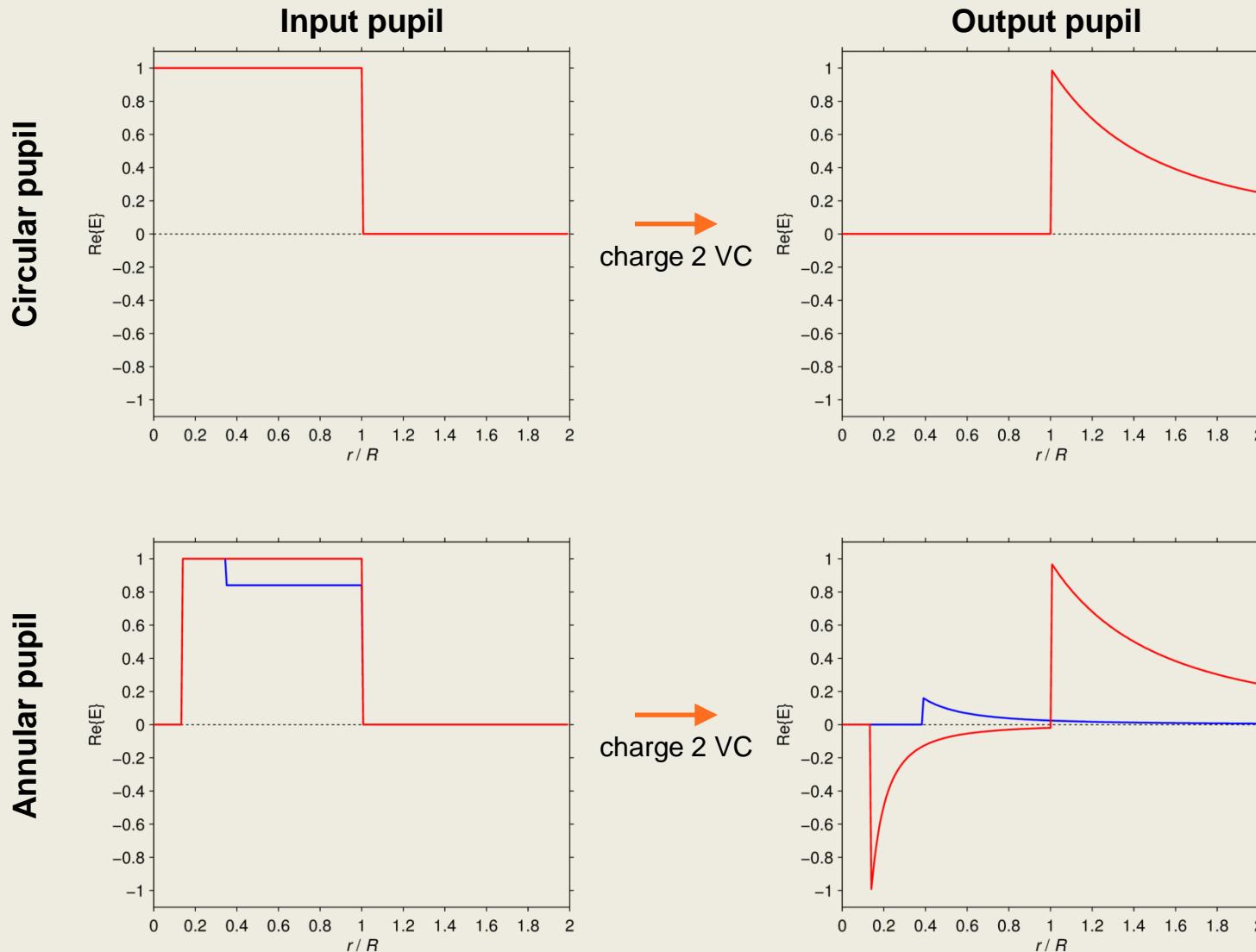
Ring apodizers



Starlight cancellation with a ring apodizer

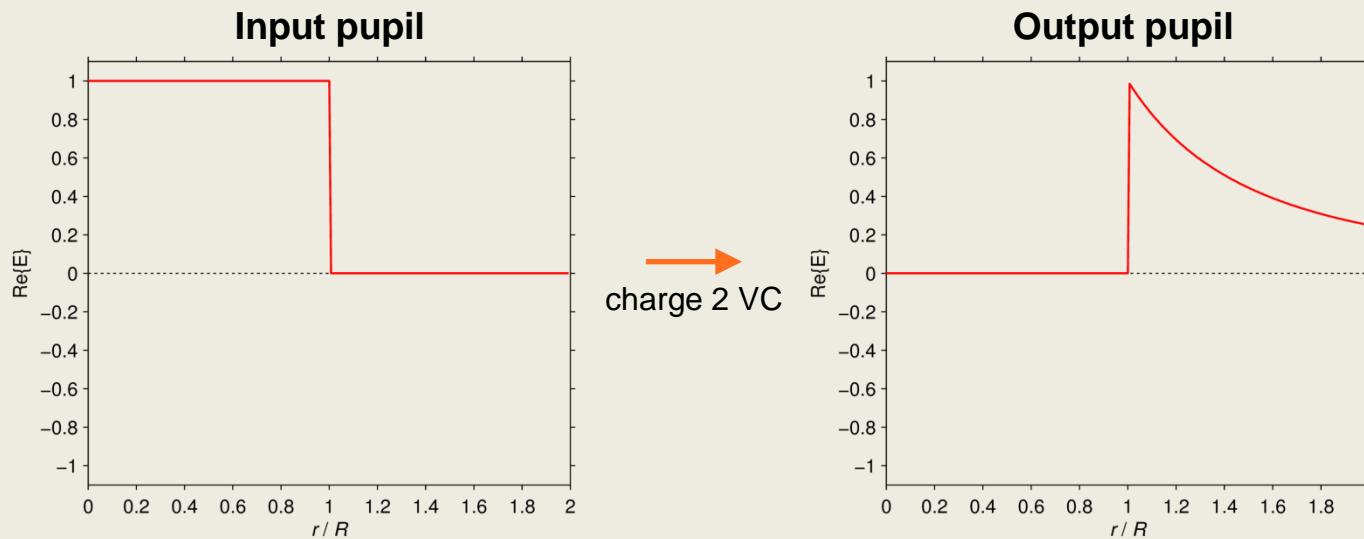


Starlight cancellation with a ring apodizer

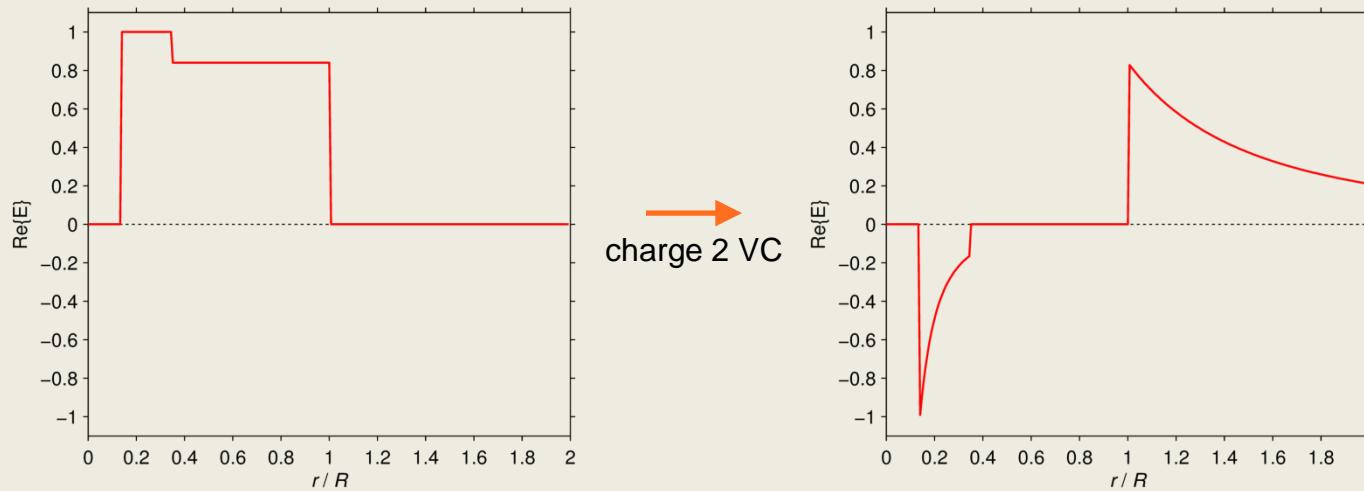


Starlight cancellation with a ring apodizer

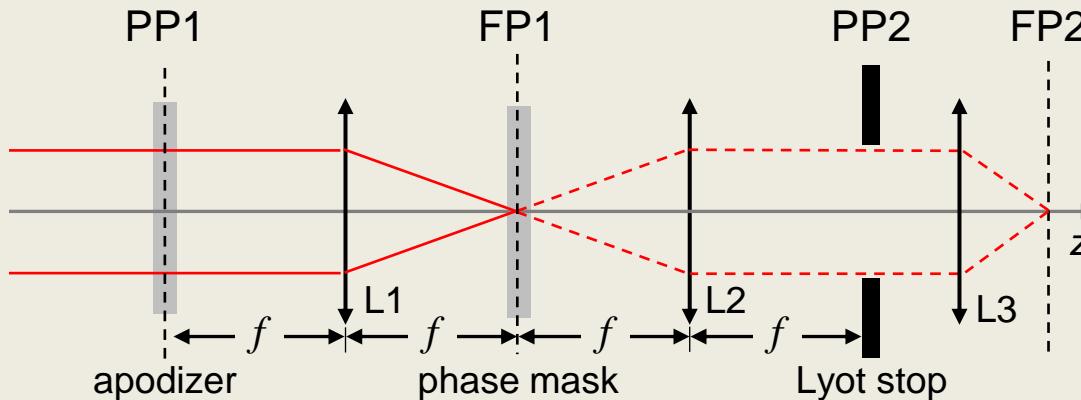
Circular pupil



Ring apodized pupil

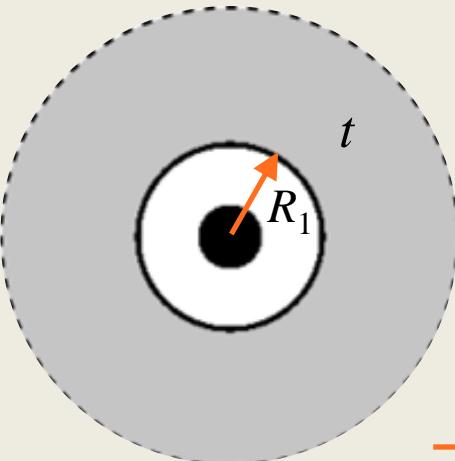


Apodizer optimization



Mawet et al., *ApJS* **209** 7 (2013)

Ring apodizer

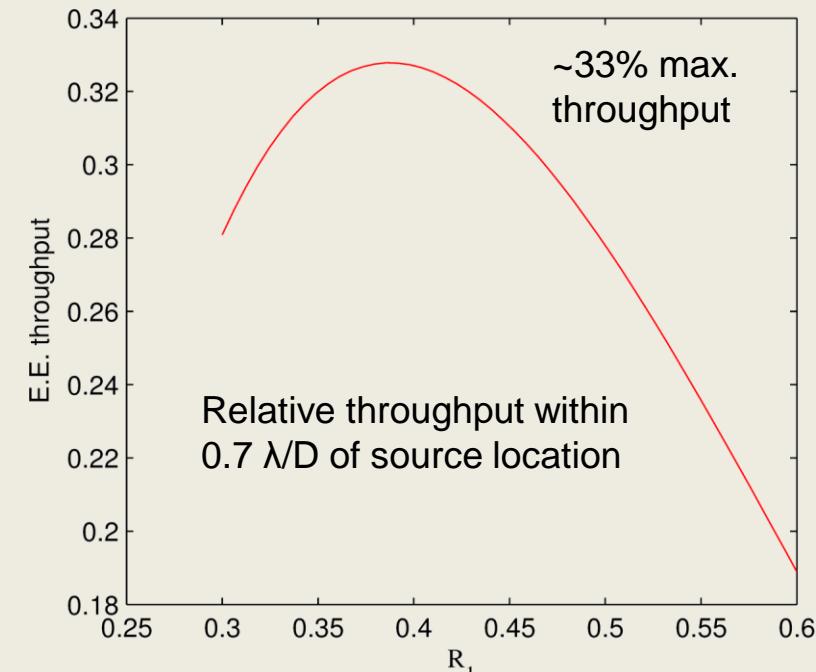


charge 4 VC

Field at PP2



Yields theoretically perfect starlight cancellation for annular aperture



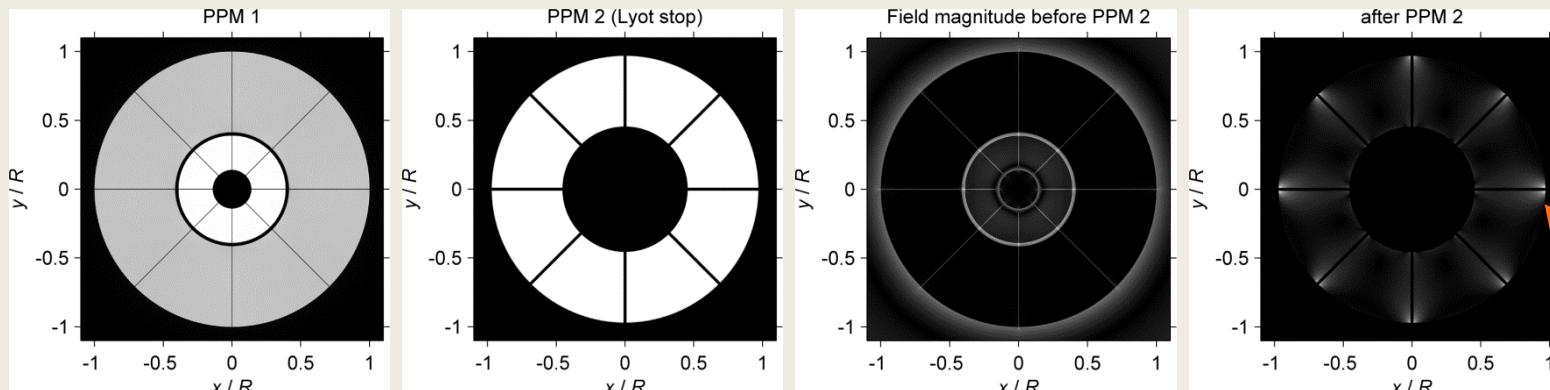
~33% max.
throughput

Relative throughput within
0.7 λ/D of source location

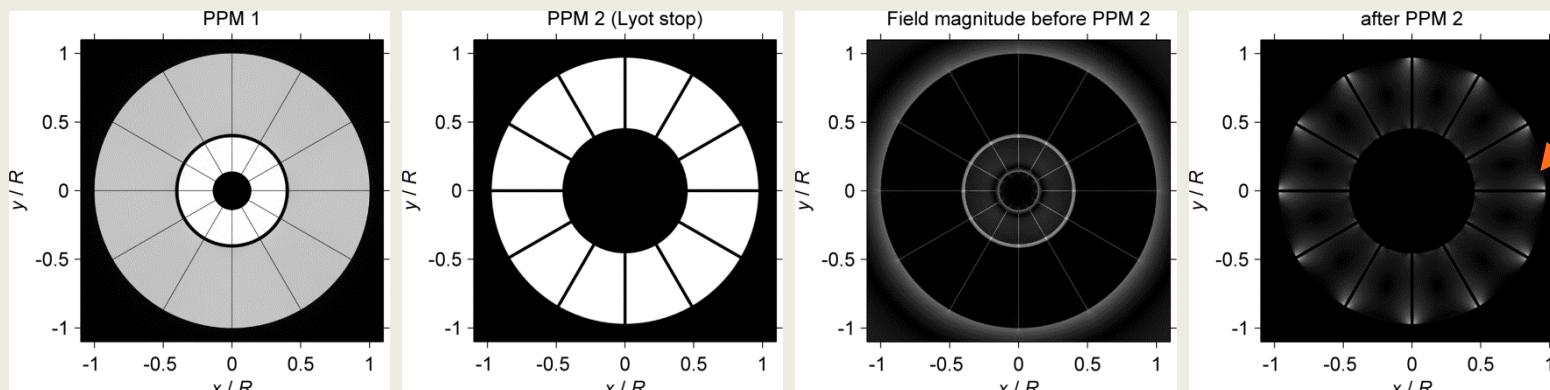
Apodized VC performance with segmented apertures

Analytically-inspired, ring-apodized VC (RAVC) with charge 4

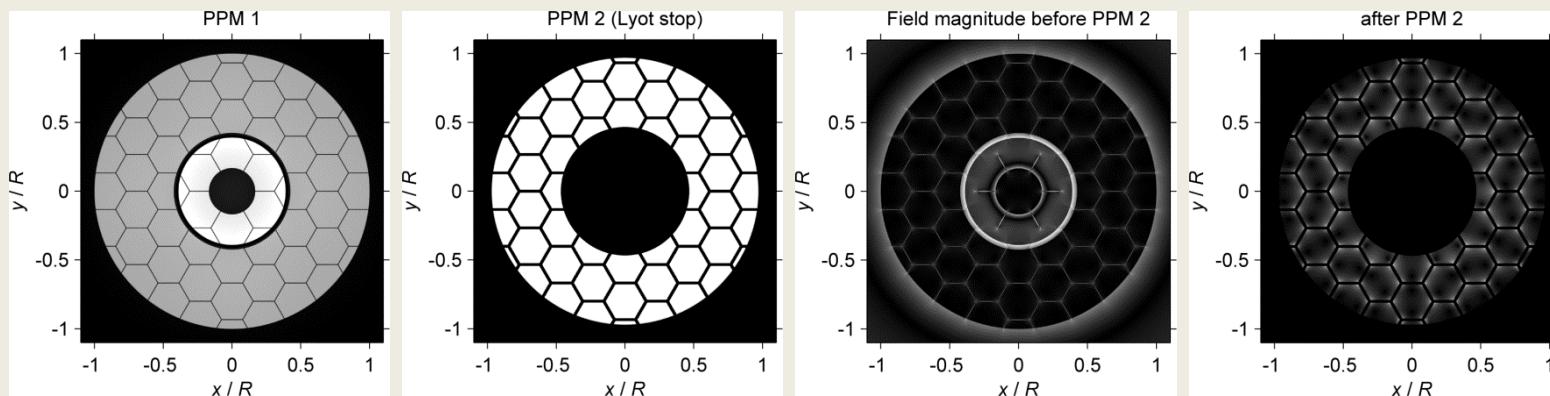
Piewedge 8



Piewedge 12



Clipped Hex 4

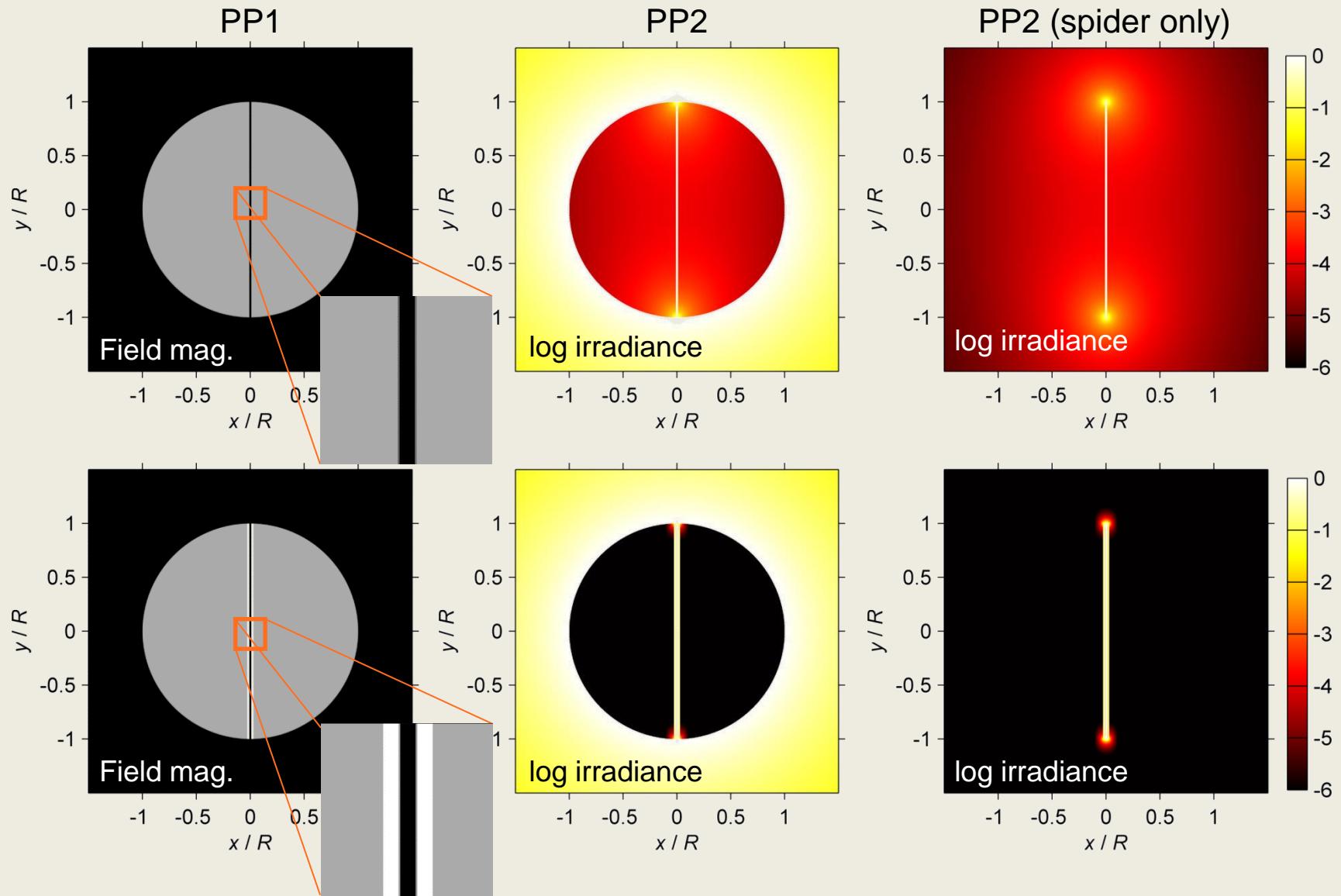


Leaked starlight owing to segment gaps

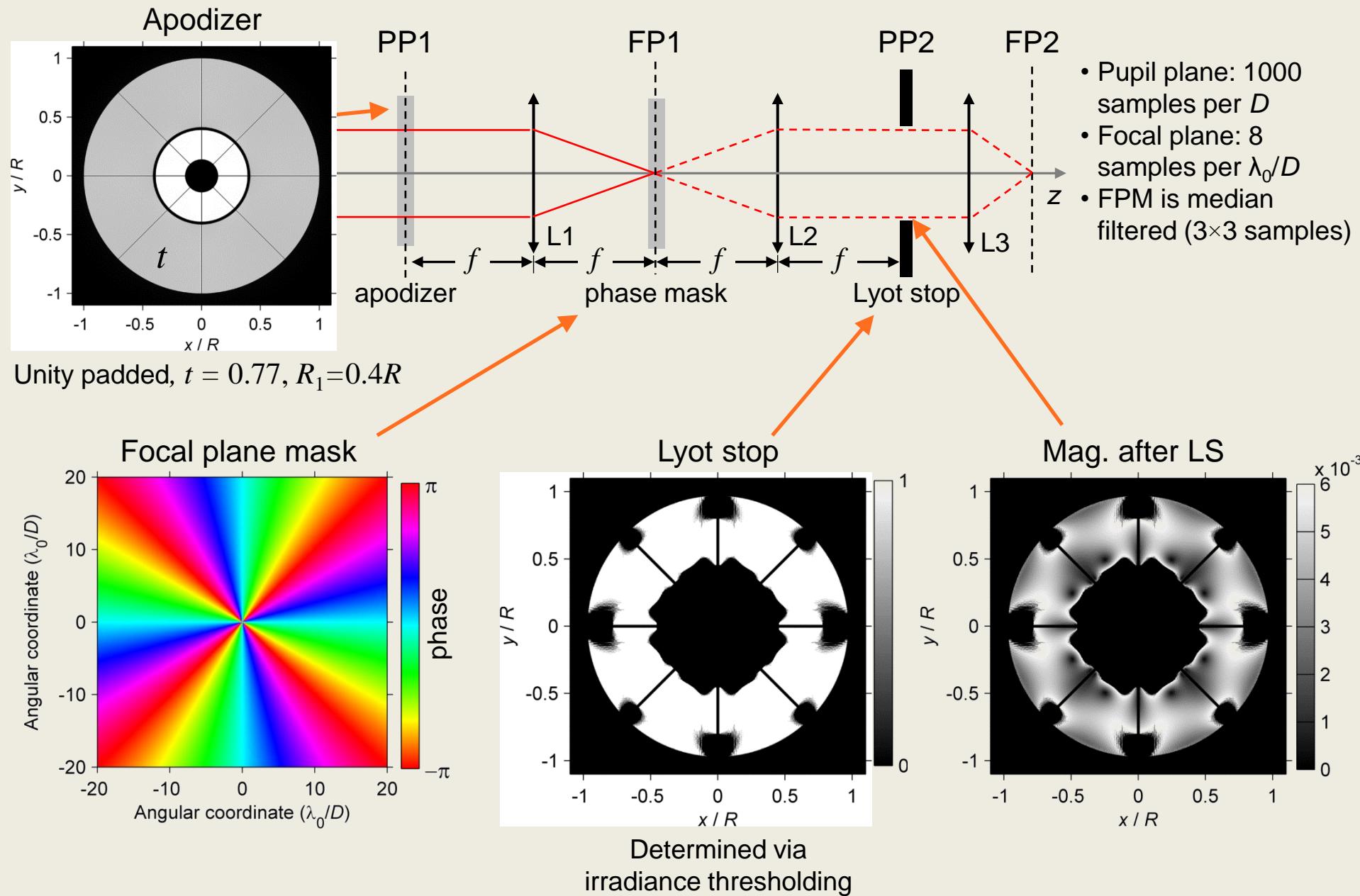
2. Optimizing the masks

Option I: Optimizing the apodizer

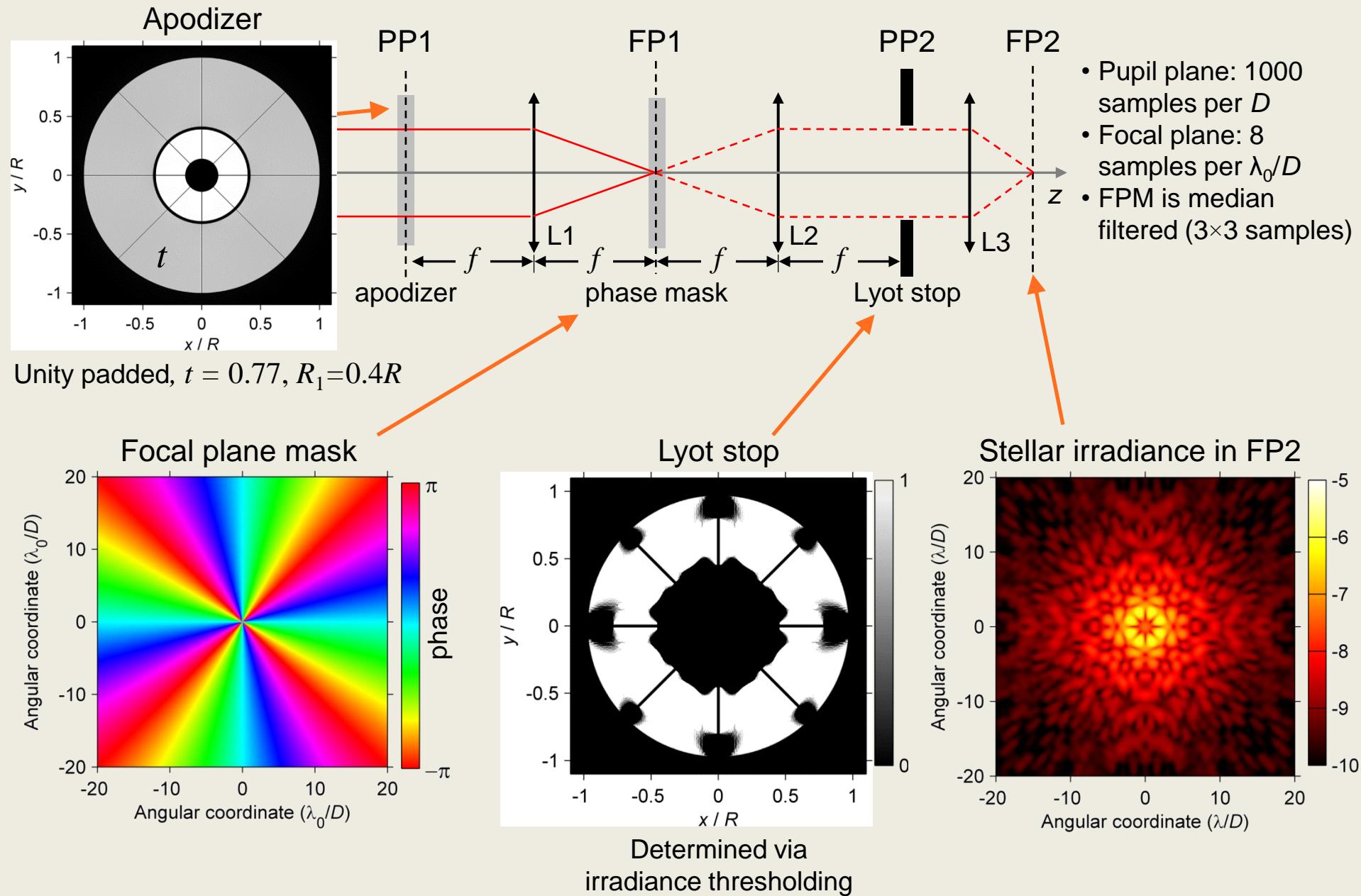
Unity padding of aperture discontinuities



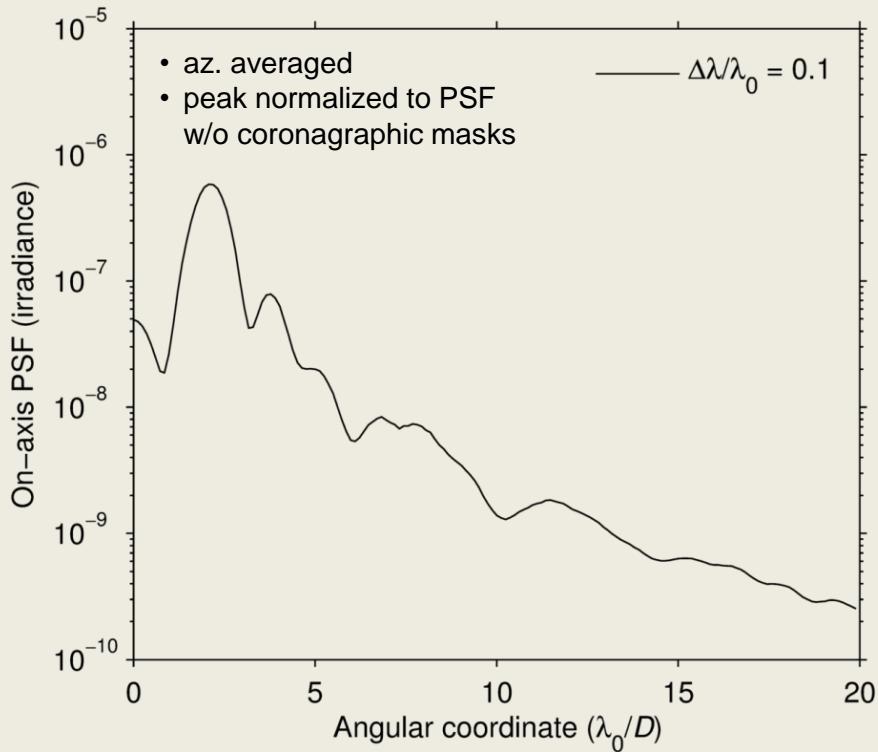
Option I: Optimizing the apodizer and Lyot stop



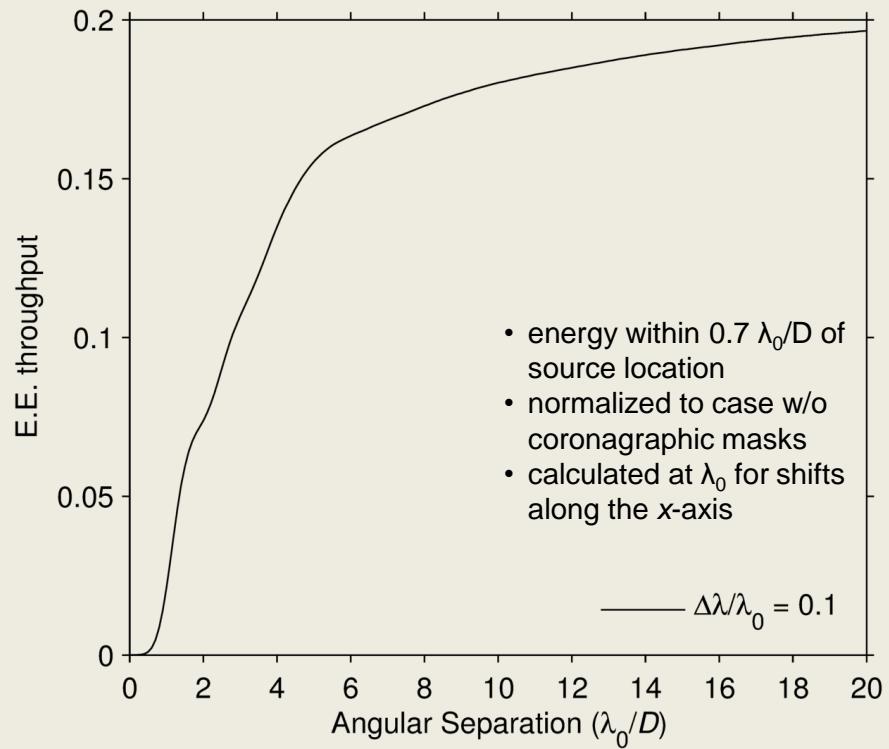
Option I: Optimizing the apodizer and Lyot stop



Option I: Optimizing the apodizer and Lyot stop

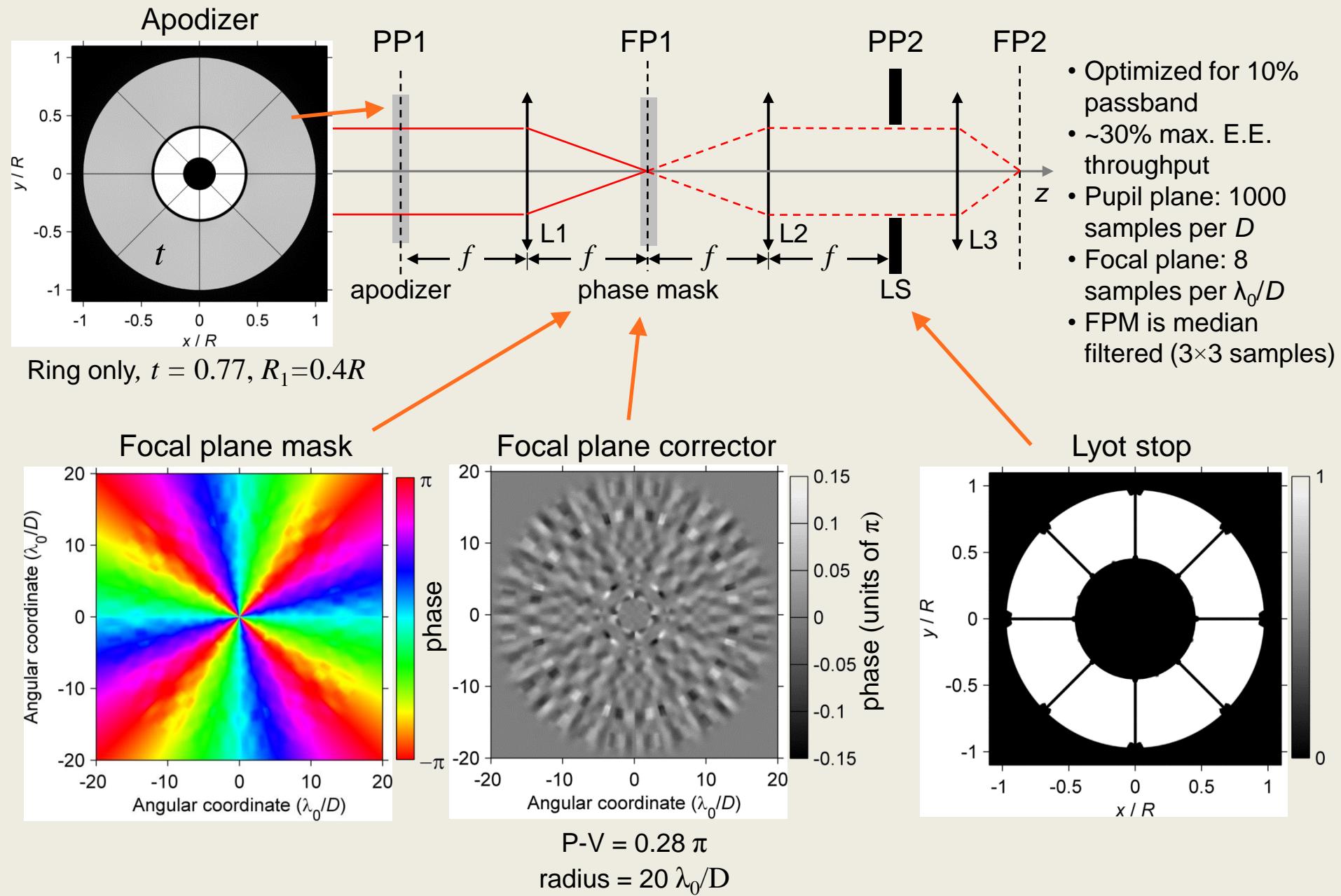


<10⁻⁷ stellar irradiance for angular separations >3 λ_0/D

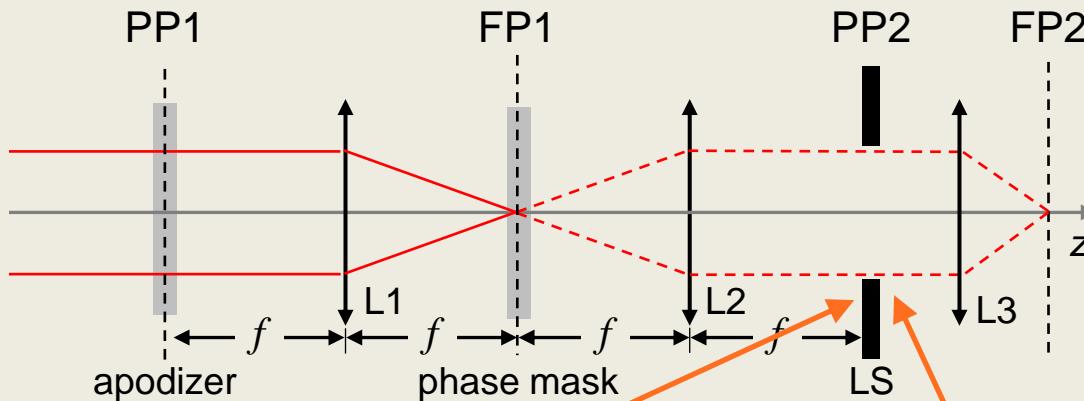


>10% encircled energy throughput for angular separations >3 λ_0/D (w.r.t the telescope)

Option II: Optimizing the focal plane mask

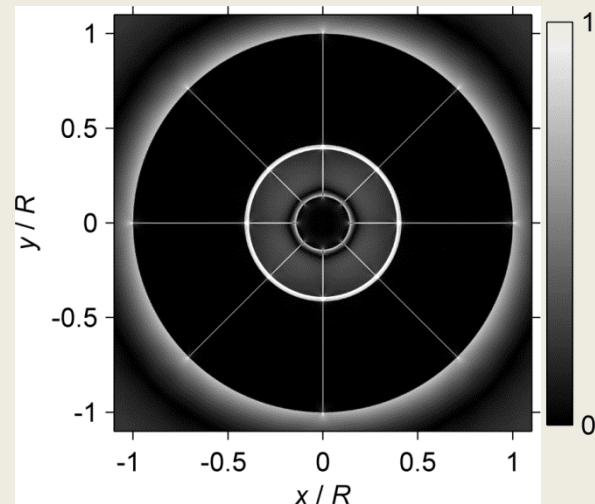


Option II: Optimizing the focal plane mask

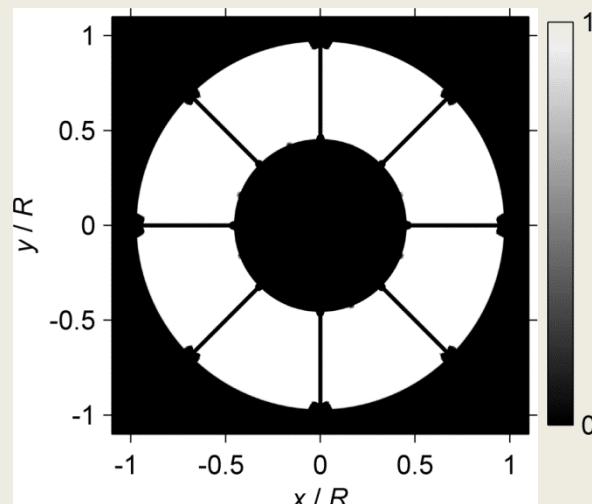


Field in PP2 (at λ_0)

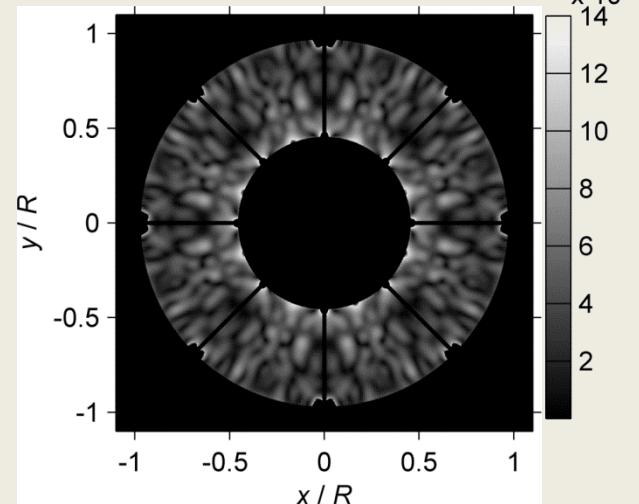
Mag. before LS



Lyot stop (LS)

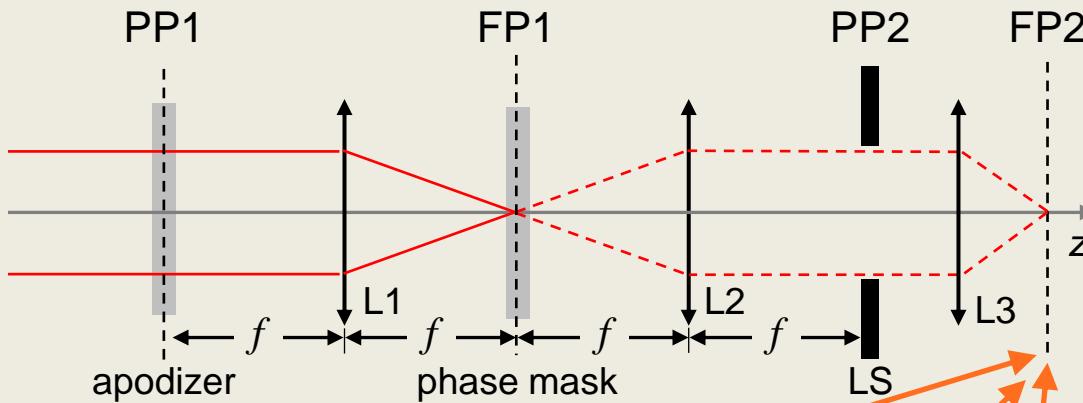


Mag. after LS

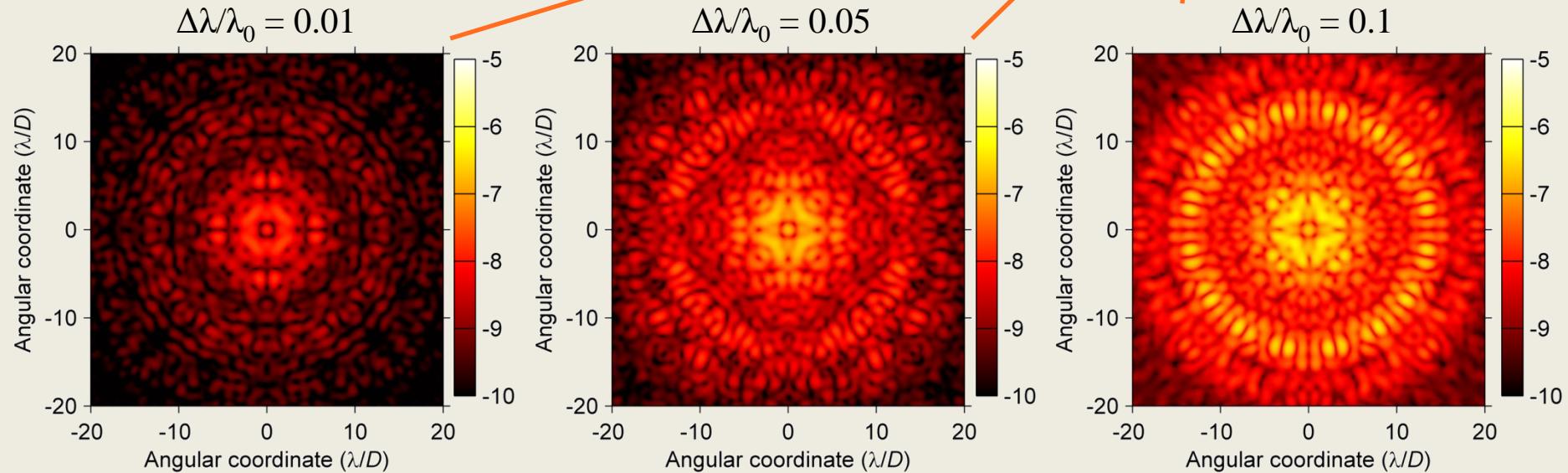


leaked energy fraction at λ_0
 $= 1.3 \times 10^{-4}$

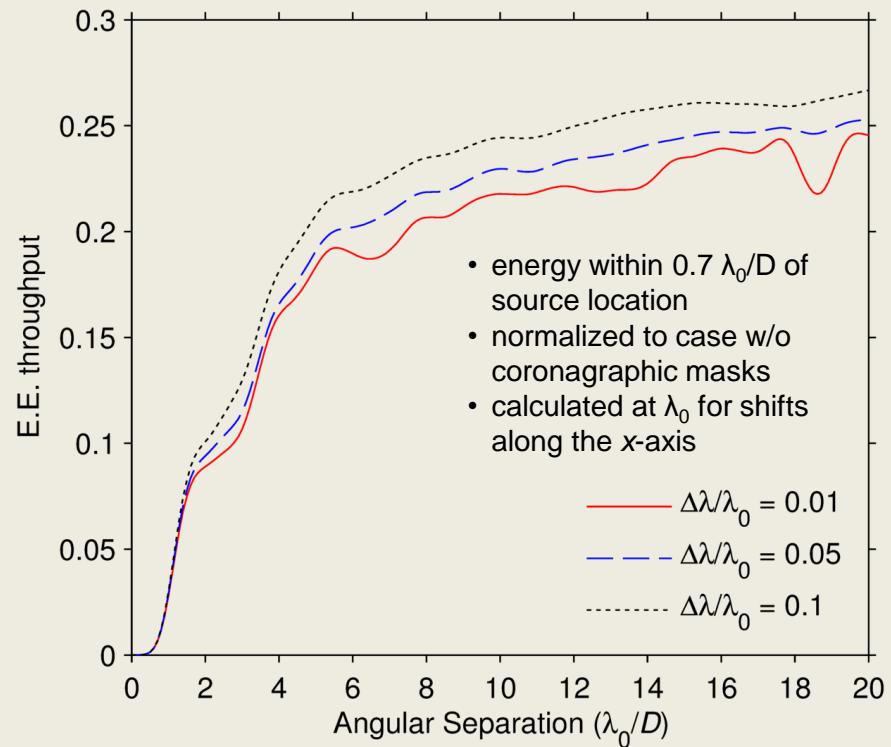
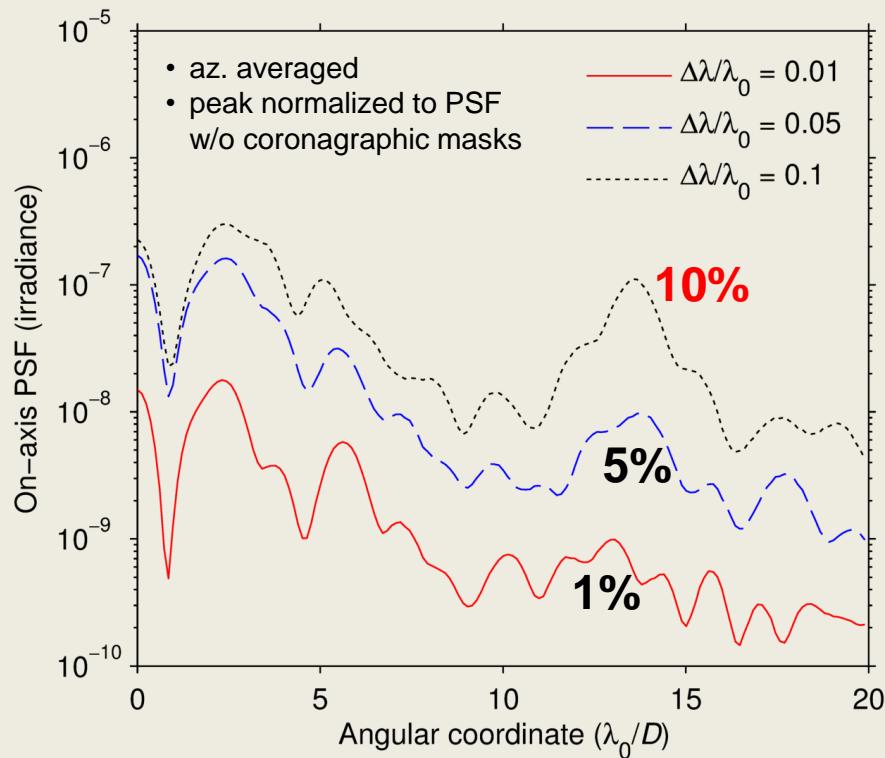
Option II: Optimizing the focal plane mask



Stellar irradiance in FP2



Option II: Optimizing the focal plane mask



>10% encircled energy throughput for angular separations > $3 \lambda_0/D$ (w.r.t the telescope)

Optimizing the *sensitivity* to planets

In photon-noise limited regime:

$$\text{SNR} \sim \frac{\text{planet energy}}{\sqrt{\text{star energy} + \text{noise terms}}} \approx \frac{\text{planet energy}}{\sqrt{\text{star energy}}}$$

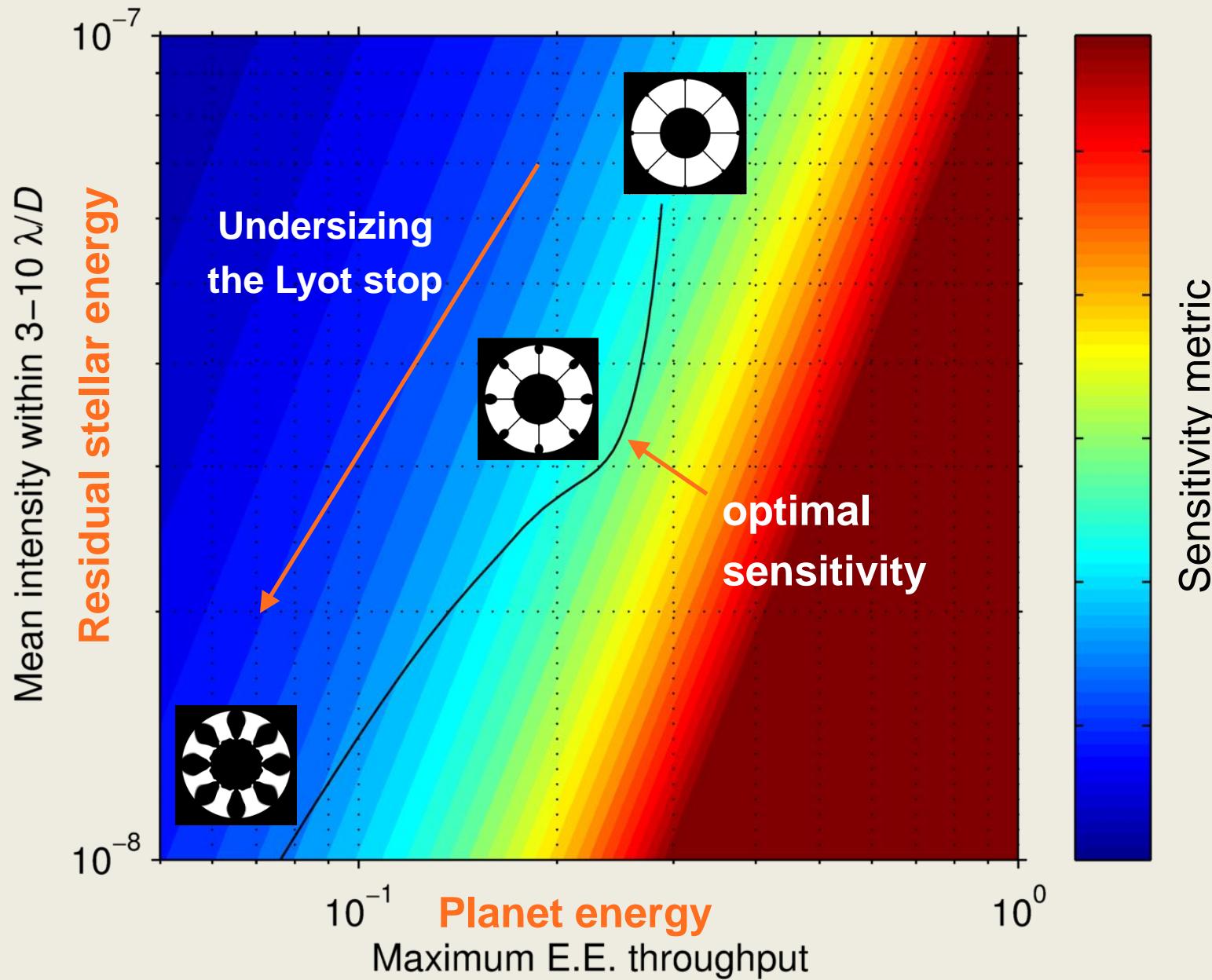
$$\text{sensitivity metric} = \frac{\eta \times B}{\sqrt{s \times B}} = \eta \sqrt{\frac{B}{s}}$$

η – Max. encircled energy throughput (within $0.7 \lambda_0/D$ of source position, normalized to telescope throughput)

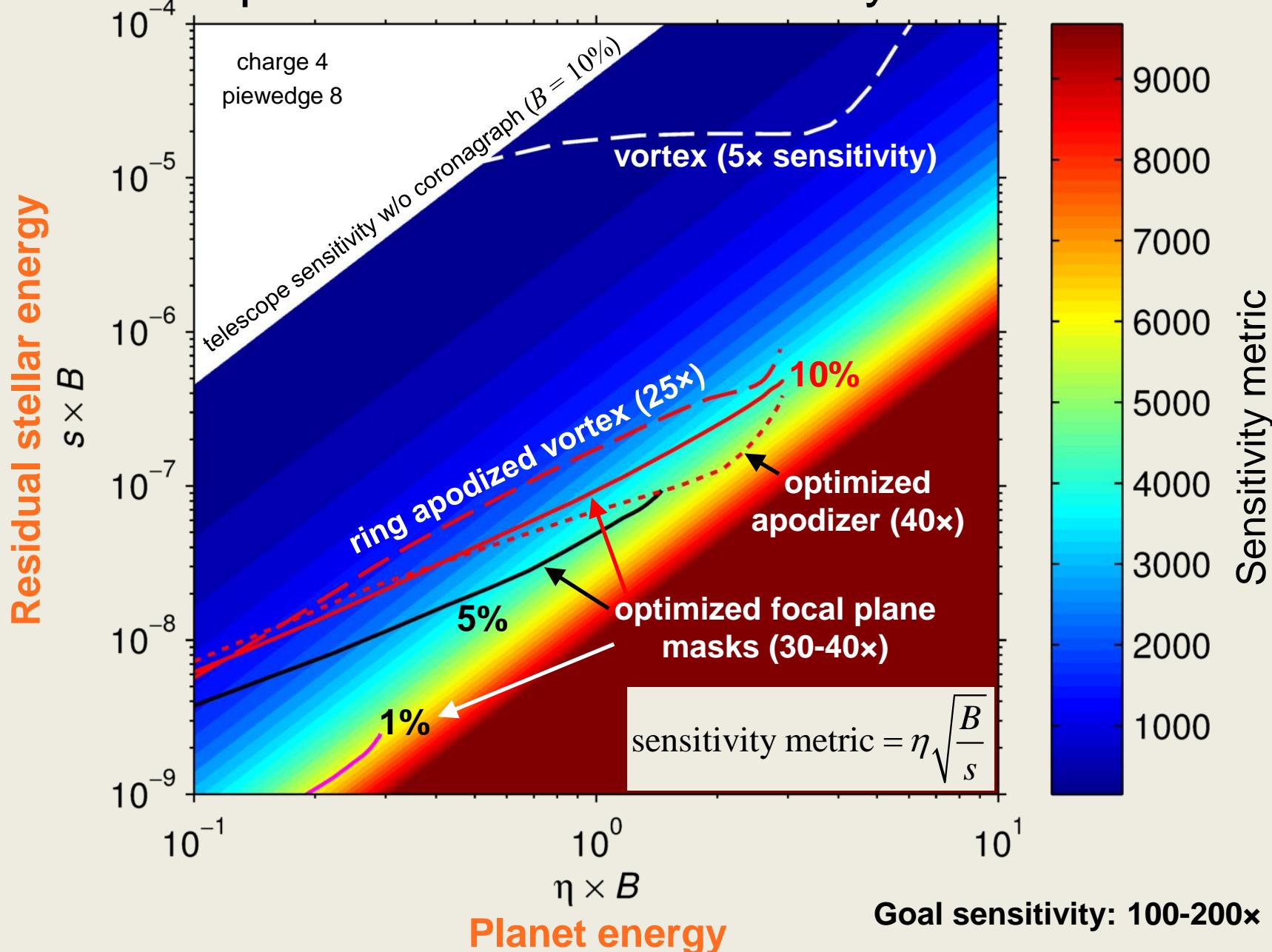
s – Residual stellar energy in the image plane
(averaged over $3-10 \lambda_0/D$ annulus and passband)

B – Percent bandwidth $B = \Delta\lambda/\lambda_0 \times 100$

For example: optimizing the Lyot stop



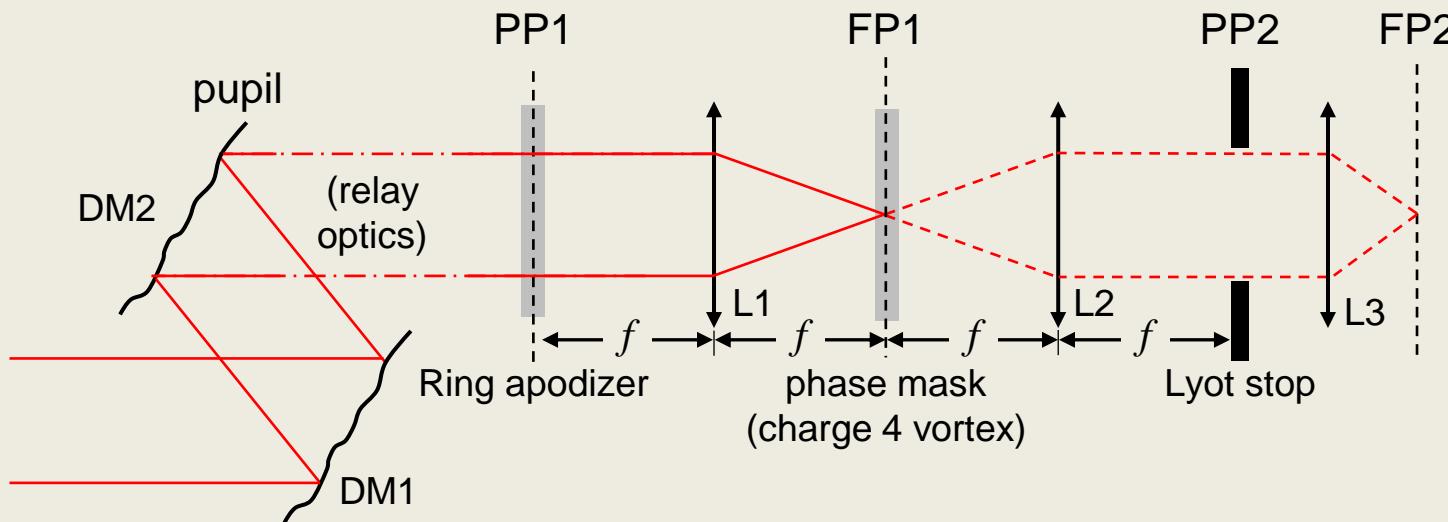
Optimization via a sensitivity metric



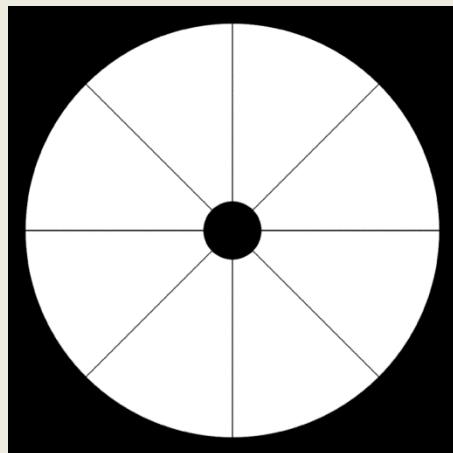
3. Wavefront control for segmented apertures

Active Compensation of Aperture Discontinuities (ACAD)

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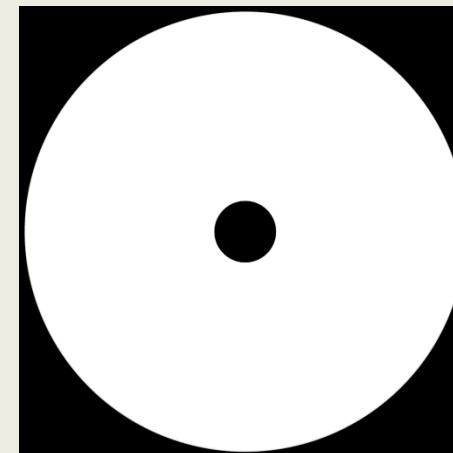


Original pupil

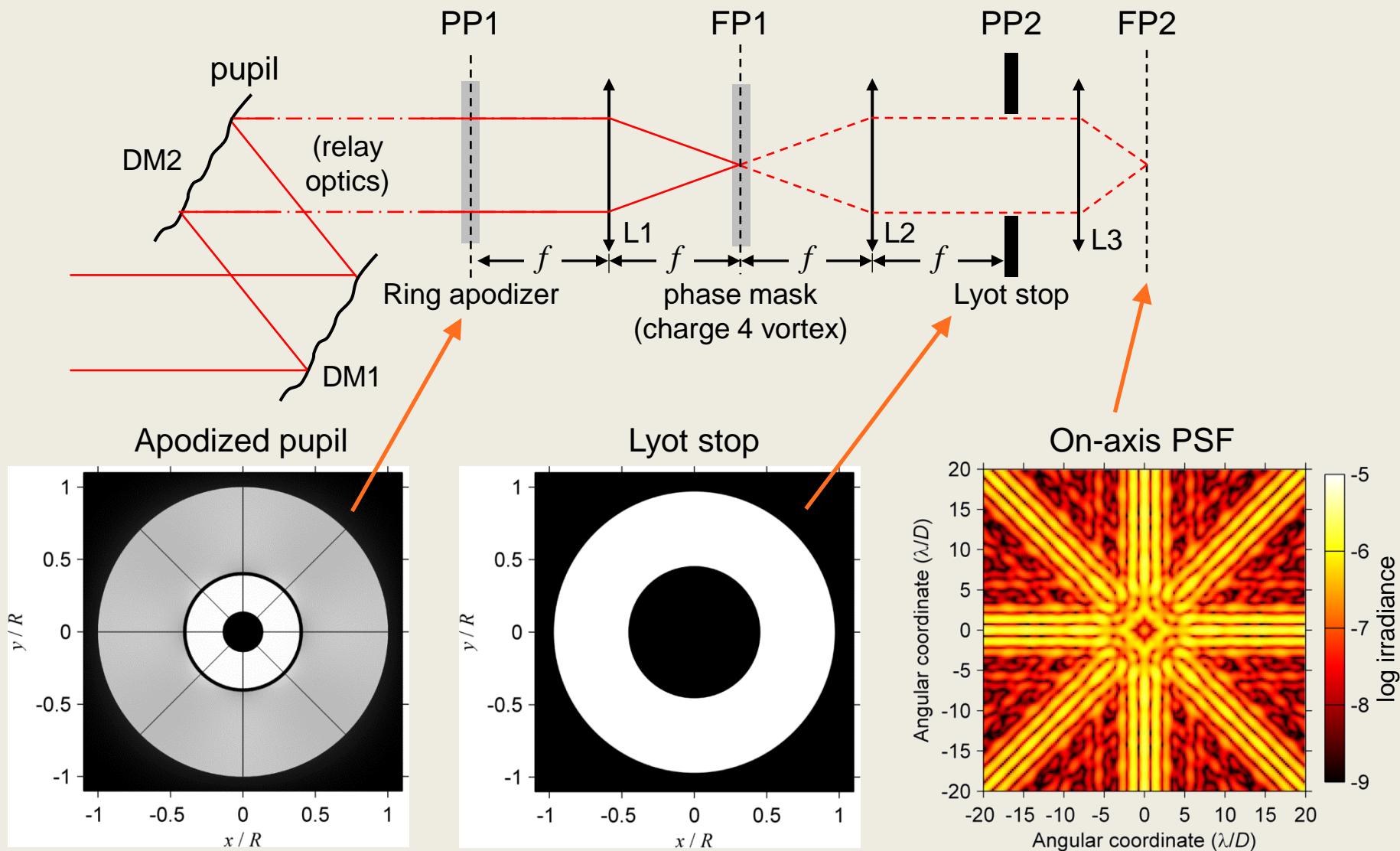


→
ACAD

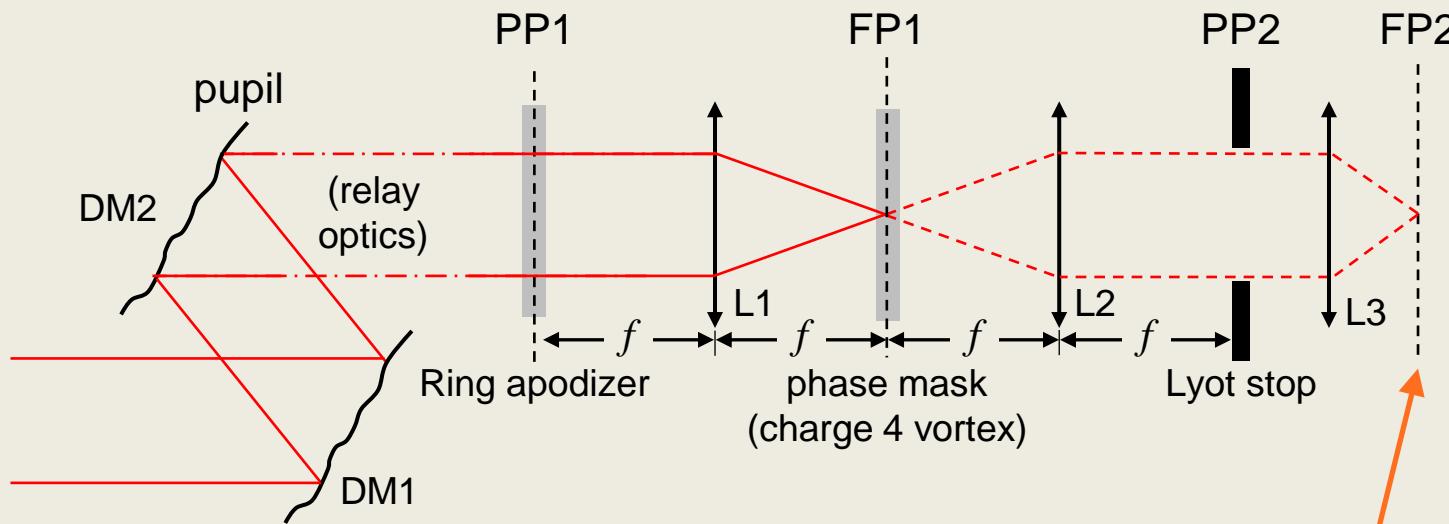
Goal pupil



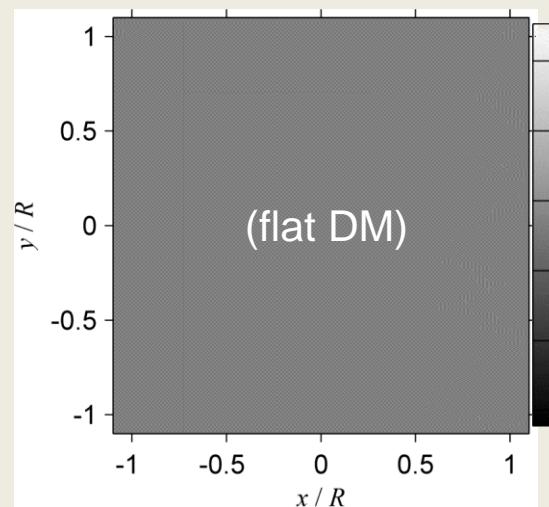
Active Compensation of Aperture Discontinuities (ACAD)



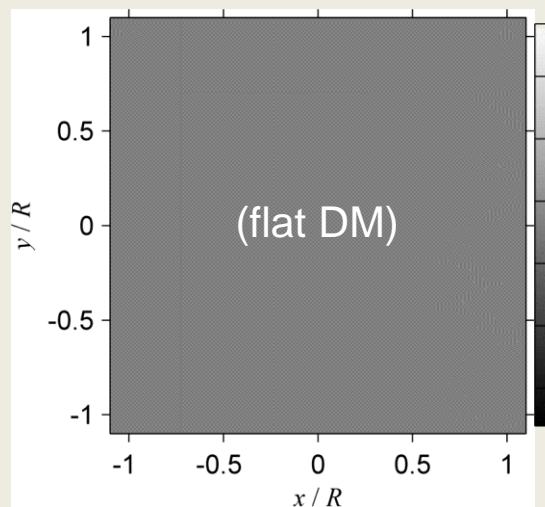
Active Compensation of Aperture Discontinuities (ACAD)



Surface height DM1 (nm)

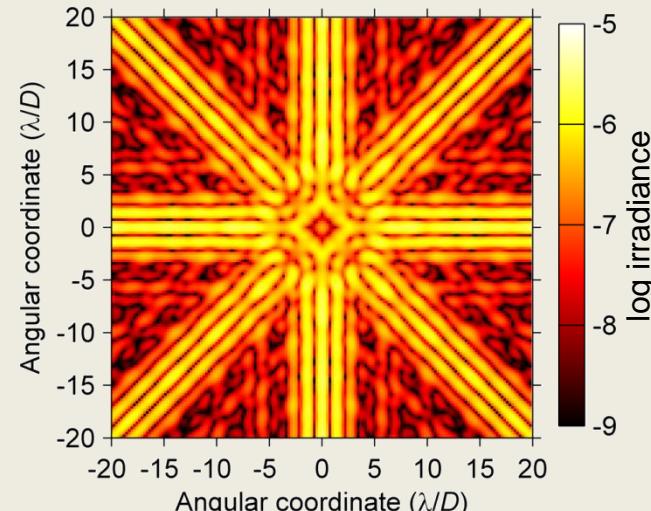


Surface height DM2 (nm)

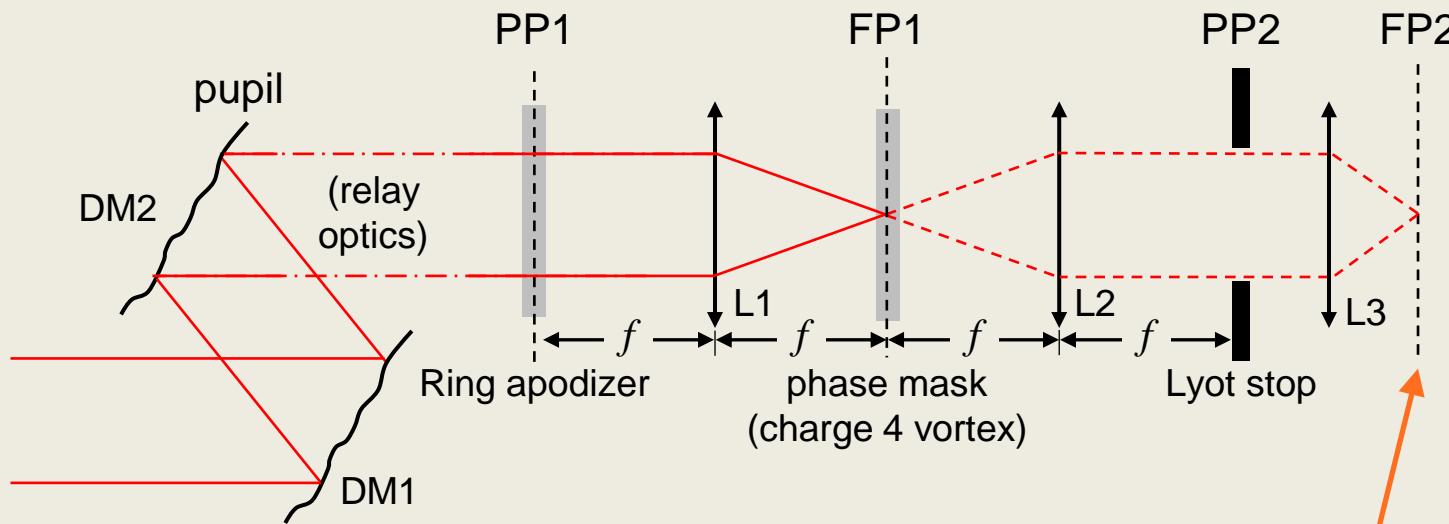


(Located in pupil)

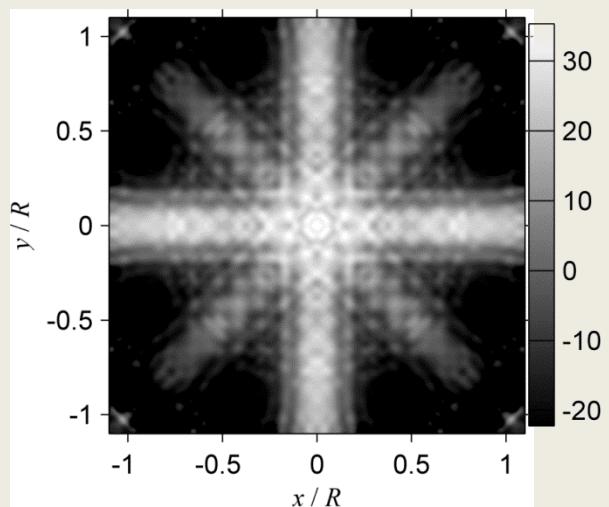
On-axis PSF



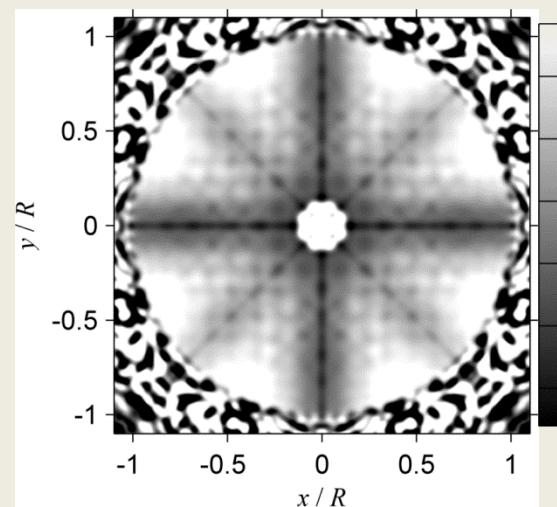
Active Compensation of Aperture Discontinuities (ACAD)



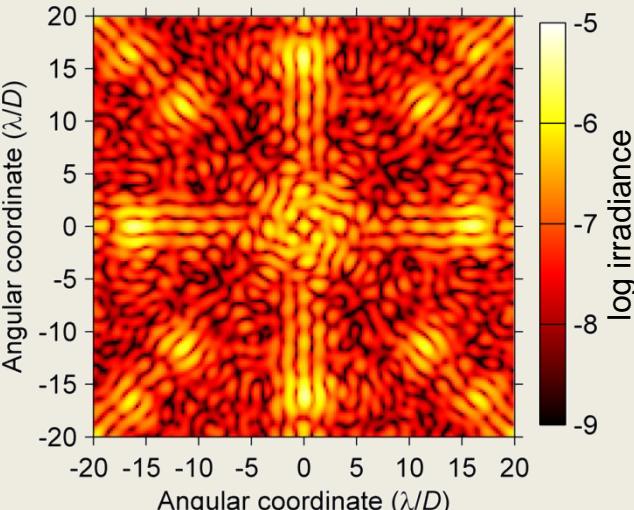
Surface height DM1 (nm)



Surface height DM2 (nm)



On-axis PSF



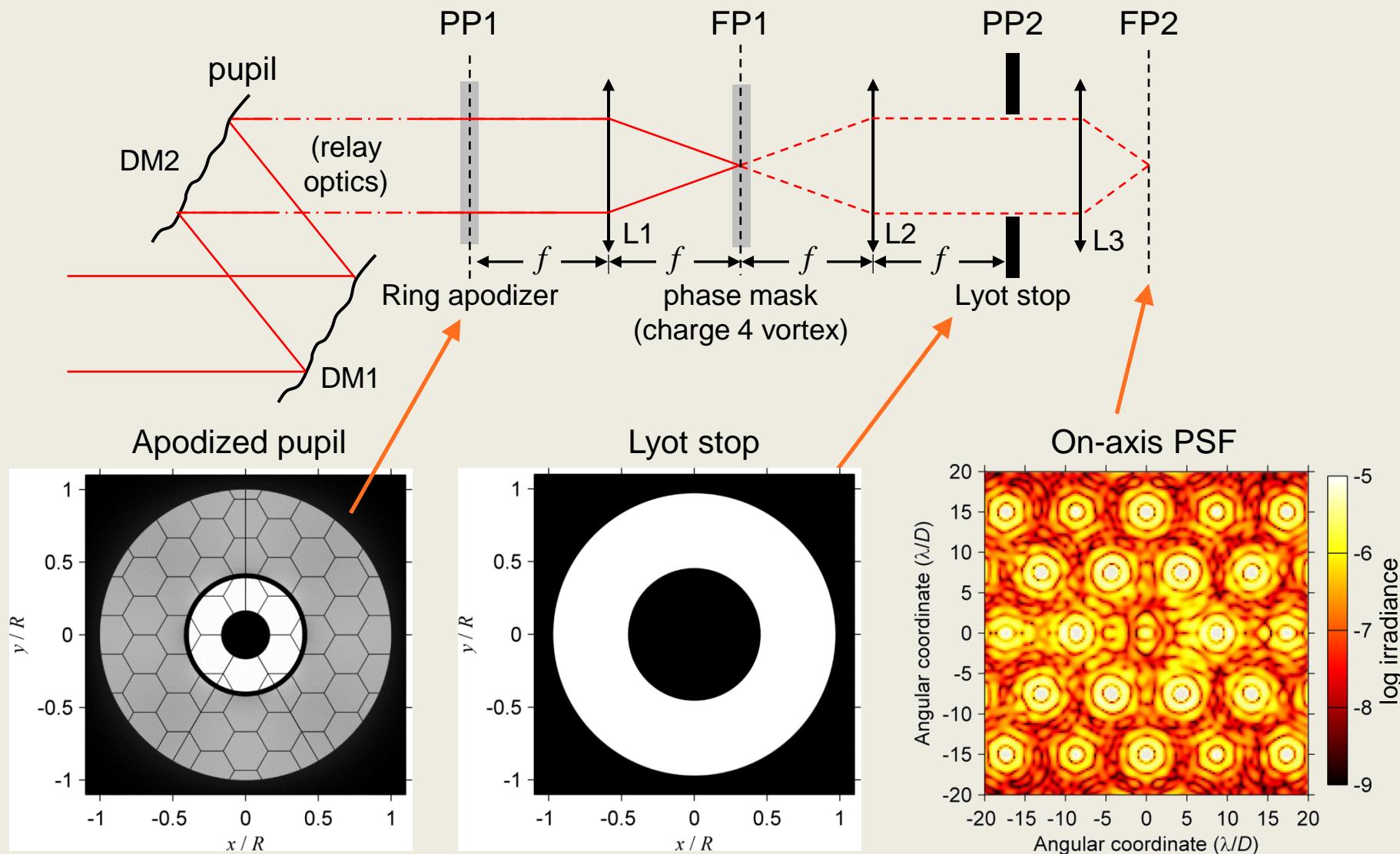
(Located in pupil)

$$\lambda = 500 \text{ nm}$$

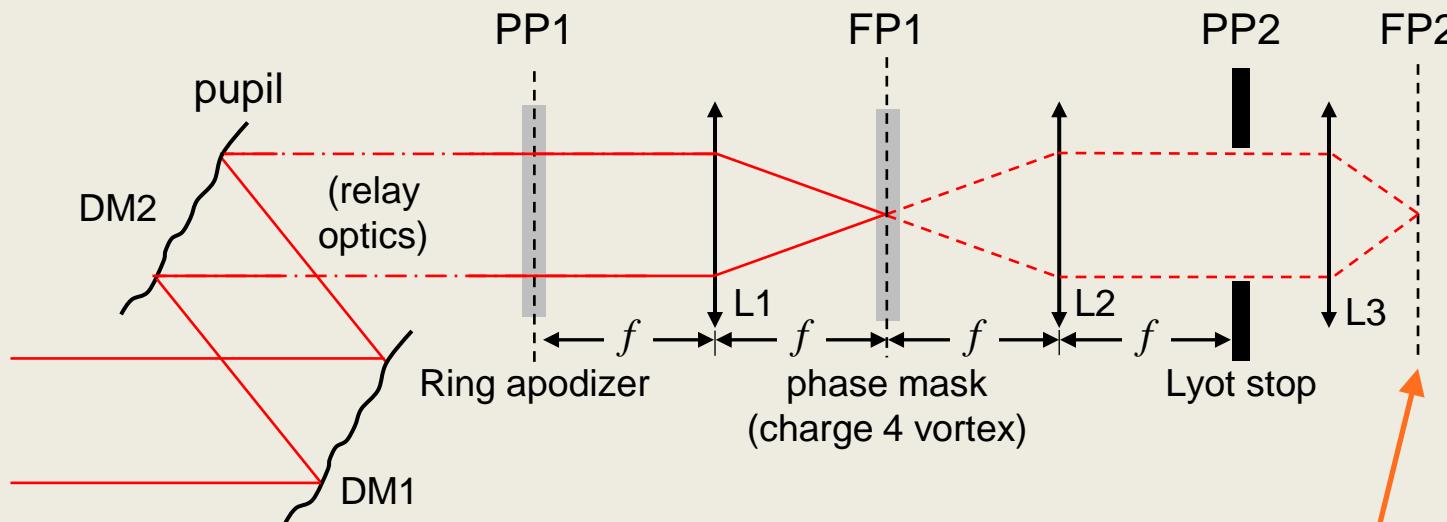
$$N_{act} = 64$$

Active Compensation of Aperture Discontinuities (ACAD)

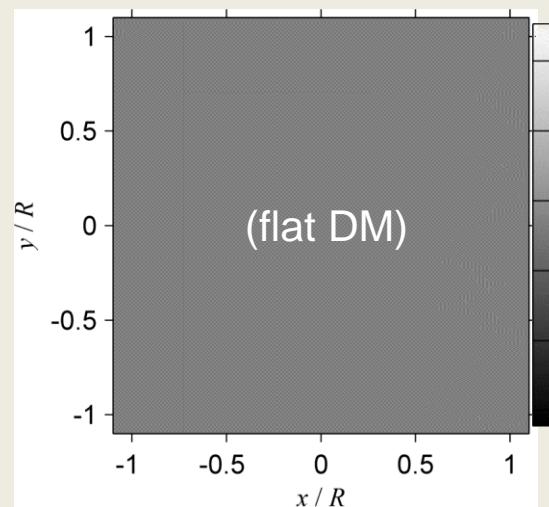
30



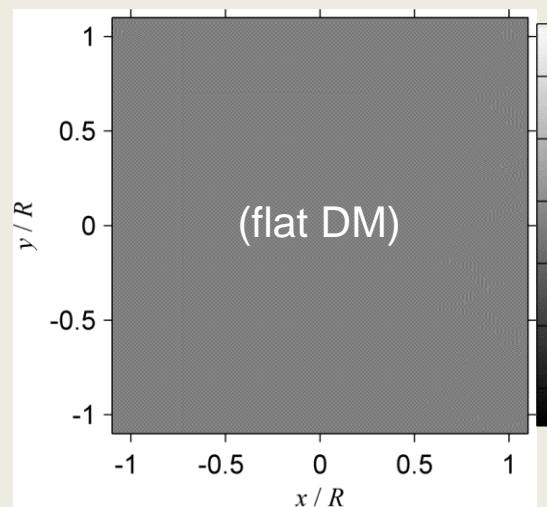
Active Compensation of Aperture Discontinuities (ACAD)



Surface height DM1

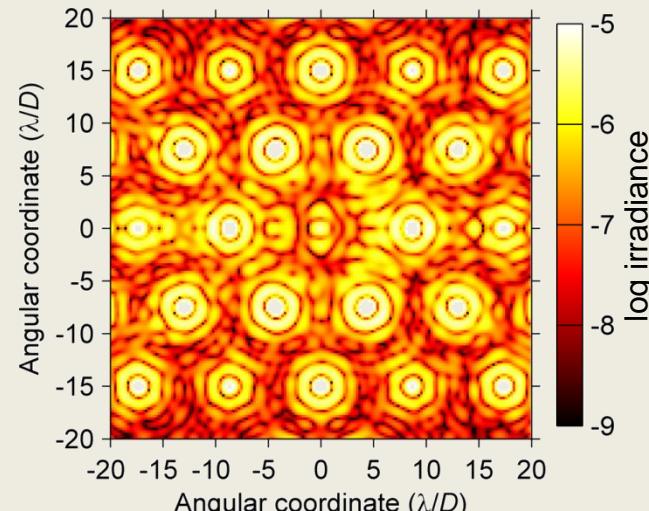


Surface height DM2

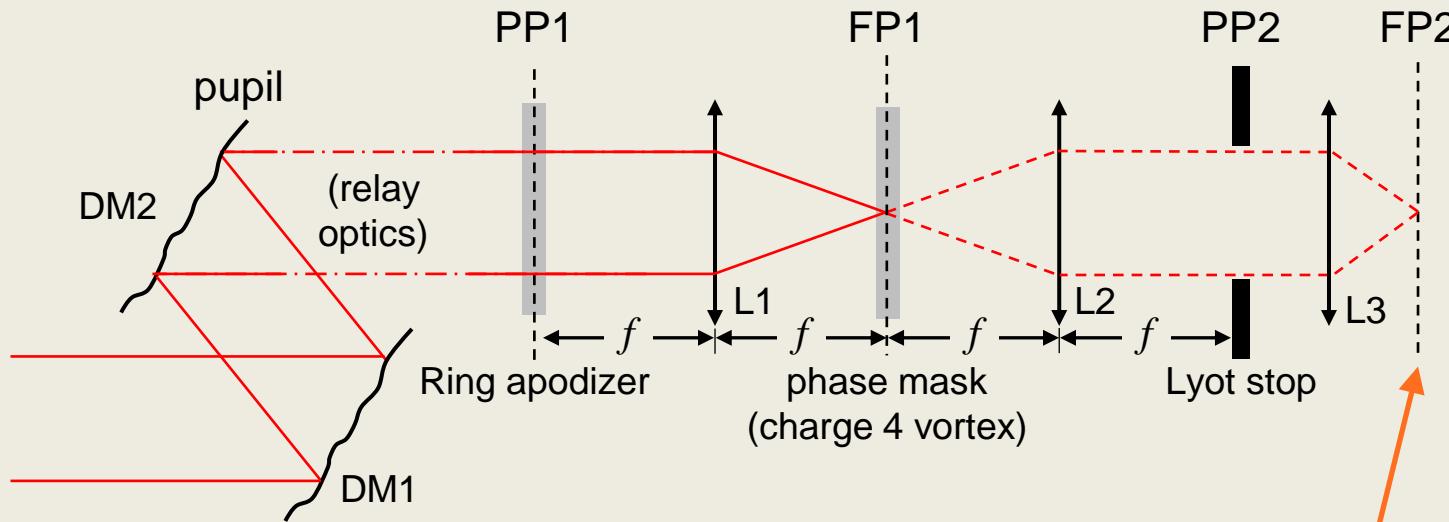


(Located in pupil)

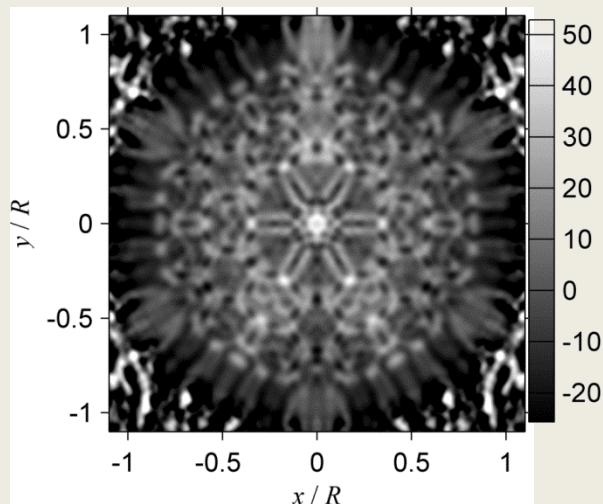
On-axis PSF



Active Compensation of Aperture Discontinuities (ACAD)



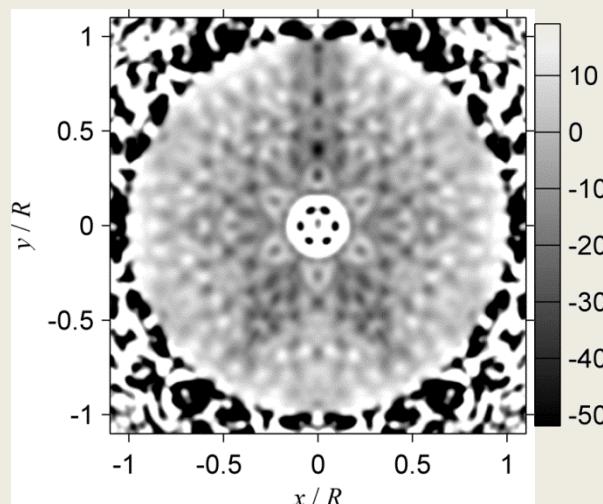
Surface height DM1 (nm)



$\lambda = 500 \text{ nm}$

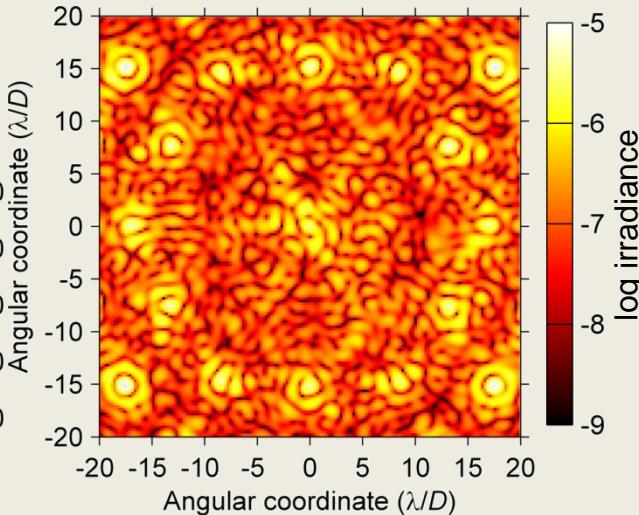
$N_{act} = 64$

Surface height DM2 (nm)

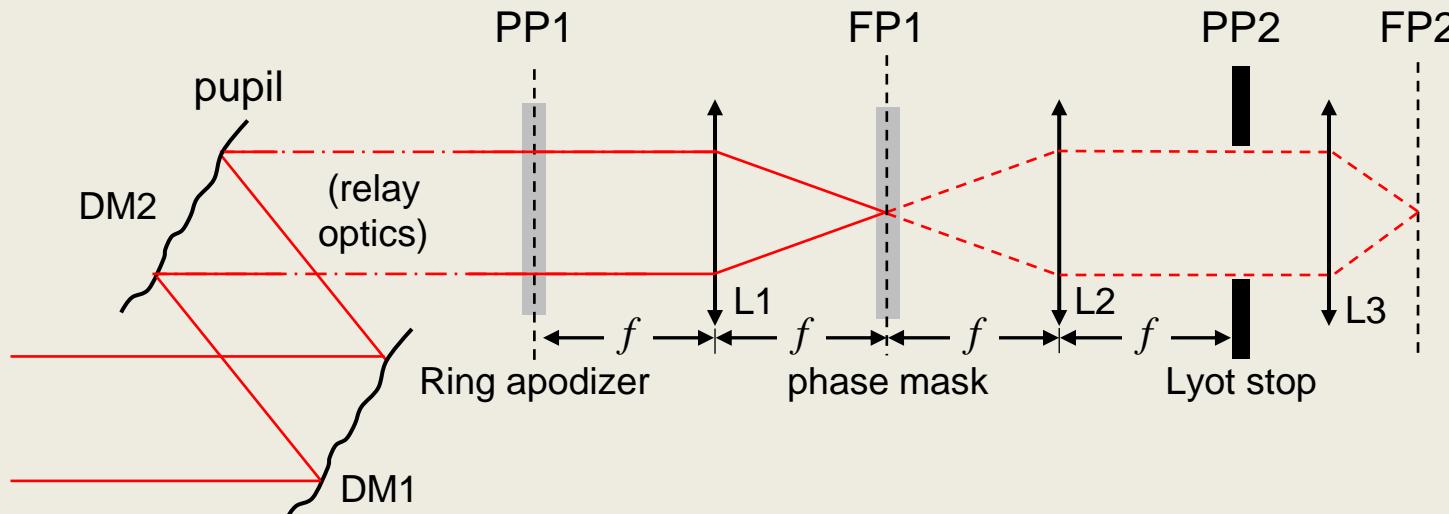


(Located in pupil)

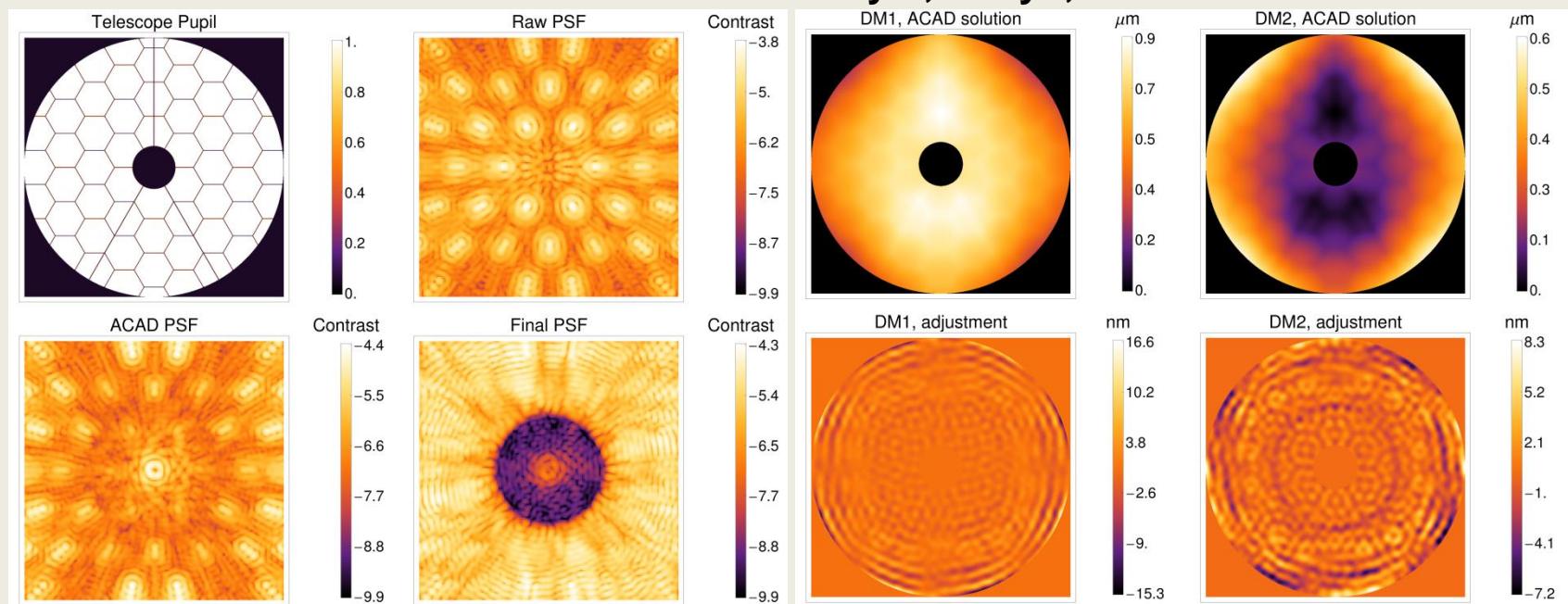
On-axis PSF



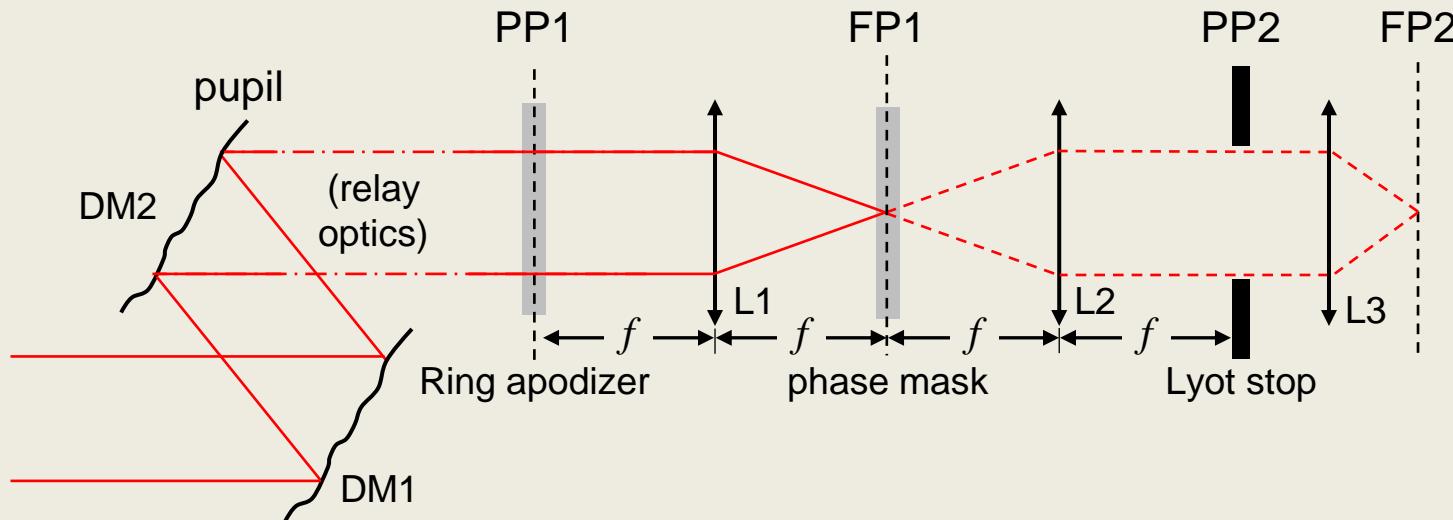
Active Compensation of Aperture Discontinuities (ACAD)



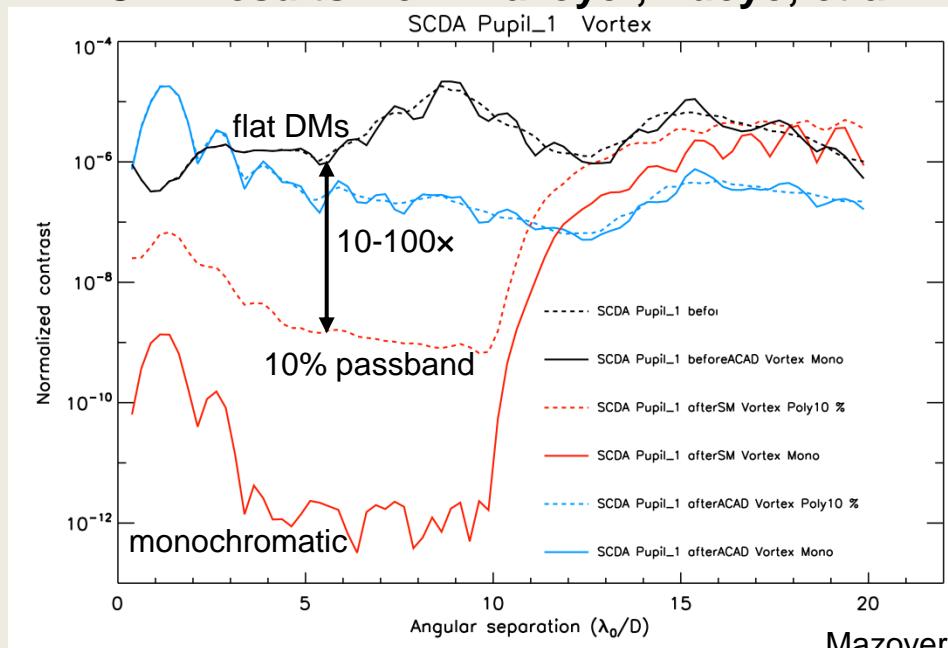
ACAD results from Mazoyer, Pueyo, et al.



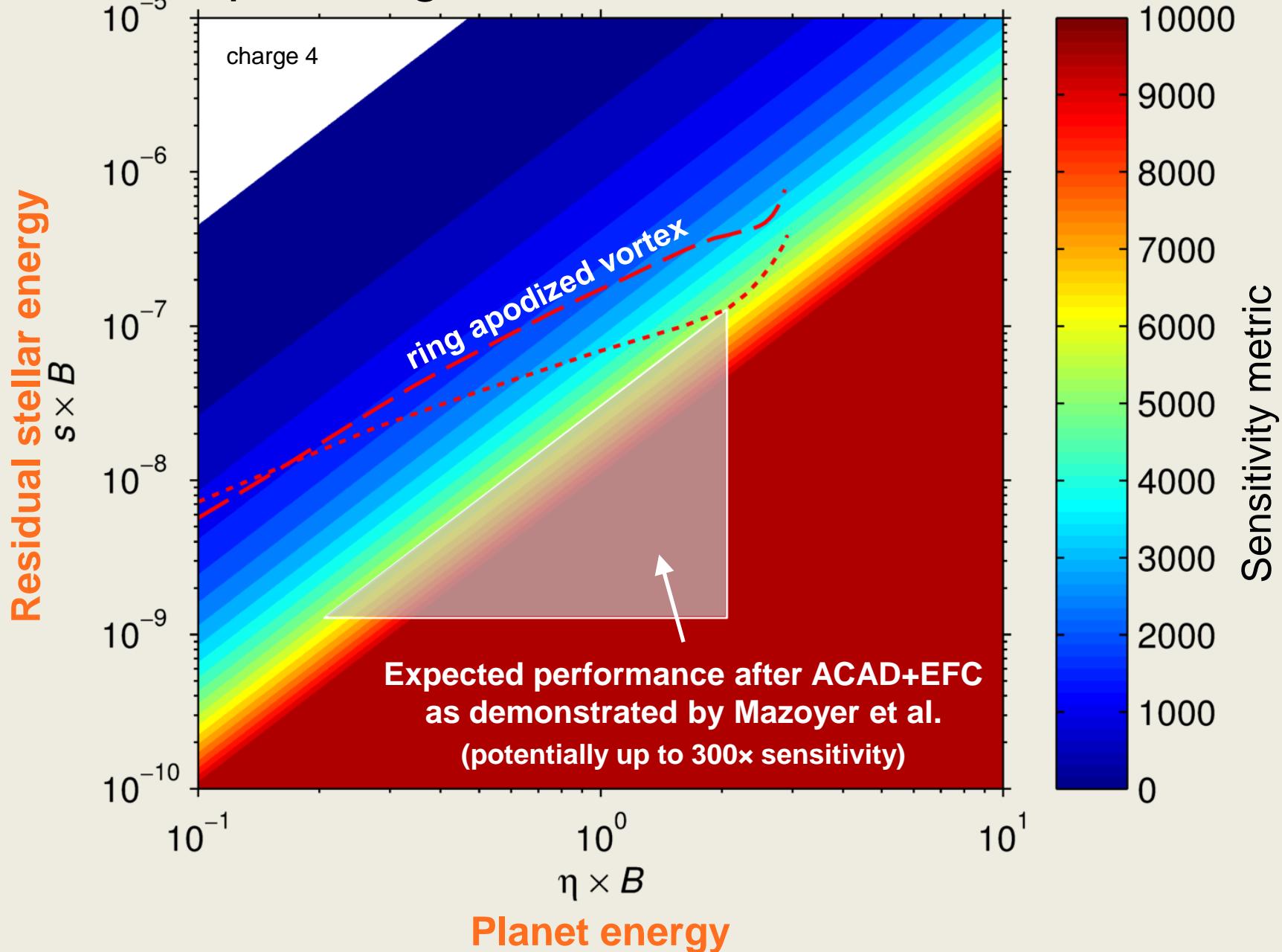
Active Compensation of Aperture Discontinuities (ACAD)



ACAD results from Mazoyer, Pueyo, et al.



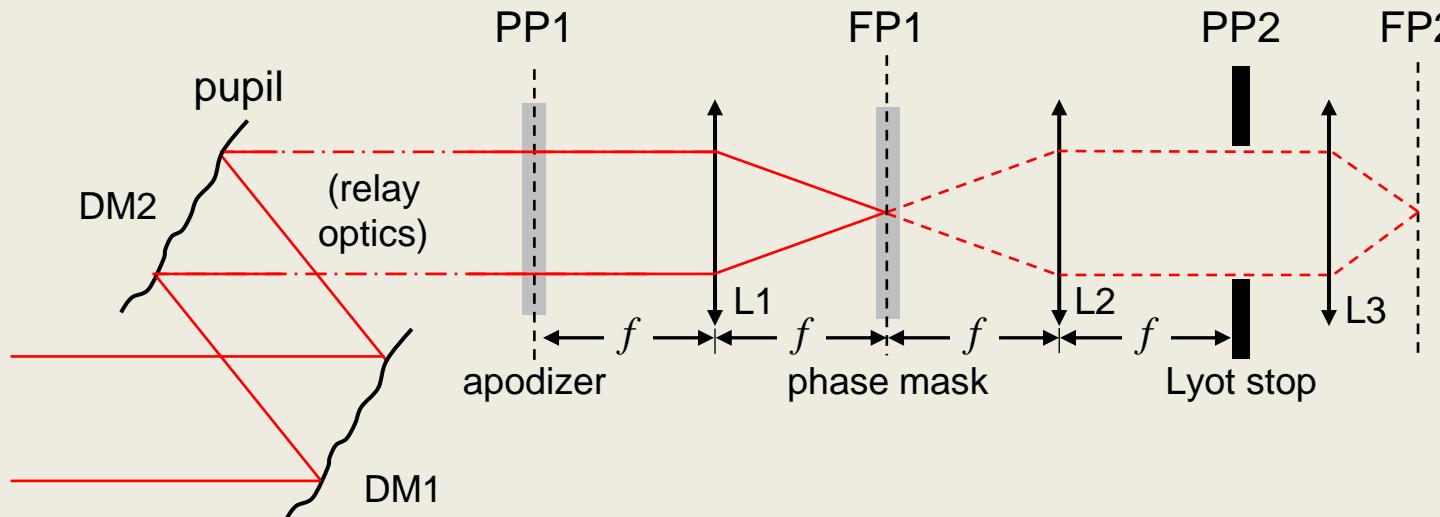
Expected gains with wavefront control



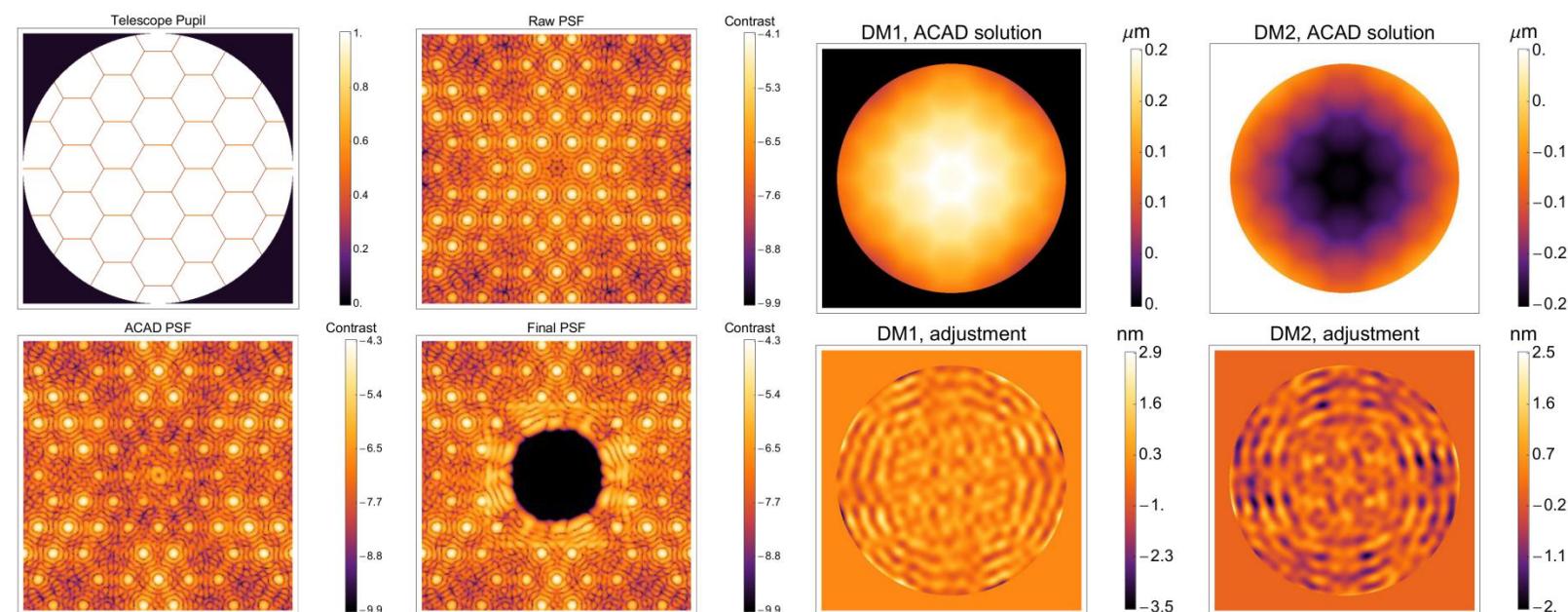
- 1. Develop numerical optimization of grayscale apodizers for VCs.**
- 2. Optimize broadband performance of wavefront control algorithms for VCs on segmented apertures.**
- 3. Investigate potential performance gains by combining wavefront control and optimized coronagraphic masks.**

Extra slides

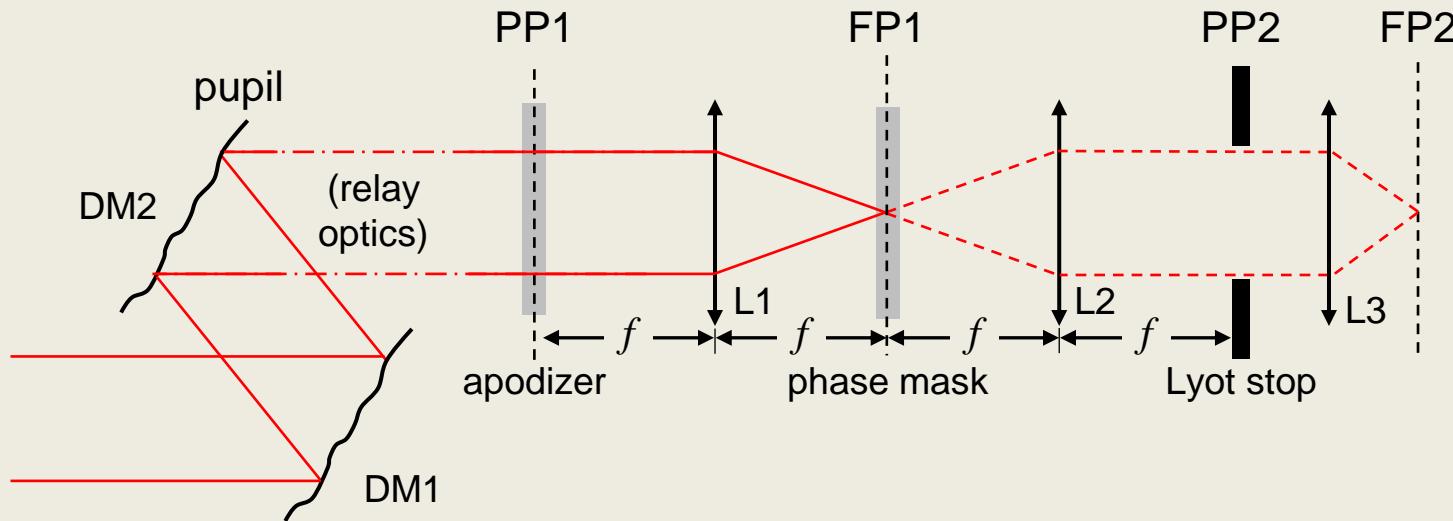
Active Compensation of Aperture Discontinuities (ACAD)



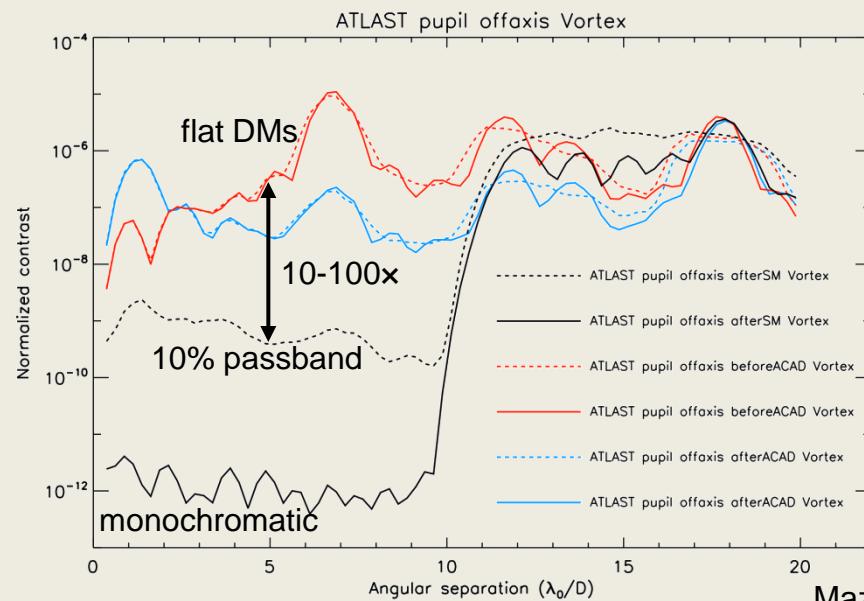
ACAD results from Mazoyer et al. (2015)



Active Compensation of Aperture Discontinuities (ACAD)



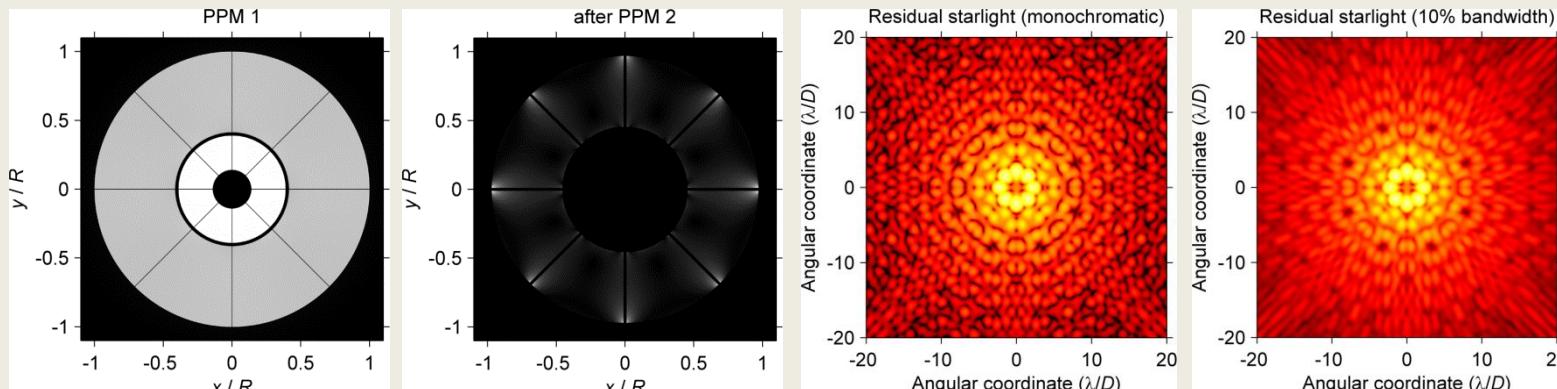
ACAD results from Mazoyer et al. (2015)



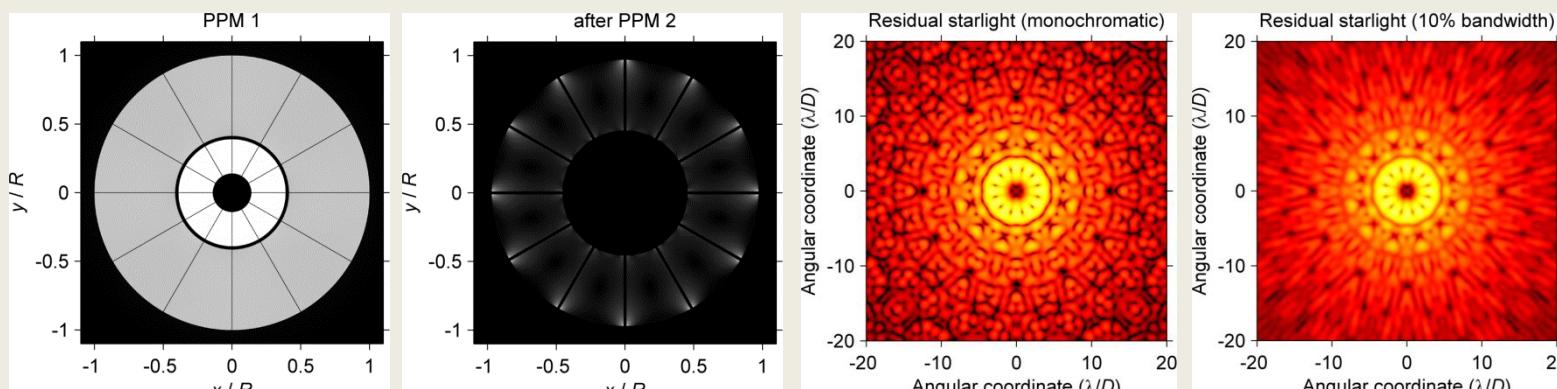
Apodized VC performance with segmented apertures

Analytically-inspired, ring-apodized VC (RAVC) with charge 4

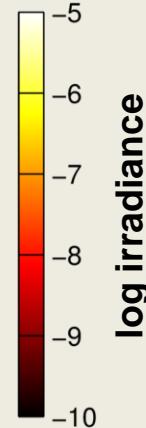
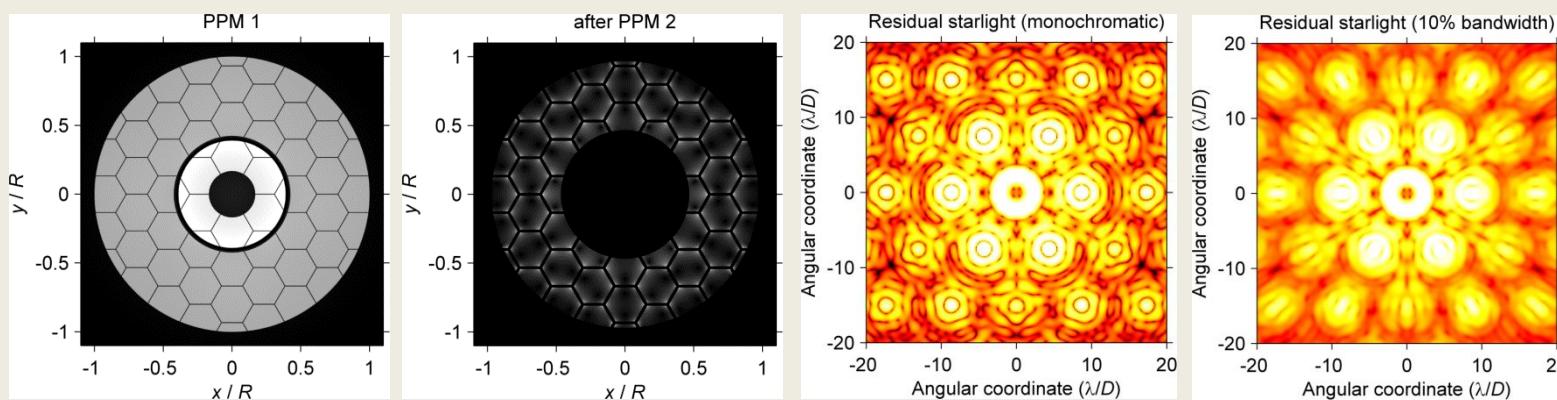
Piewedge 8



Piewedge 12

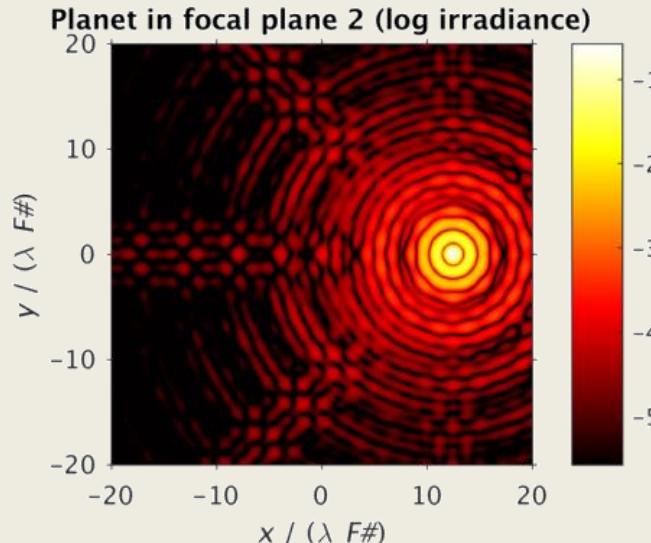
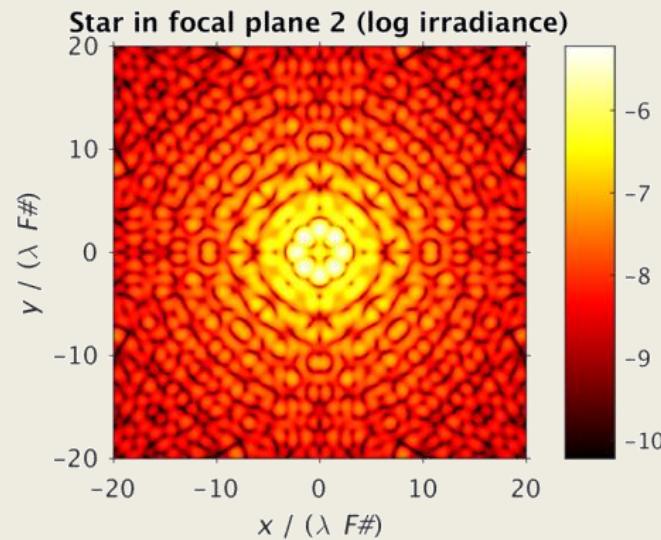
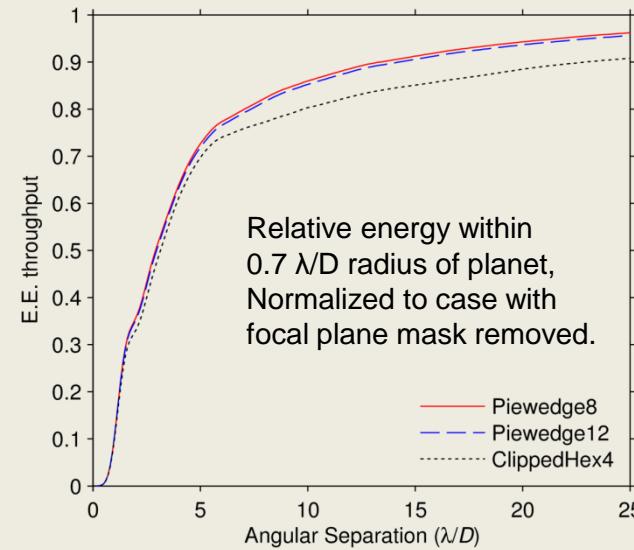
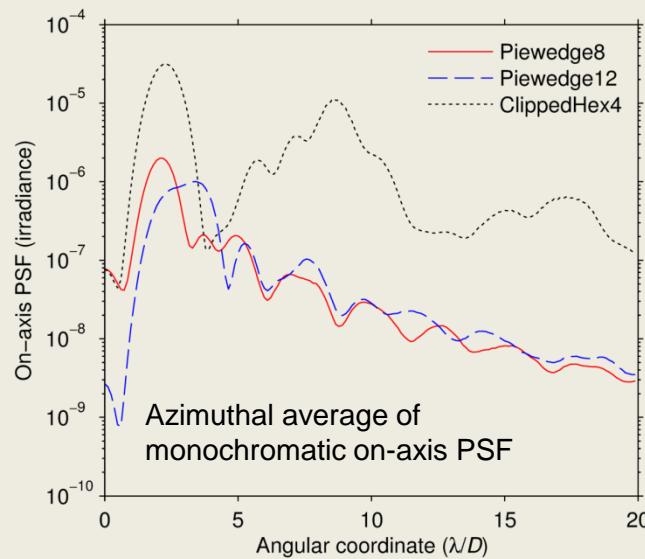


Clipped Hex 4

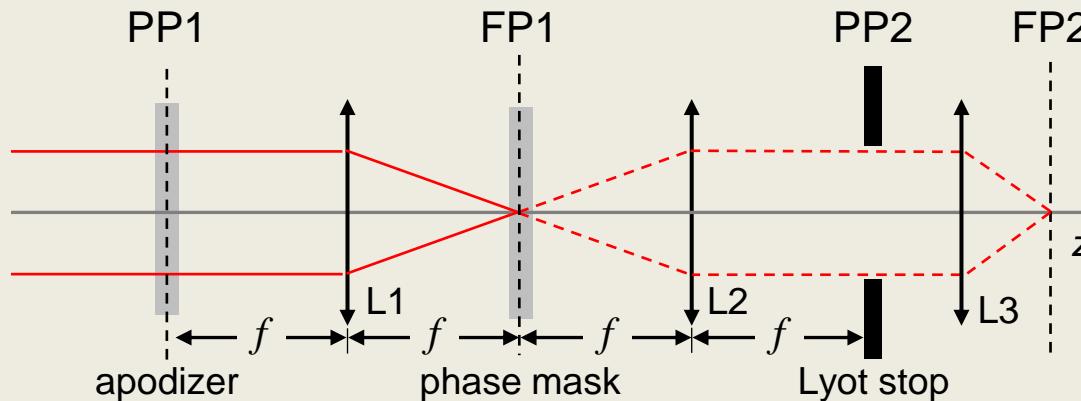


Apodized VC performance with segmented apertures

Analytically-inspired, ring-apodized VC (RAVC) with charge 4

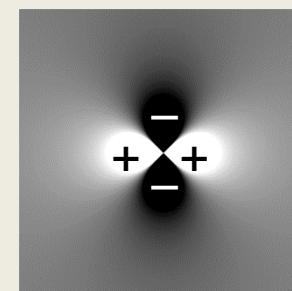


Option I: Optimizing the apodizer

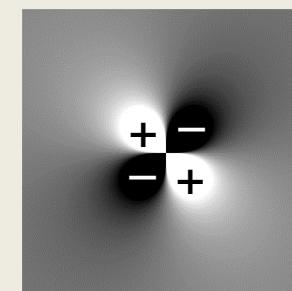


$$VC_l \{ P(x, y) \} = P(x, y) * \underbrace{FT^{-1} [e^{il\phi}]}_{}$$

$$FT^{-1} [e^{il\phi}] = \frac{1}{r^2} e^{il\theta}$$

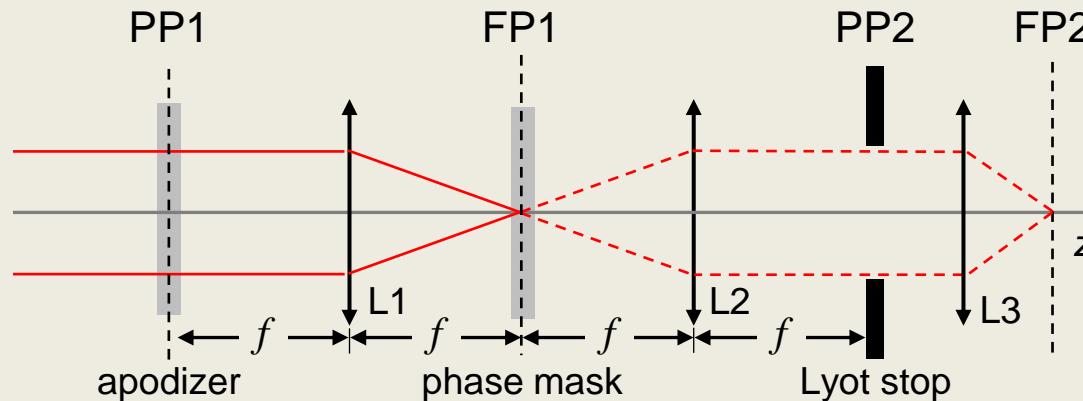


real part



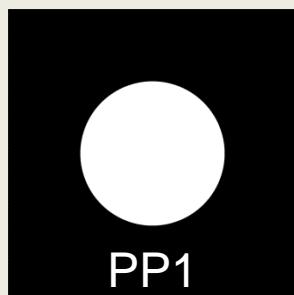
imag. part

Option I: Optimizing the apodizer

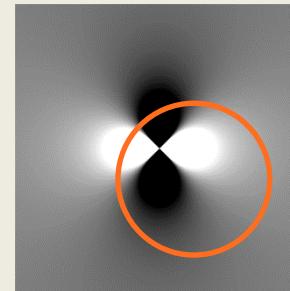
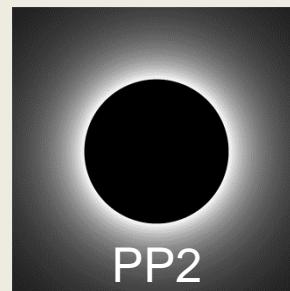


$$VC_l \{P(x, y)\} = P(x, y) * FT^{-1} [e^{il\phi}]$$

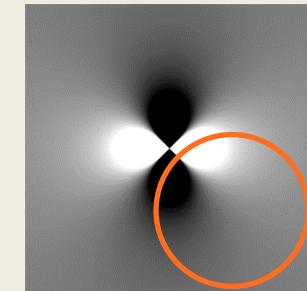
Convolution with a circular pupil



$$* \frac{1}{r^2} e^{i2\theta} =$$



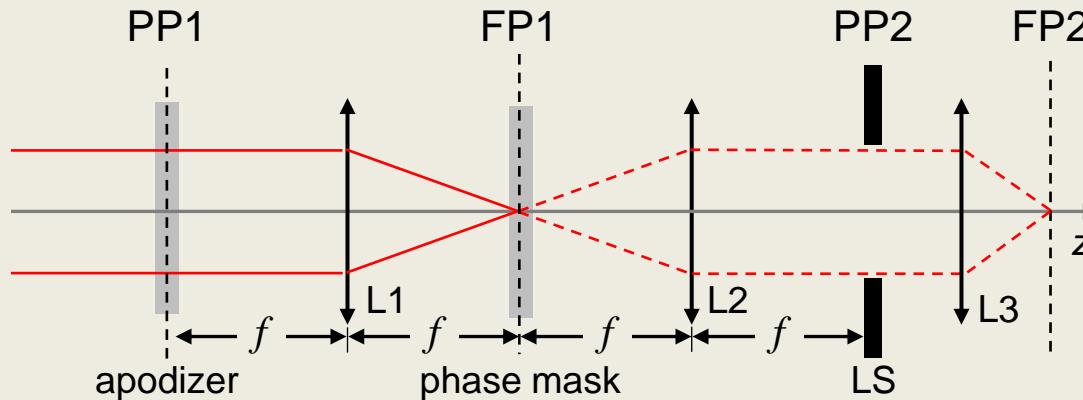
zero
(inside)



non-zero
(outside)

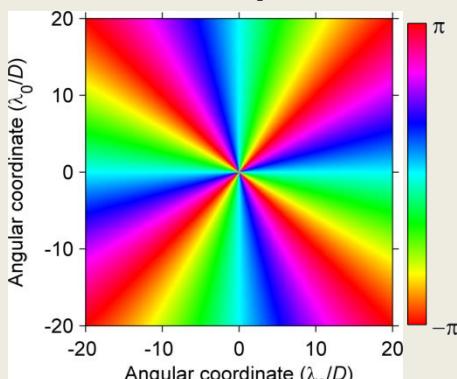
Occurs for nonzero even values of l

Option II: Optimizing the focal plane mask



Broadband FPM optimization process

1. Initial phase



(charge 4 vortex)

2. Solve for new phase at each λ

$$\Phi_1(\lambda_1)$$

$$\Phi_2(\lambda_2)$$

\vdots

$$\Phi_i(\lambda_i)$$

\vdots

$$\Phi_N(\lambda_N)$$

3. Take weighted average of solutions

Achromatic (e.g. liquid crystal):

$$\Phi = \sum_i c_i \Phi_i(\lambda_i)$$

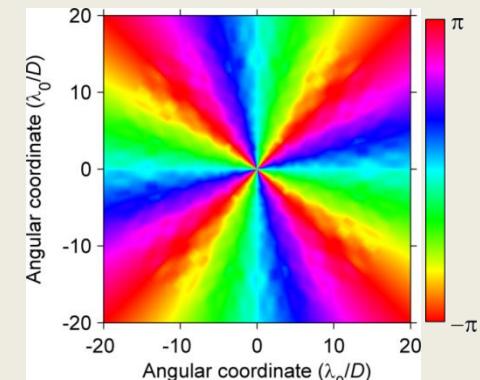
$$M = \exp(i\Phi)$$

Dielectric material:

$$h = \sum_i \frac{c_i \lambda_i}{n(\lambda_i)} \Phi_i(\lambda_i)$$

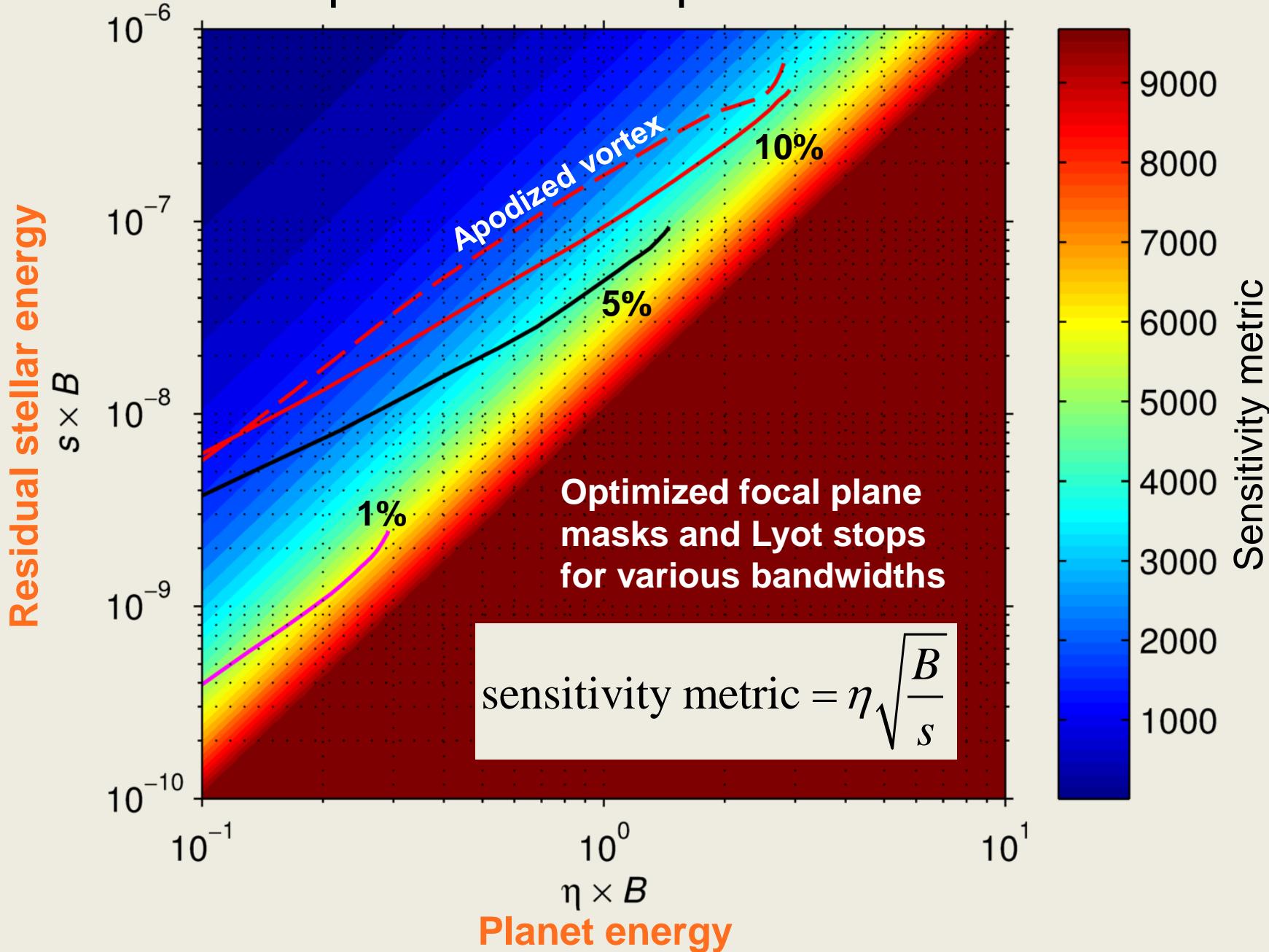
$$M = \exp\left(i \frac{2\pi}{\lambda} n(\lambda) h\right)$$

4. Update phase mask

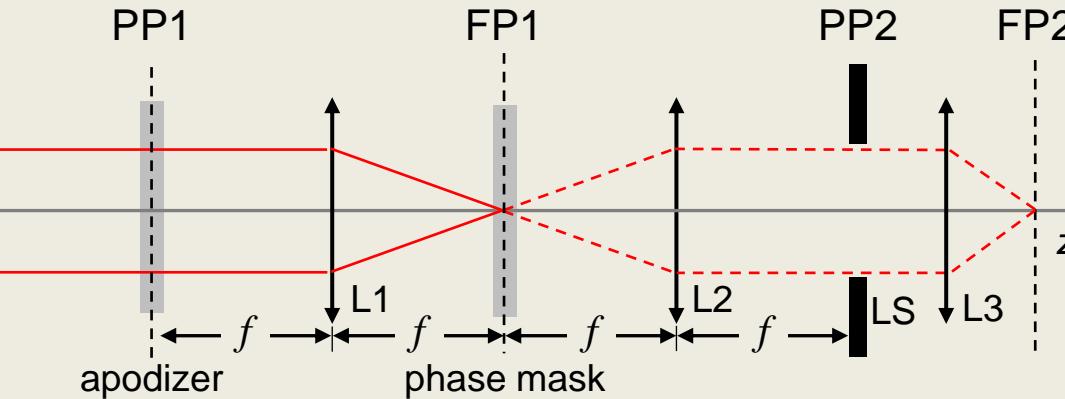


5. Repeat steps 2 - 4

Optimized focal plane masks



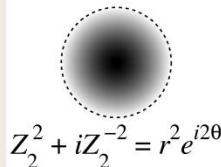
Alternate apodization schemes



Zernike amplitude apodizers

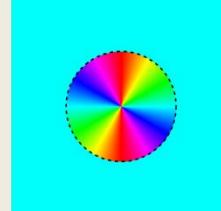
PP1: ampl.

(a)



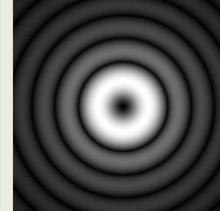
PP1: phase

(a)



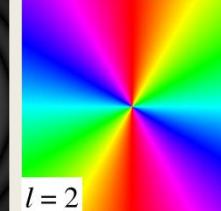
FP1: ampl.

(a)



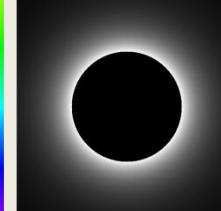
FP1: mask

(a)



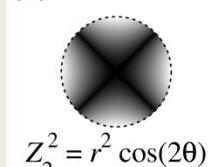
PP2: ampl.

(a)

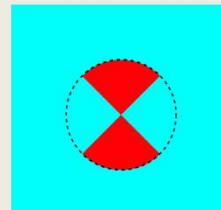
rules

l is even

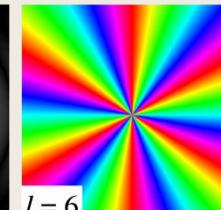
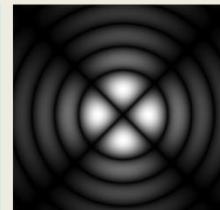
(b)



(b)



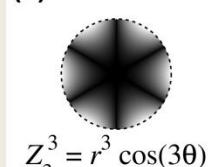
(b)



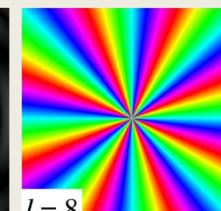
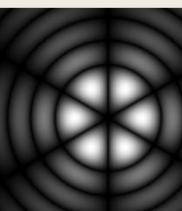
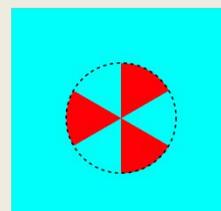
$$P = \sum a_{nm} Z_n^m(\rho, \theta)$$

$$|l| > \max \{n + |m|\}$$

(c)



(c)



$$\text{or } P = \sum b_m r^{|m|} e^{im\theta}$$

$$\text{sgn}(l) = \text{sgn}(m)$$

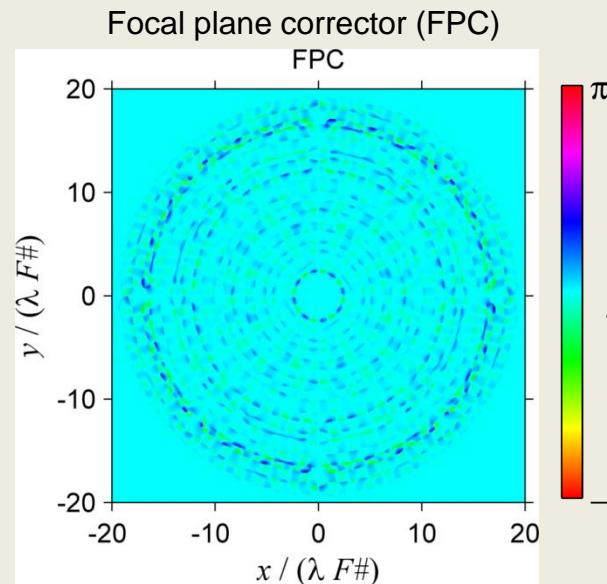
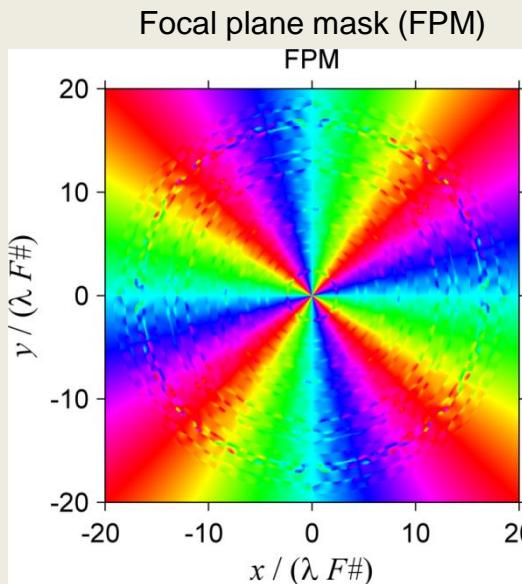
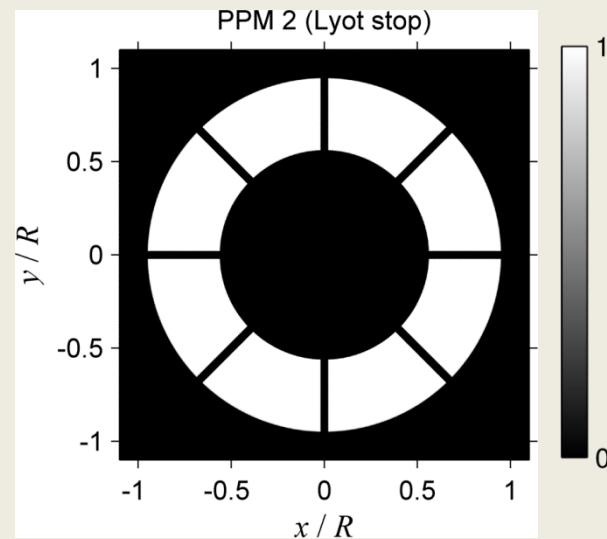
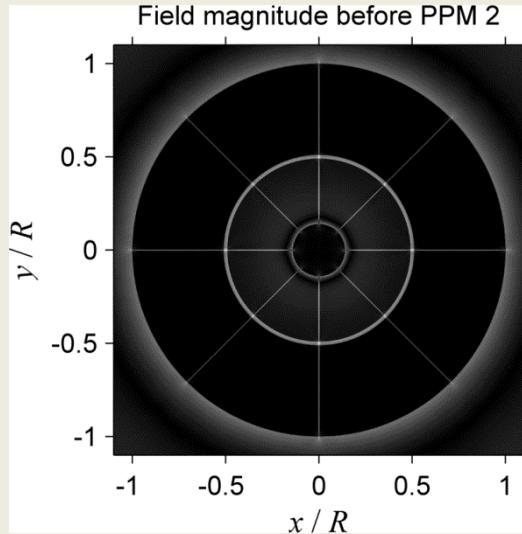
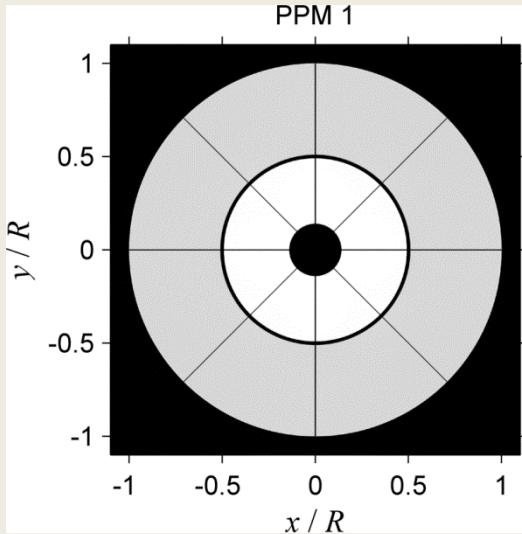
0 amplitude 1

−π phase π

Ruane et al., Proc. SPIE 96051I (2015)

Monochromatic focal plane mask optimization

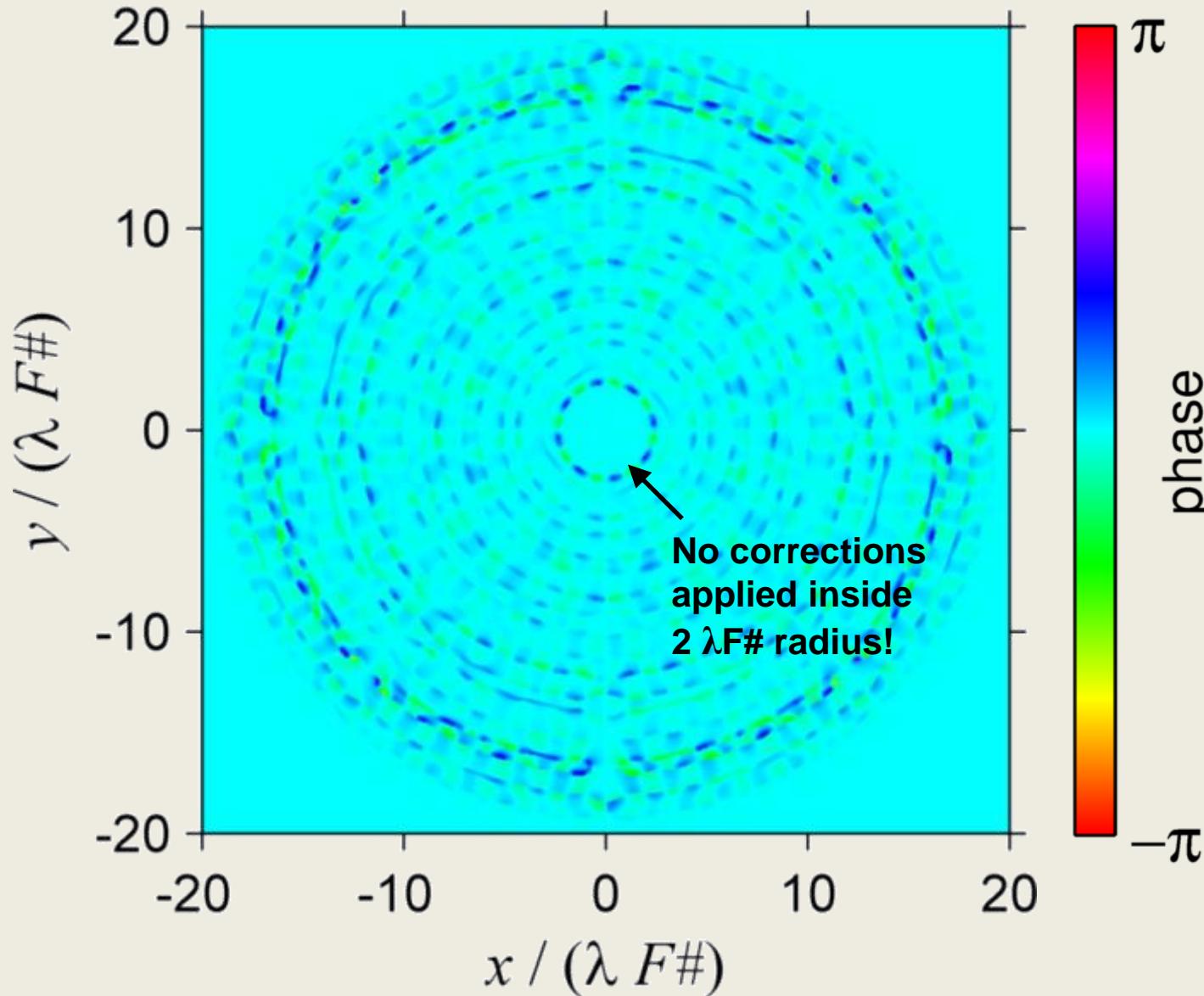
RAVC4 w/ focal plane corrector (FPC)



The focal plane mask (FPM) is numerically optimized to improve starlight suppression at a single wavelength.

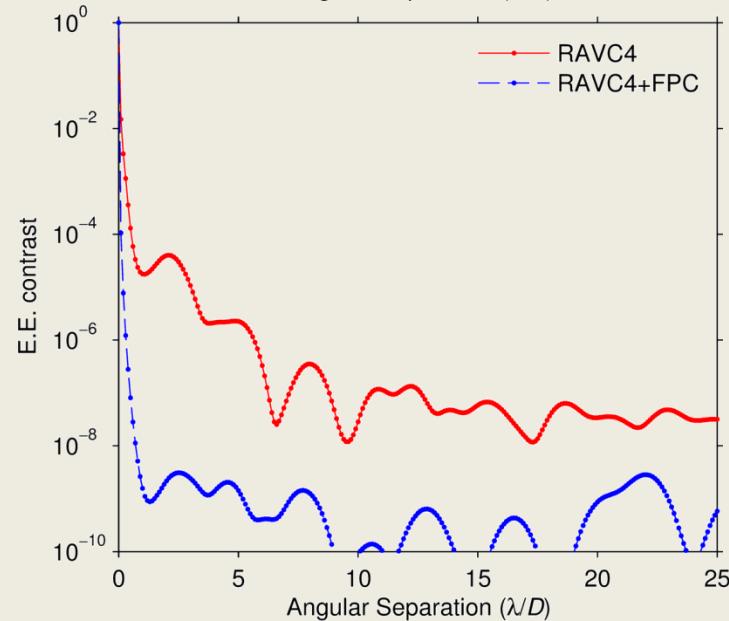
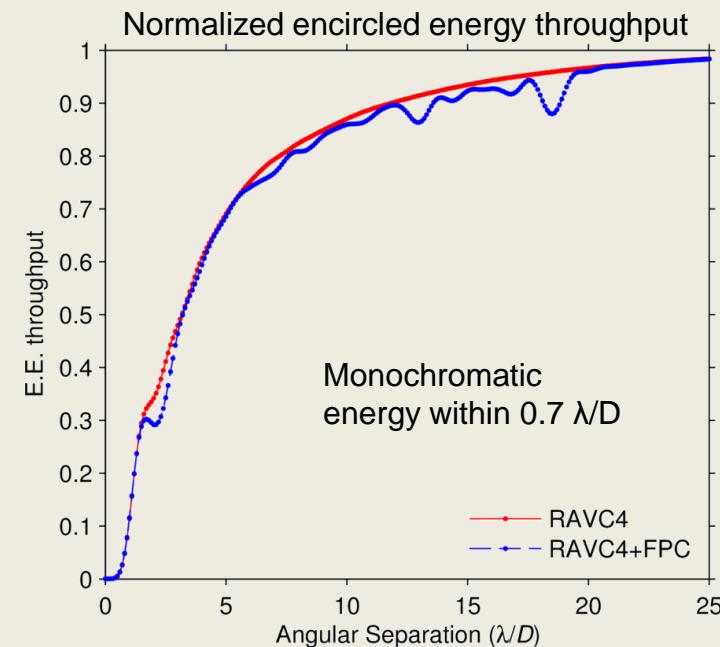
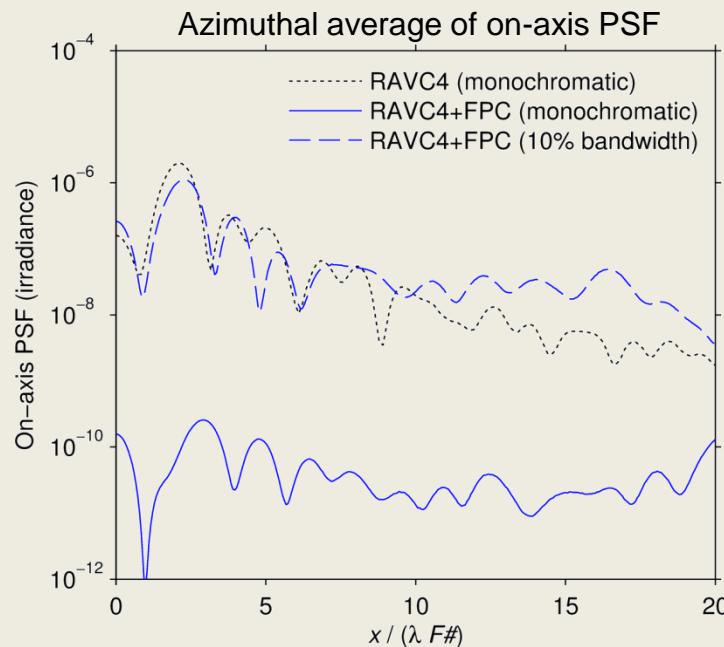
Ruane et al., *Optica* 2, 147 (2015)
Ruane et al., *Proc. SPIE* 9605 11 (2015)

Monochromatic focal plane mask optimization



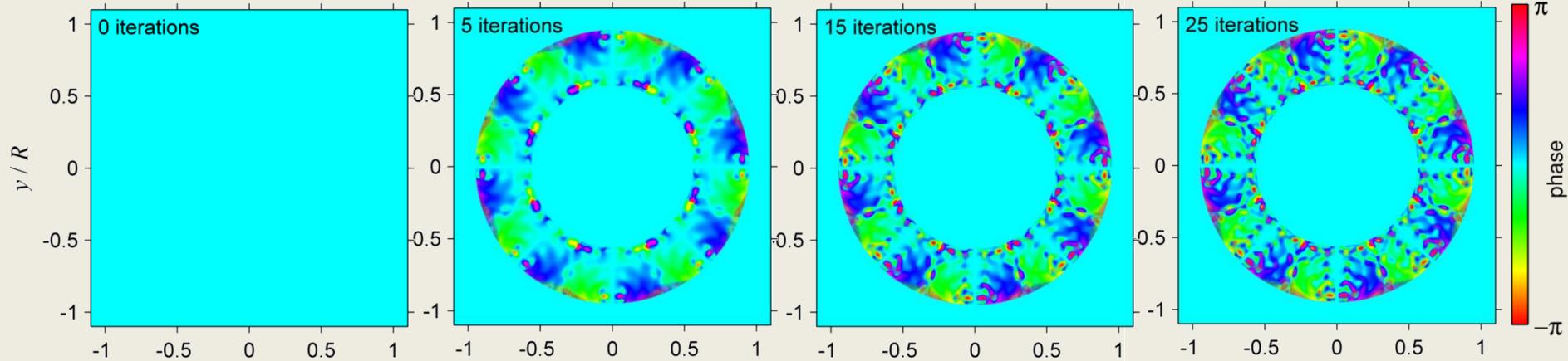
Phase corrections needed for monochromatic suppression.
This will inform the basis used for broadband optimization.

Monochromatic focal plane mask optimization

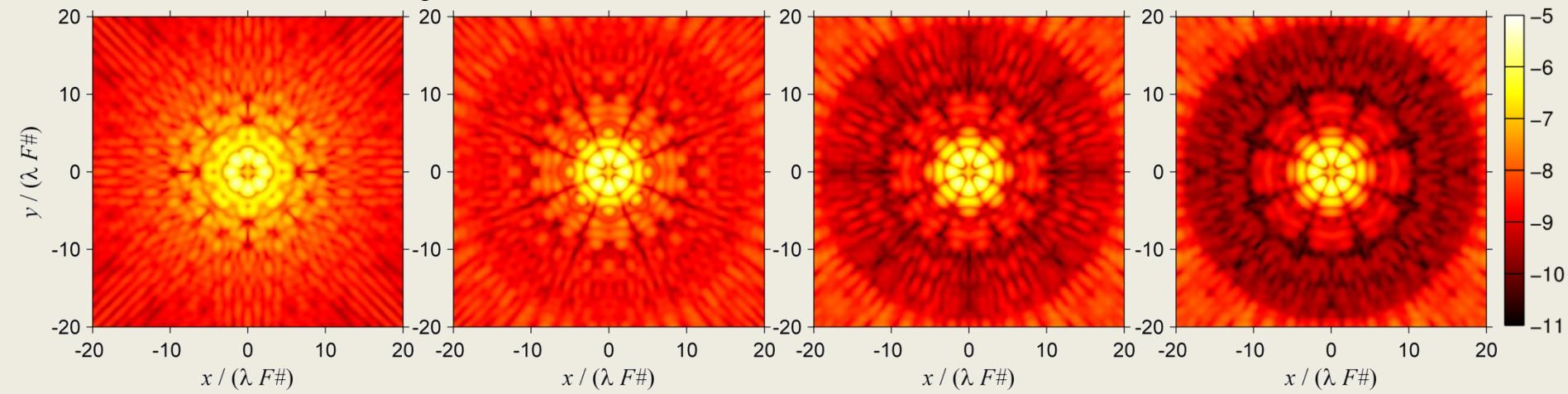


Phase-shifting Lyot plane masks for RAVC4

Phase masks optimized for angular separations of 5-20 λ/D

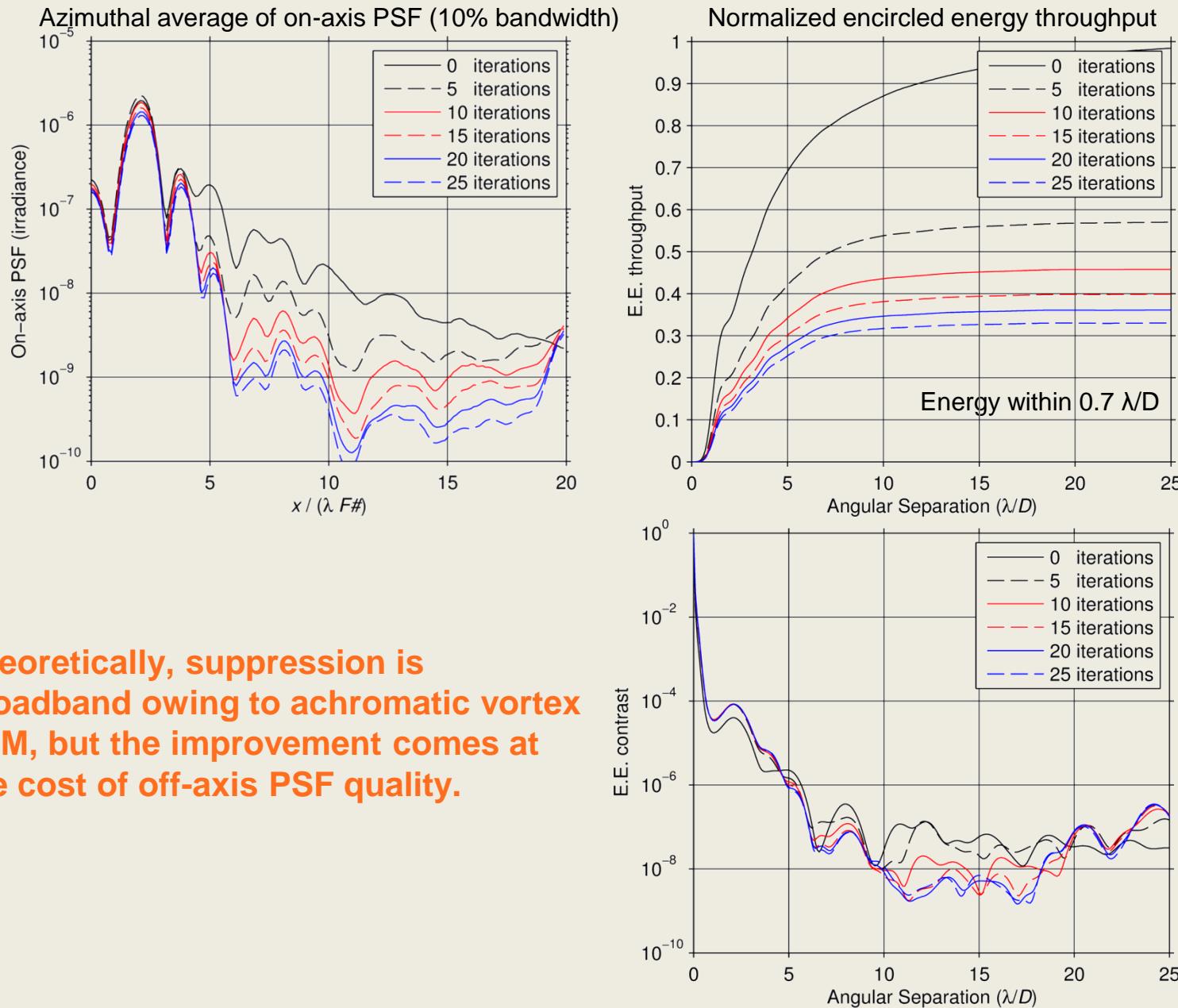


On-axis PSF in normalized log irradiance, 10% bandwidth

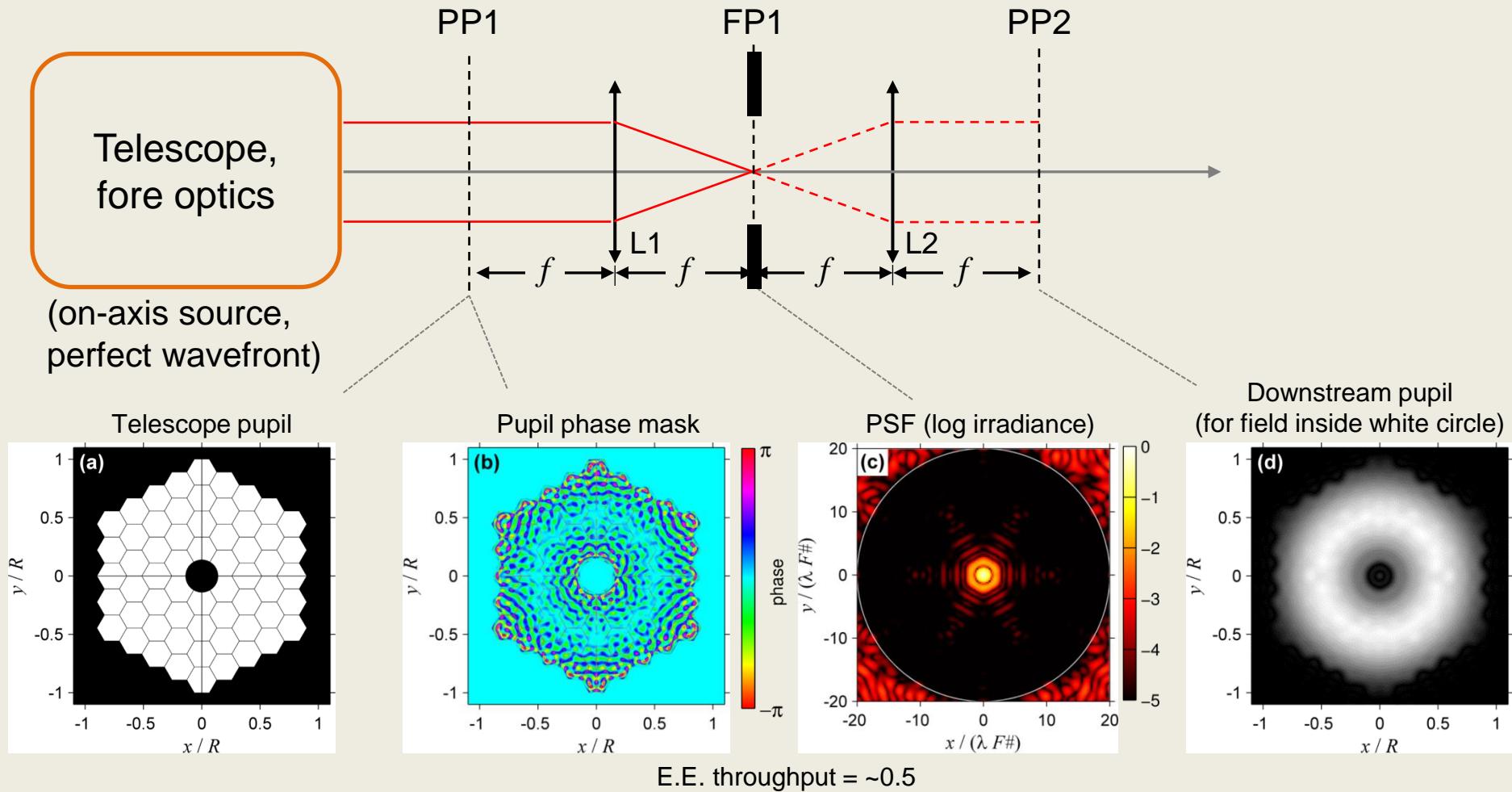


Optimized LPMs for the VC improve the suppression over a substantial spectral bandwidth (achromatic phase shifts assumed)

Phase-shifting Lyot plane masks for RAVC4



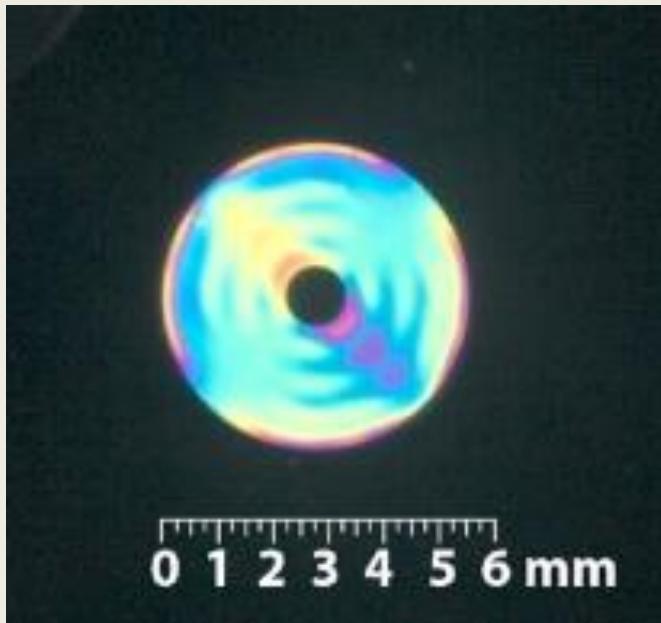
Phase masks designed for apodization



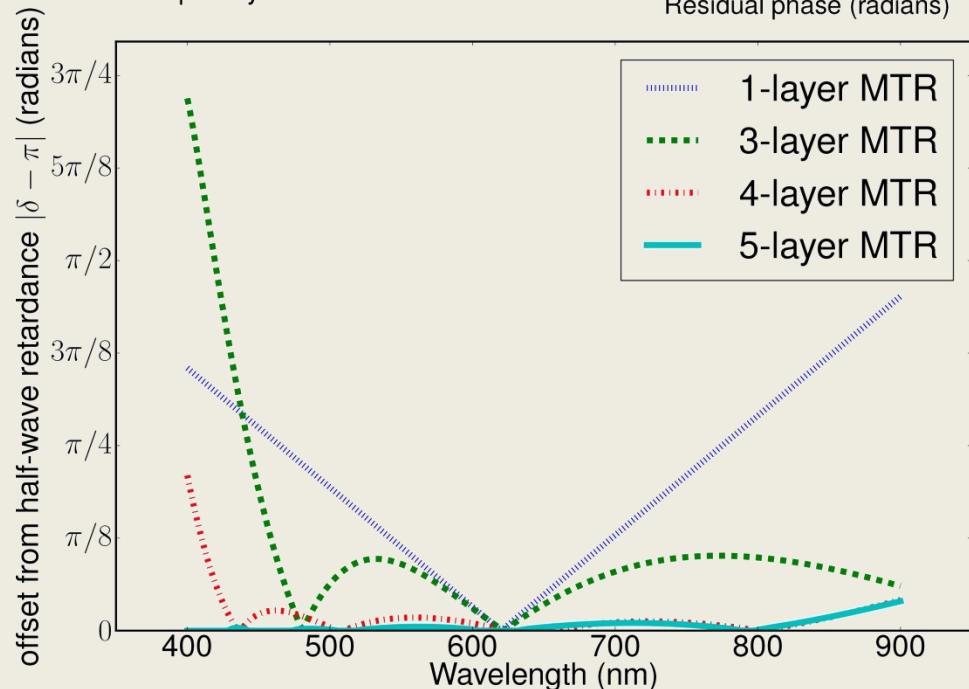
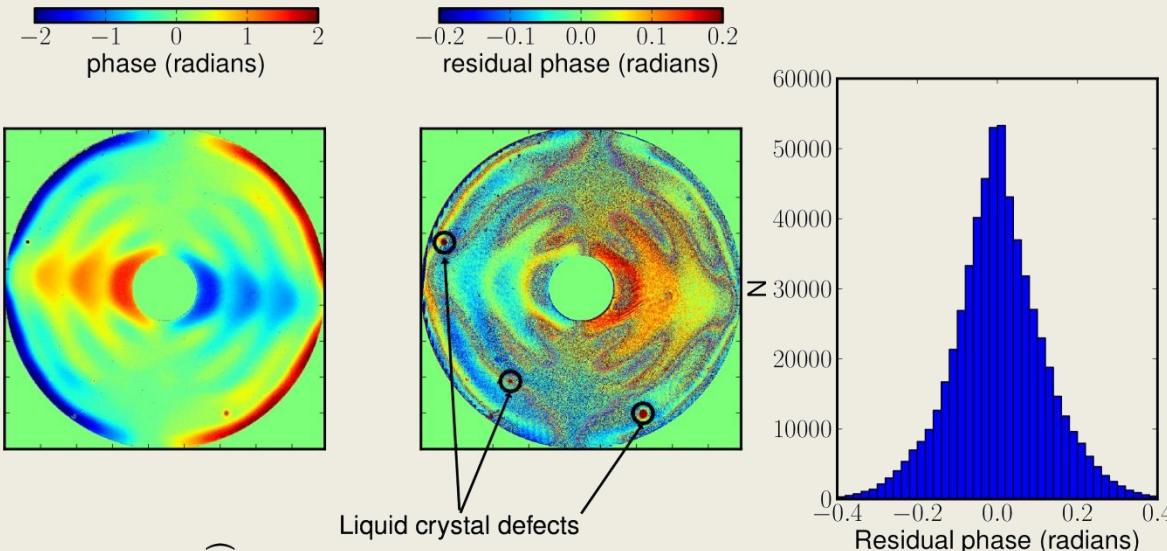
Phase masks may be used to apodize segmented aperture telescopes, effectively erase aperture discontinuities, and maintain high throughput (e.g. w.r.t. shaped pupils).

Achromatic phase mask technologies

Vector phase masks
photo-aligned liquid crystal



Vector phase mask imaged through crossed polarizers



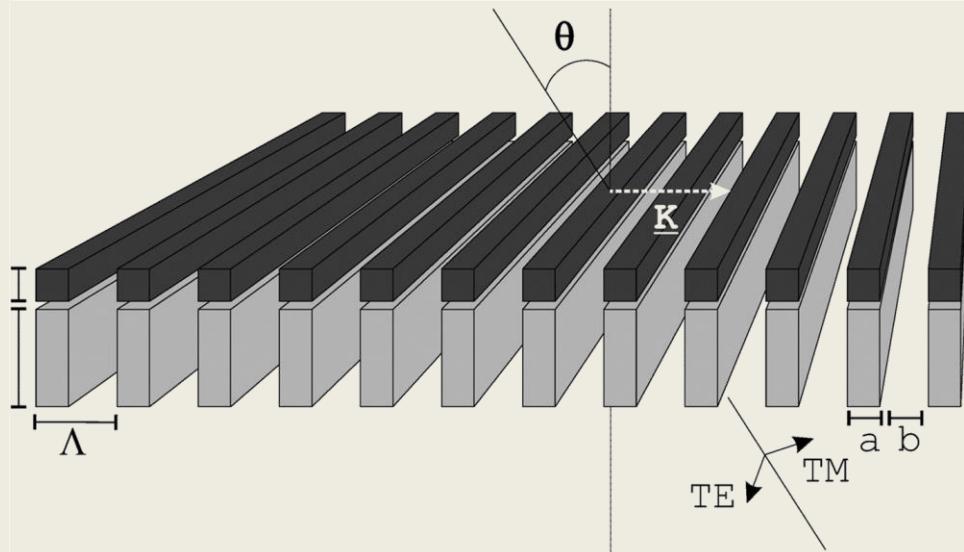
Otten et al., *Opt. Express* 22, 30287 (2014)

Miskiewicz and Escuti, *Opt. Express* 22, 12691 (2014)

Komanduri et al. *Opt. Express* 21, 404 (2013)

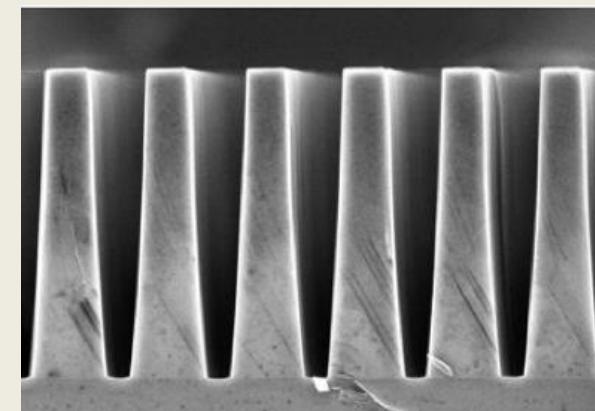
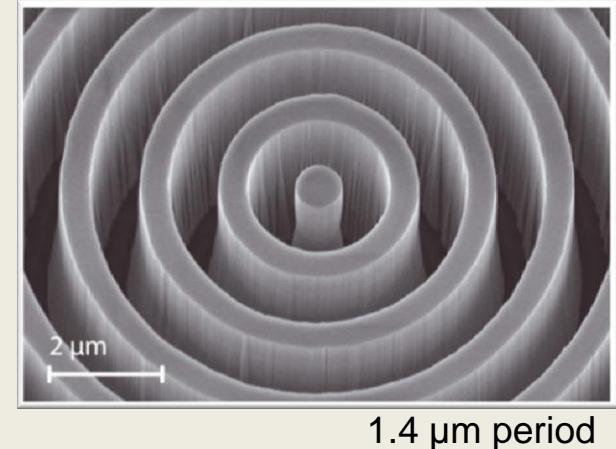
Achromatic phase mask technologies

Vector phase masks subwavelength gratings



Phase shift depends on direction of grating.

Annular groove phase masks (AGPM) L band (Sep 2012)



- Delacroix et al., *A&A* 553, A98 (2013)
- Mawet et al., *Appl. Opt.* 44, 7313 (2005)
- Bomzon et al., *Opt. Lett.* 26, 1424 (2001)