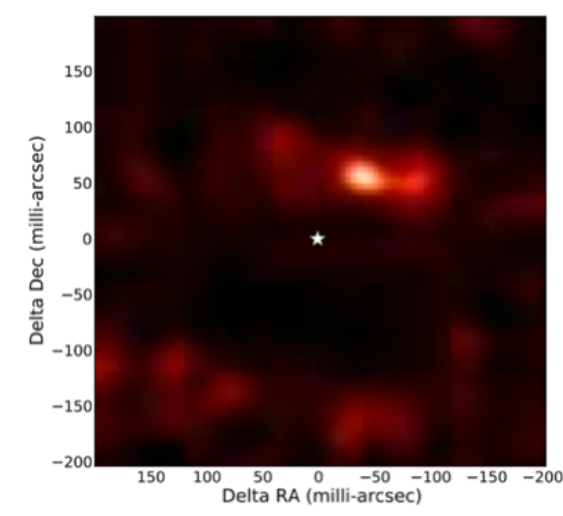


Aperture masking and kernel phases: extracting cophasing errors from science data.



Michael Ireland *On behalf of* collaborators: Benjamin Pope (Oxford), Adam Kraus, Trent Dupuy (UT Austin), Frantz Martinache (Nice OCA), Peter Tuthill, Barnaby Norris (University of Sydney), Olivier Guyon (Subaru/Arizona), Simon Gross, Alex Arriola (Macquarie)

Topics I would like to see covered:

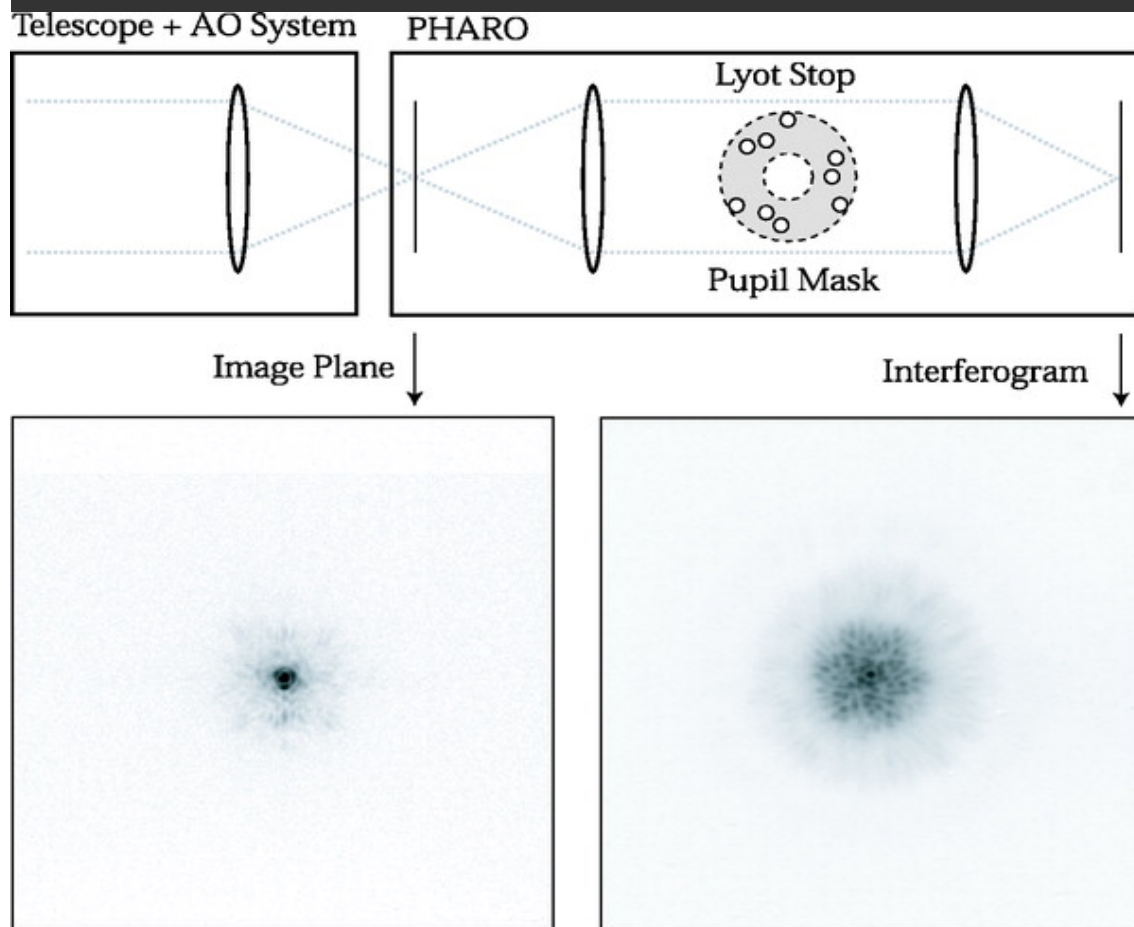
- - using Kphases for precise sensing of cophasing errors from focal plane images
- how does the technique extend to coronagraphic images ?
- - coherent photonics nulling as an alternative to conventional mask-based coronagraphy
- advantages for segmented apertures, precursor systems (photonics nuller on Subaru ?)

Outline

- Aperture Masking and Kernel-Phase/eigenphase Background
- Using an asymmetric pupil for wavefront sensing.
- Wavefront sensing for GMTIFS: intra/extra-focal images or asymmetric pupil.
- Photonic pupil segmentation and nulling: convenient phase and amplitude control with high null depth?



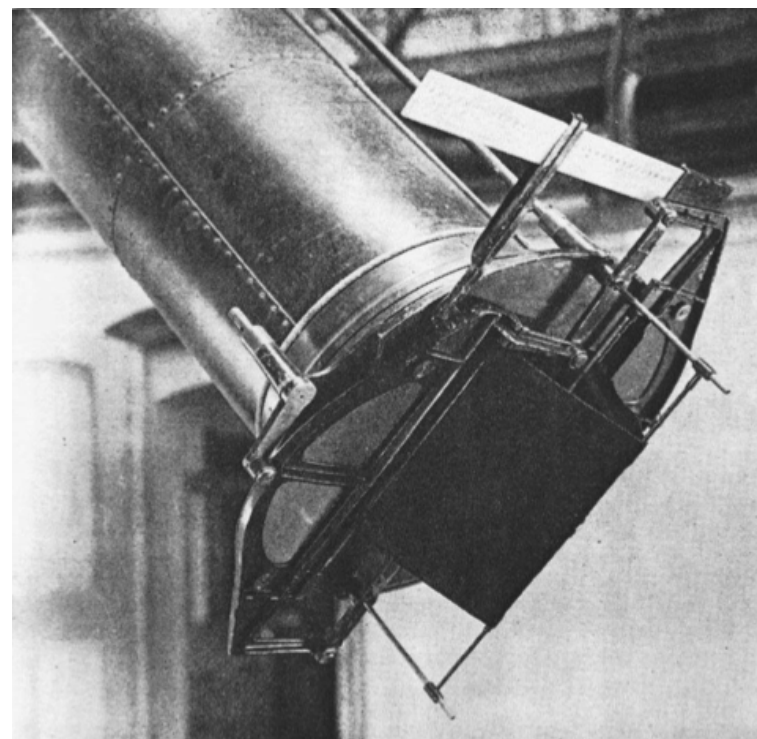
Aperture Mask Interferometry



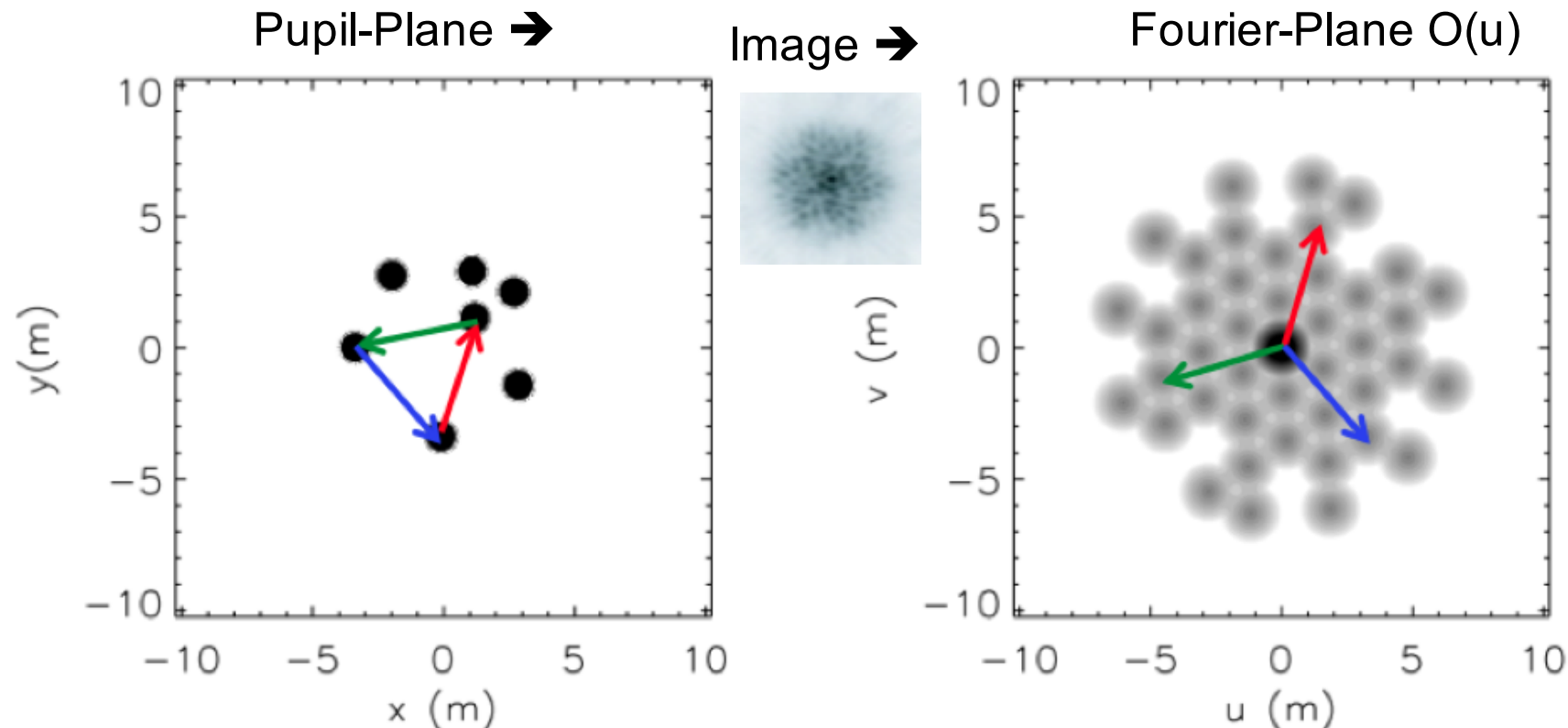
Placing an aperture mask in the pupil plane *cleans up* aberrations like defocus, coma etc.

This enables better calibration of images, and has been used as a high-resolution imaging technique for more than 100 years (although only 2 holes before 1980).

Right: Michelson in ~1890...



Aperture Mask Interferometry



- The primary observables are typically derived from the image Fourier-transform, which is *the auto-correlation* of the pupil function for a point-source.

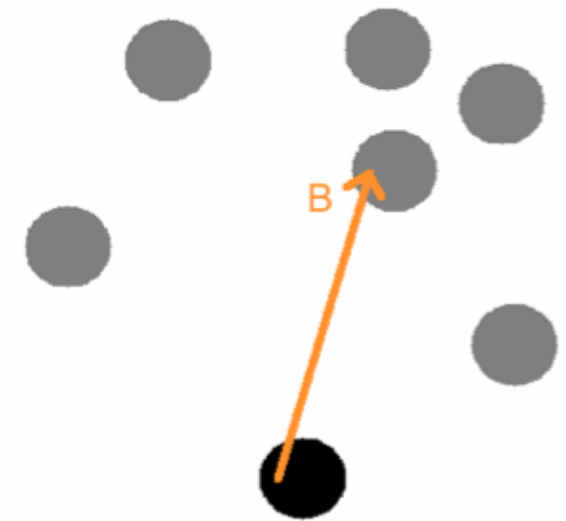
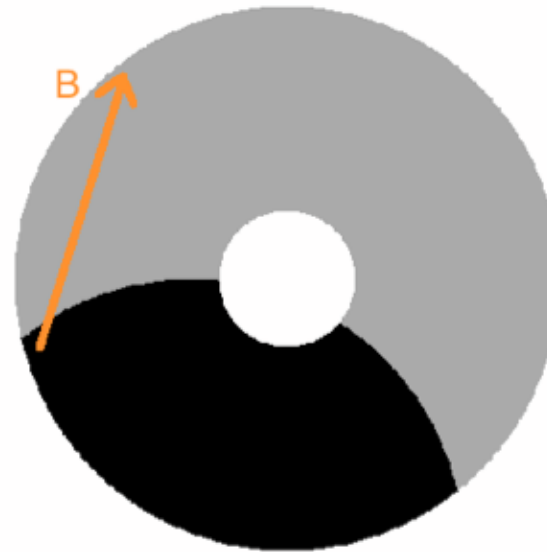
$$i(\alpha) = m(\alpha) * o(\alpha)$$

$$I(\mathbf{u}) = M(\mathbf{u}) \cdot O(\mathbf{u})$$

- An image i is formed by the convolution of a PSF m and the true object o . This is simply multiplication in the Fourier domain – as long as most of the Fourier plane is covered, the object information is available.

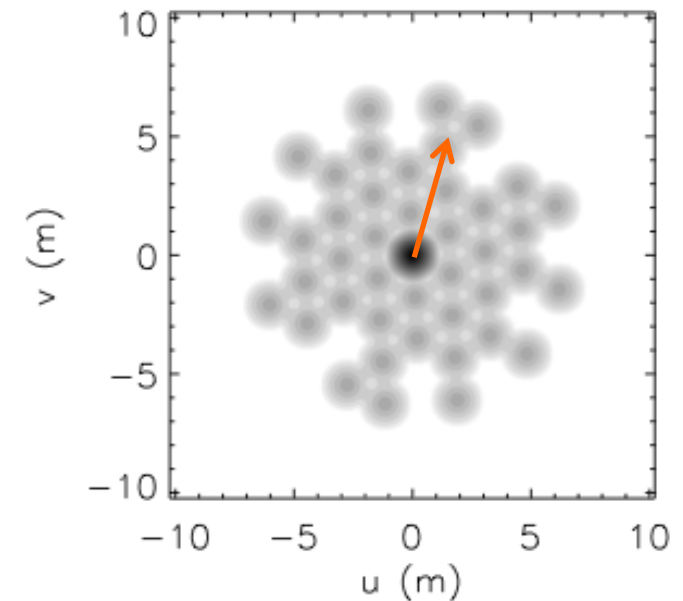
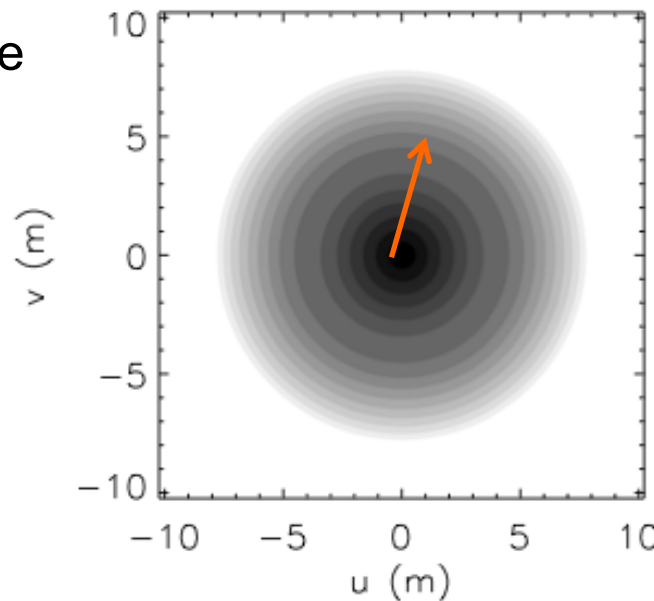
Full Pupil Versus SAM/NRM

In the (u,v) or Fourier-plane (image Fourier transform), Sparse Aperture Masking (SAM, Europe) or Non-Redundant Masking (NRM, US) has a much smaller pupil-plane footprint for each baseline compared to a full pupil.



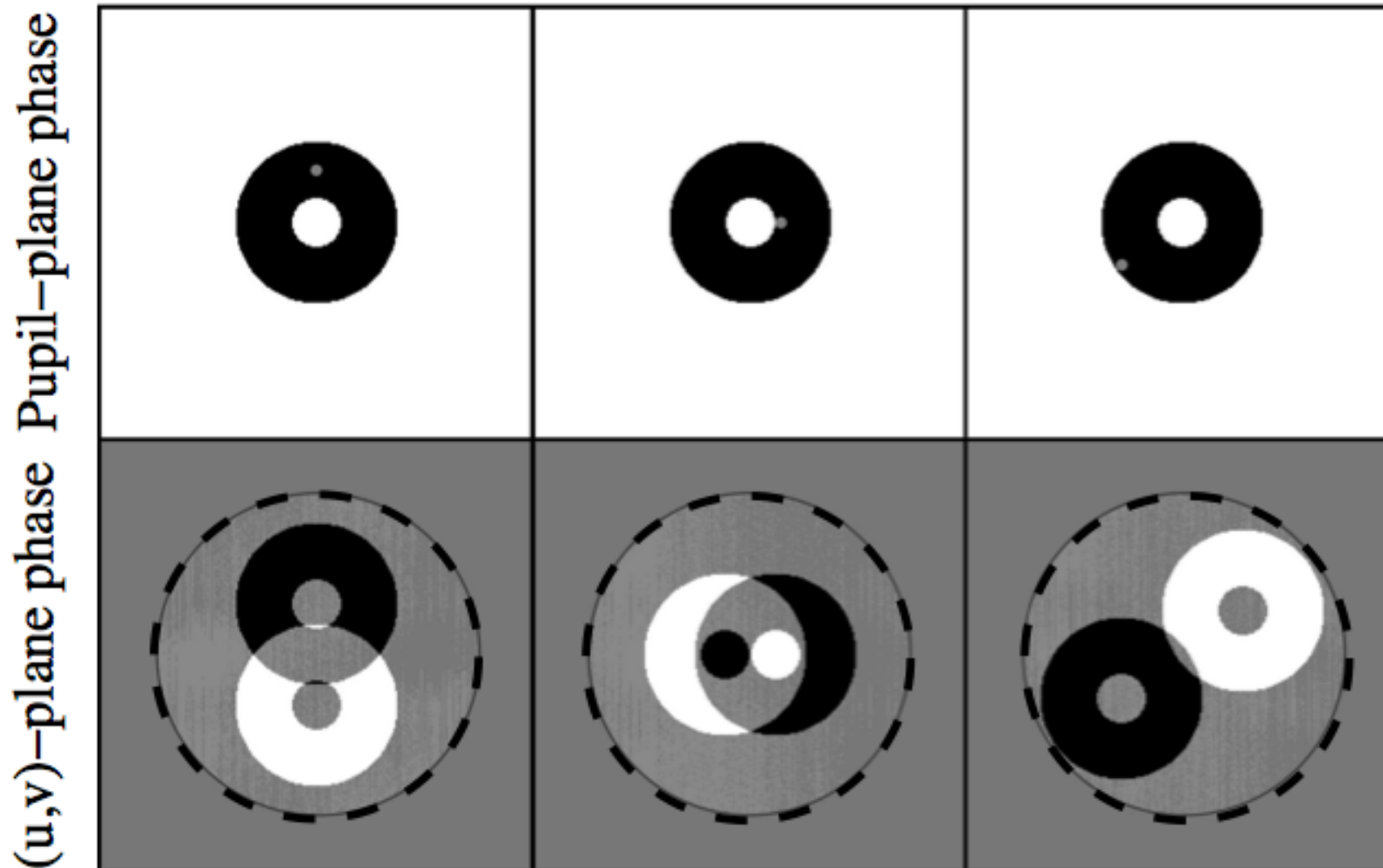
However, the (u,v) -plane remains mostly filled.

Despite losing light, high-angular resolution information is retained and calibrates better.



Kernel Phase

There is *always* more phase information in the (u,v) -plane than the pupil-plane. This extra information is the *Kernel-Phase* (Martinache 2010) and represents the smallest principle components of Fourier phase on point source images.





Example: High Strehl (full pupil)

Pupil Phase $\Rightarrow$

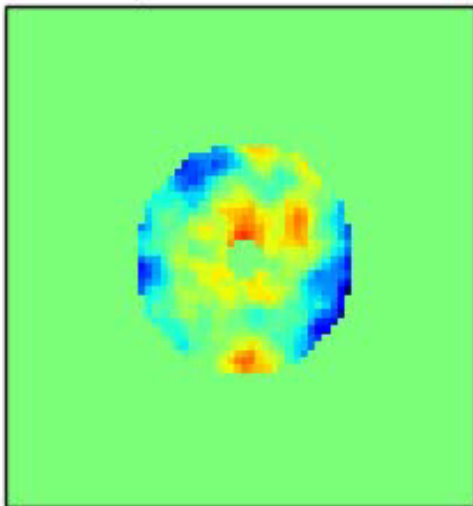
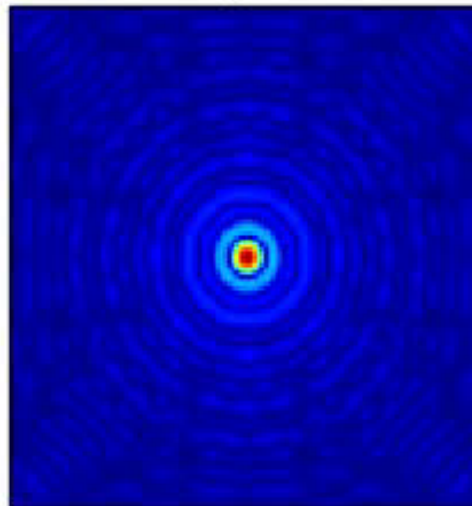
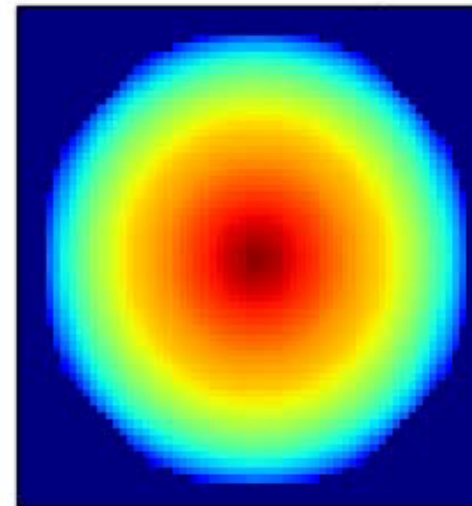


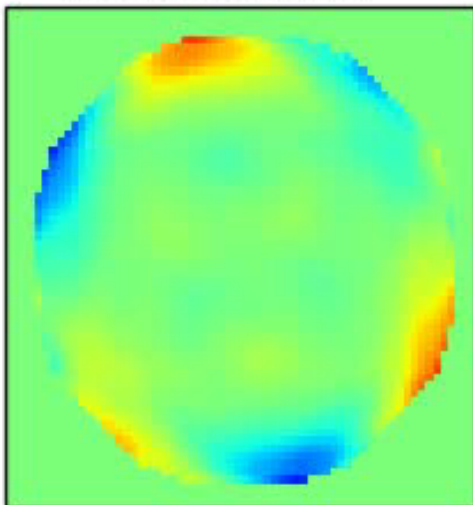
Image $\Rightarrow$



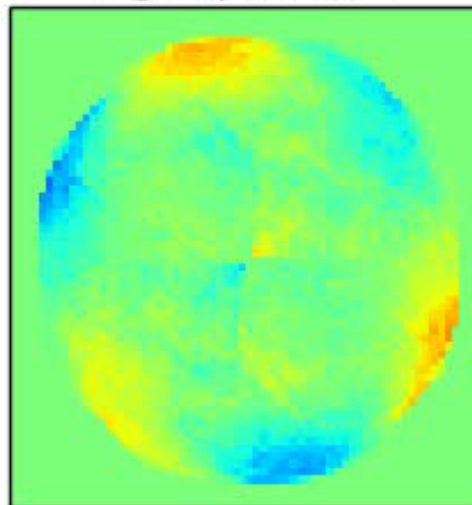
Fourier Plane (amplitude)



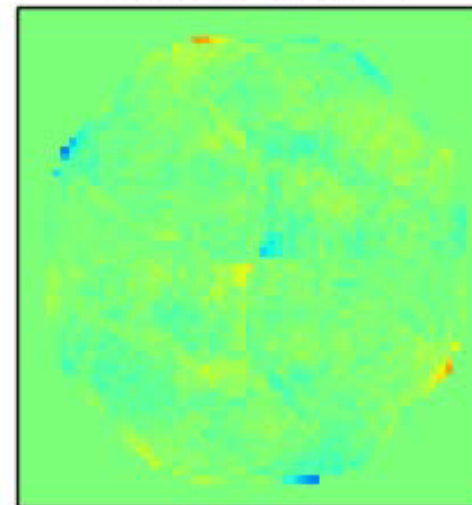
Fourier Phase =



Eigenphase +



Kernel Phase





Example: High Strehl (9h mask)

Pupil Phase $\Rightarrow$

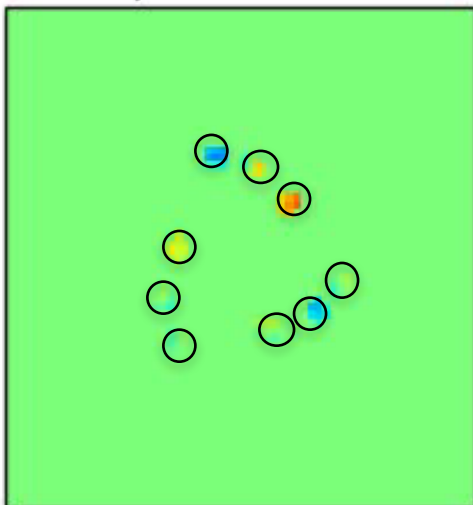
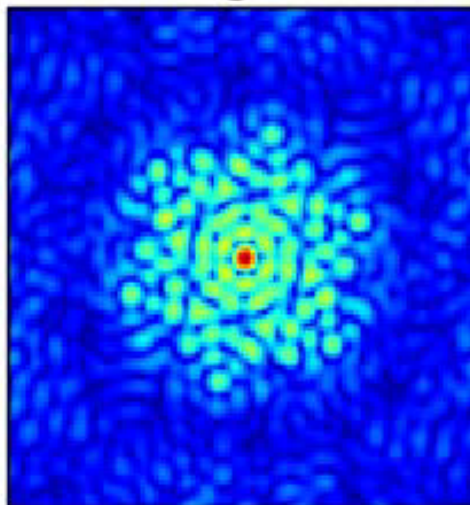
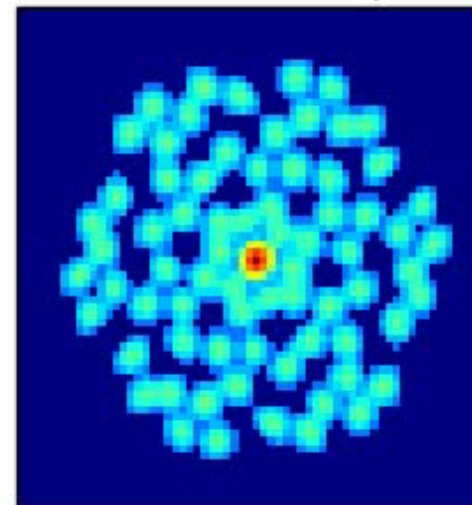


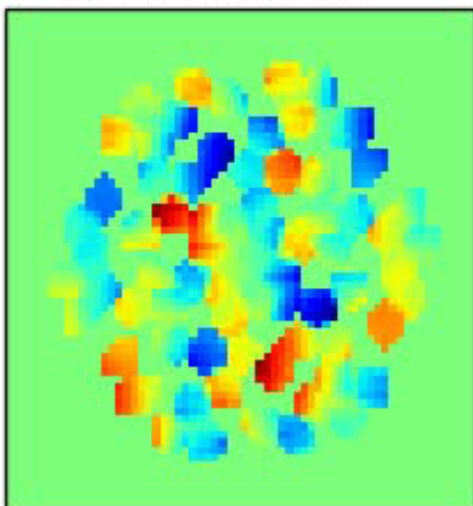
Image $\Rightarrow$



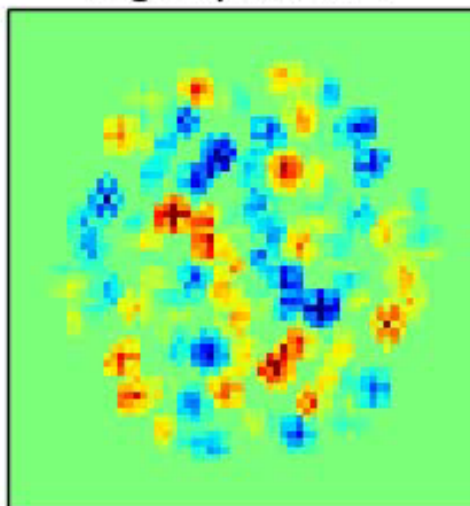
Fourier Plane (amplitude)



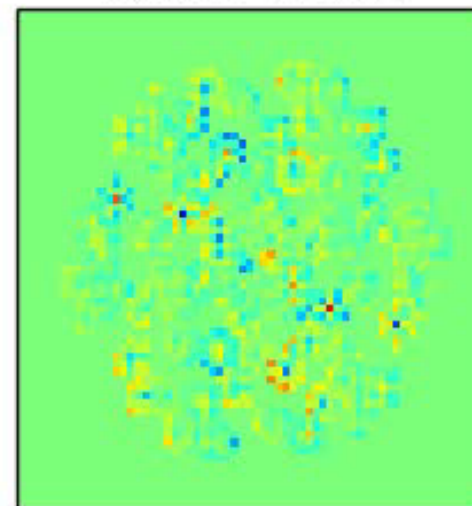
Fourier Phase =



Eigenphase +



Kernel Phase





Example: Low Strehl (full pupil)

Pupil Phase $\Rightarrow$

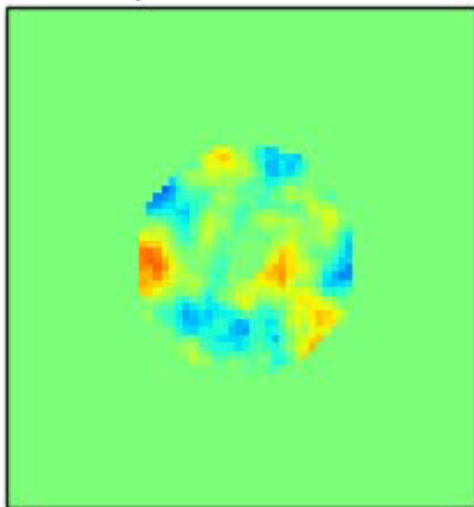
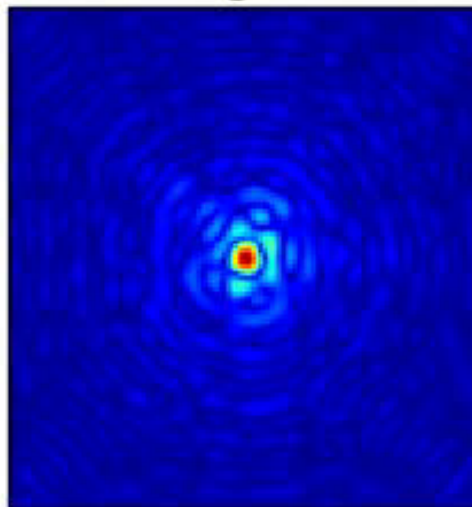
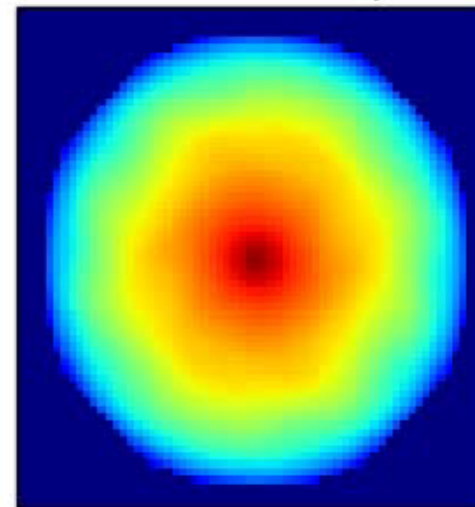


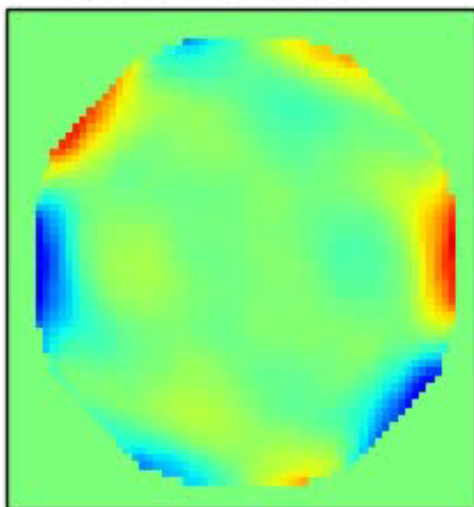
Image $\Rightarrow$



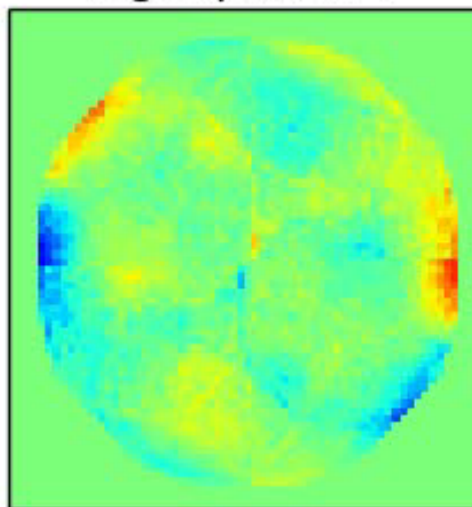
Fourier Plane (amplitude)



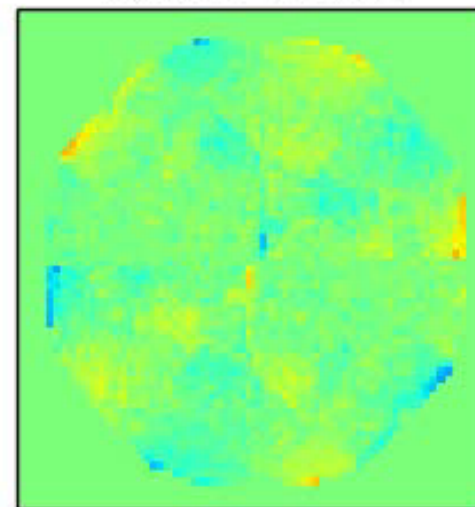
Fourier Phase =



Eigenphase +



Kernel Phase





Example: Low Strehl (9h mask)

Pupil Phase $\Rightarrow$

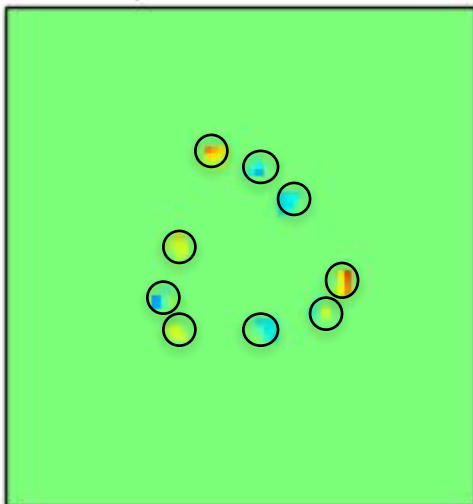
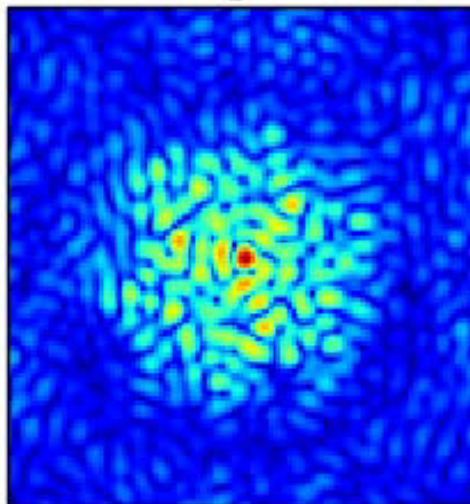
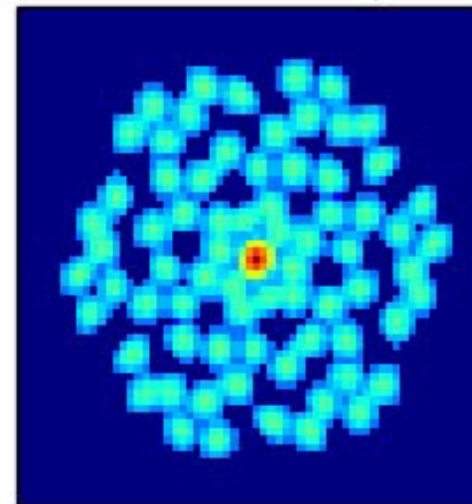


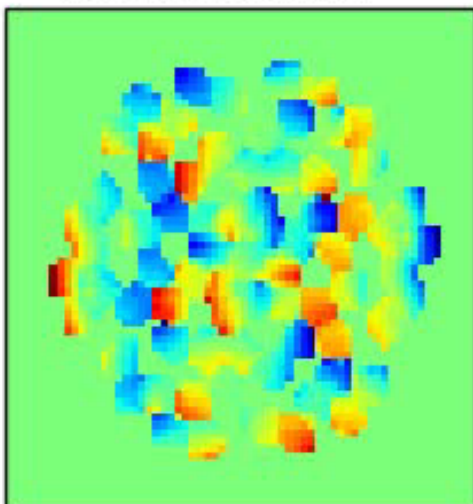
Image $\Rightarrow$



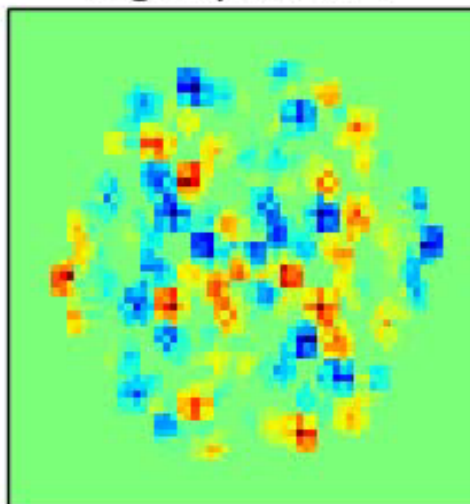
Fourier Plane (amplitude)



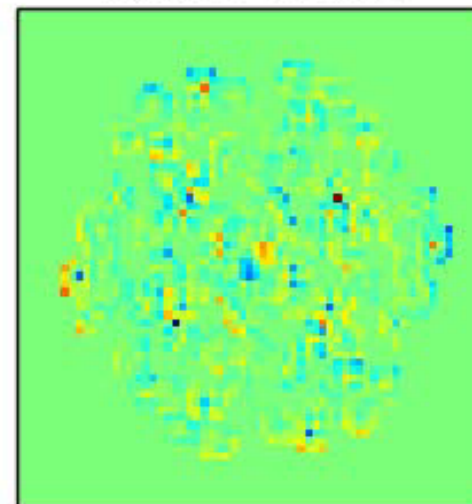
Fourier Phase =



Eigenphase +



Kernel Phase





Example: With Binary (full pupil)

Pupil Phase $\Rightarrow$

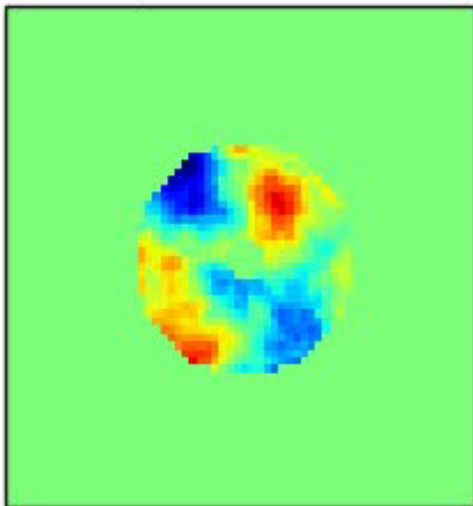
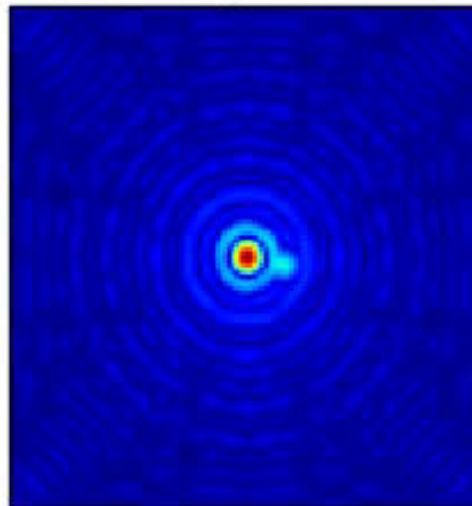
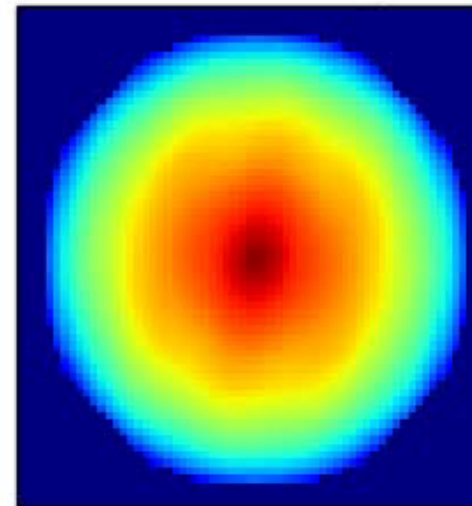


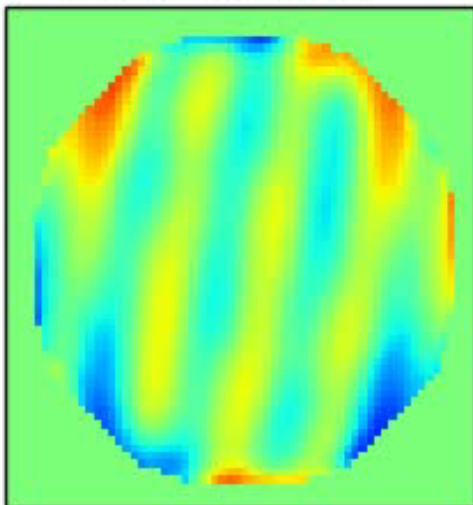
Image $\Rightarrow$



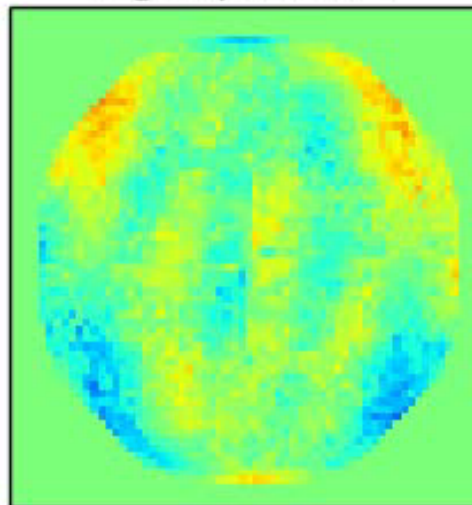
Fourier Plane (amplitude)



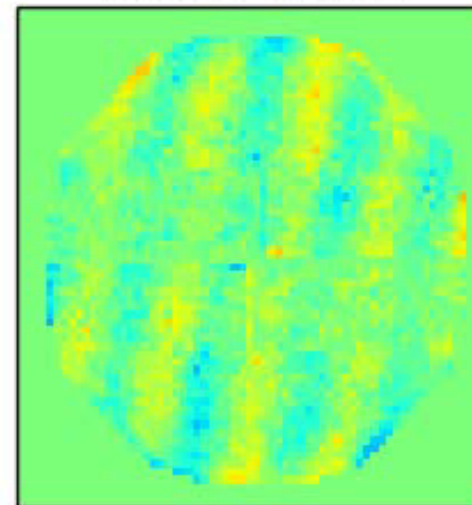
Fourier Phase =



Eigenphase +



Kernel Phase

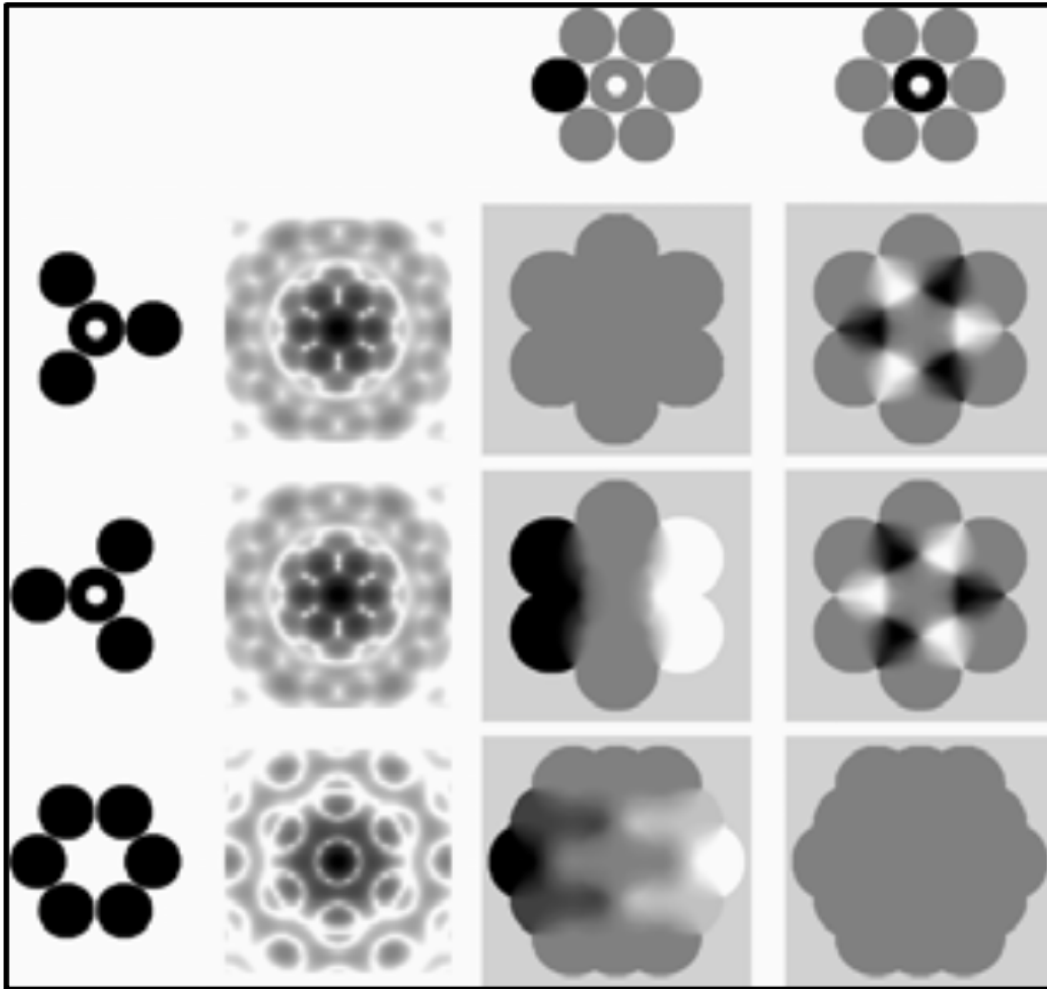


Five recent published/submitted) masking phase or Kerphase implementations:

- Angel and Lloyd-Hart (AMOS figure caption, 2005)
- Cheetham et al. (Optics Express, 2014): Masking only.
- Martinache et al. (PASP, 2013; ApJ, 2016): asymmetric full-pupil mask + SCExAO
- Pope et al. (SPIE and MNRAS, 2014): asymmetric full-pupil mask + SWIFT/
- Greenbaum et al. (submitted): full-pupil +masking.

[my 2002 honours thesis and Monnier et al.
2004,2008,2009: masking only]

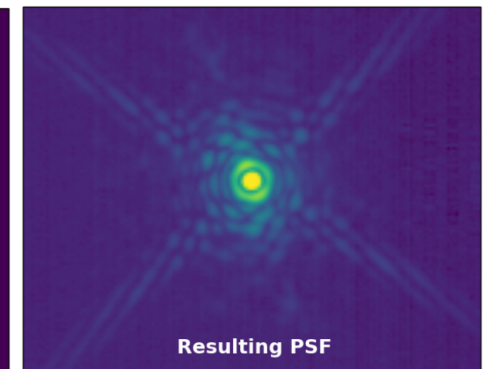
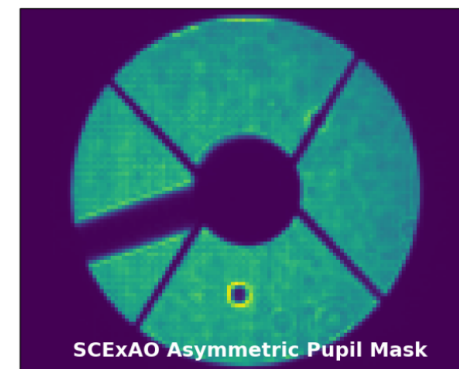
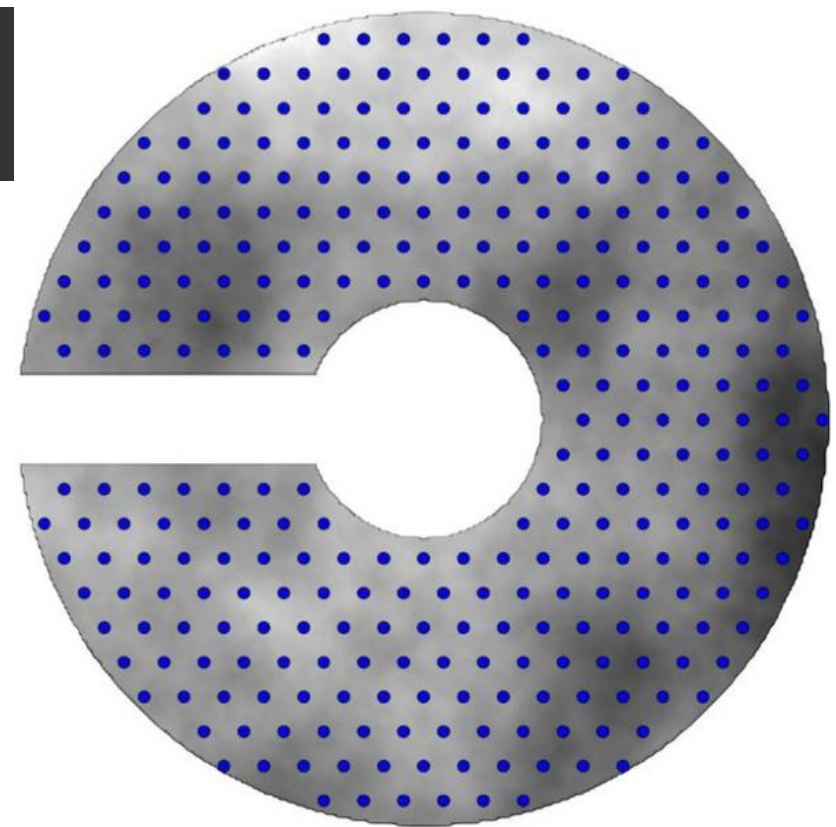
Angel/Lloyd Hart et al (2005) concept



- Original GMT NGS piston phasing concept.
- Pupil split 3 ways, with strong signals in MTF phase.
- Given up on (I think) because in practice it needed >3 movable infrared WFS.

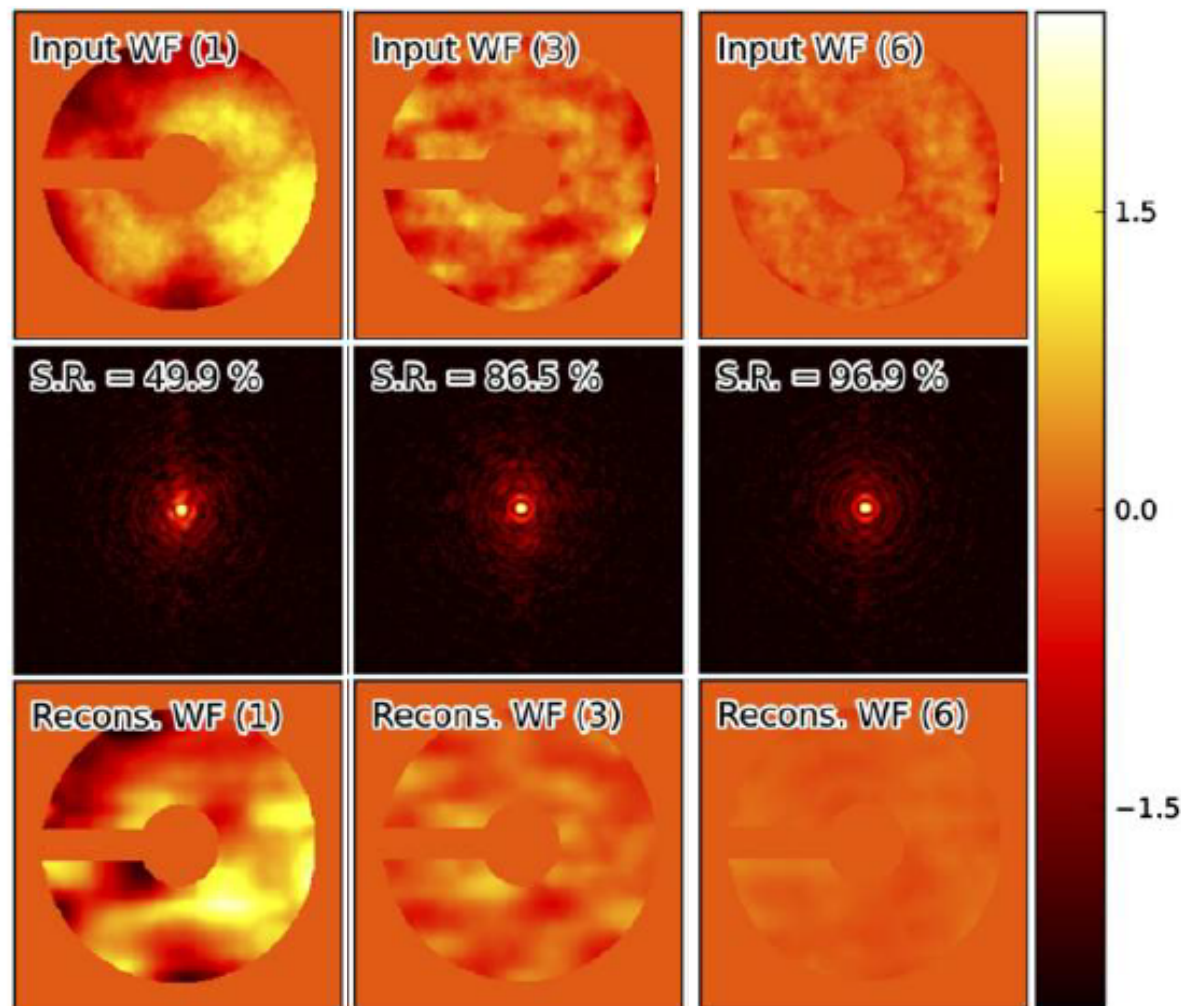
The Asymmetric Pupil

- The Fourier plane (FT of the image) is the autocorrelation of the pupil
 - Not sensitive to all symmetries! A symmetric pupil can sense only even modes
- A Fourier wavefront sensor needs to have pupil asymmetry to sense asymmetric modes
 - This could be achieved with thick spider(s), e.g. right.
 - Alternatively, could mask out subapertures



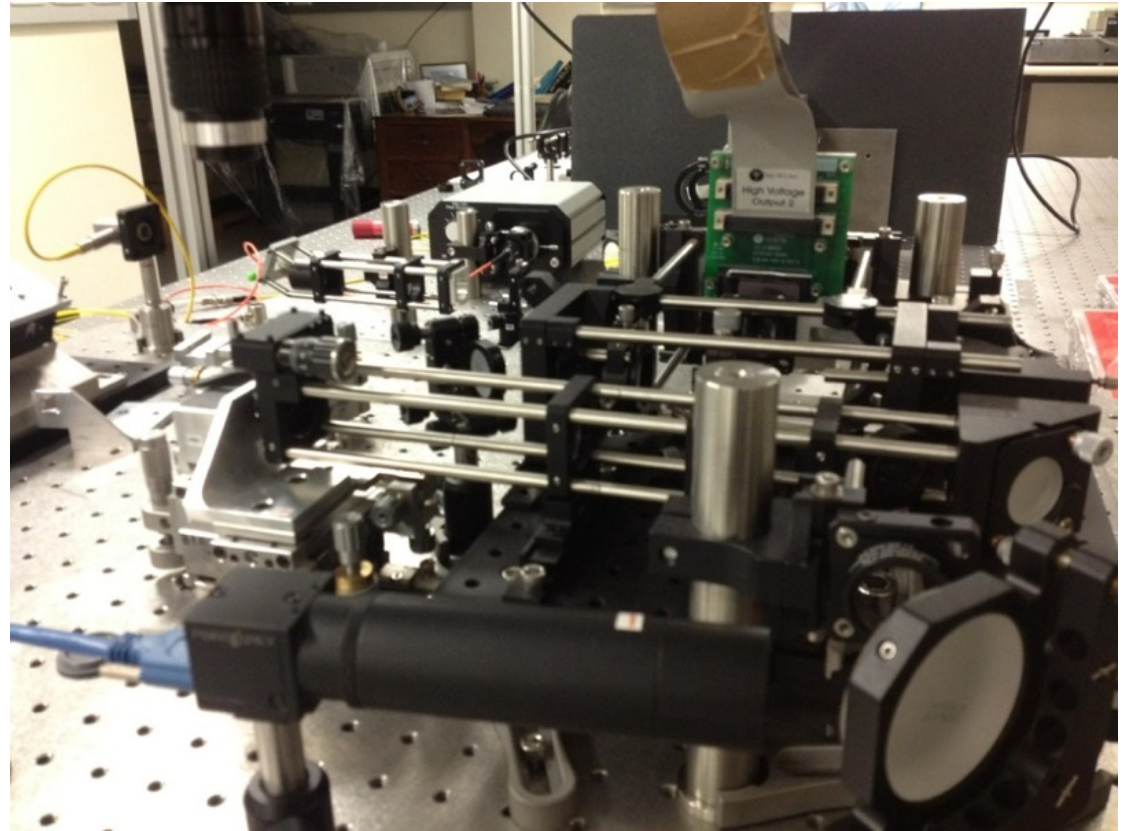
Martinache (2013, 2016) and
Pope (2014)

- Uses row phases (complement of kernel space, sometimes called eigenphases)
- Wavefront sensor is your science camera!
- Initial Strehl $> 35\%$ required – can iterate to as high as 97% in simulations
- Sensitivity near-optimal for a given flux and wavefront error



Martinache (2013) and
Pope (2014)

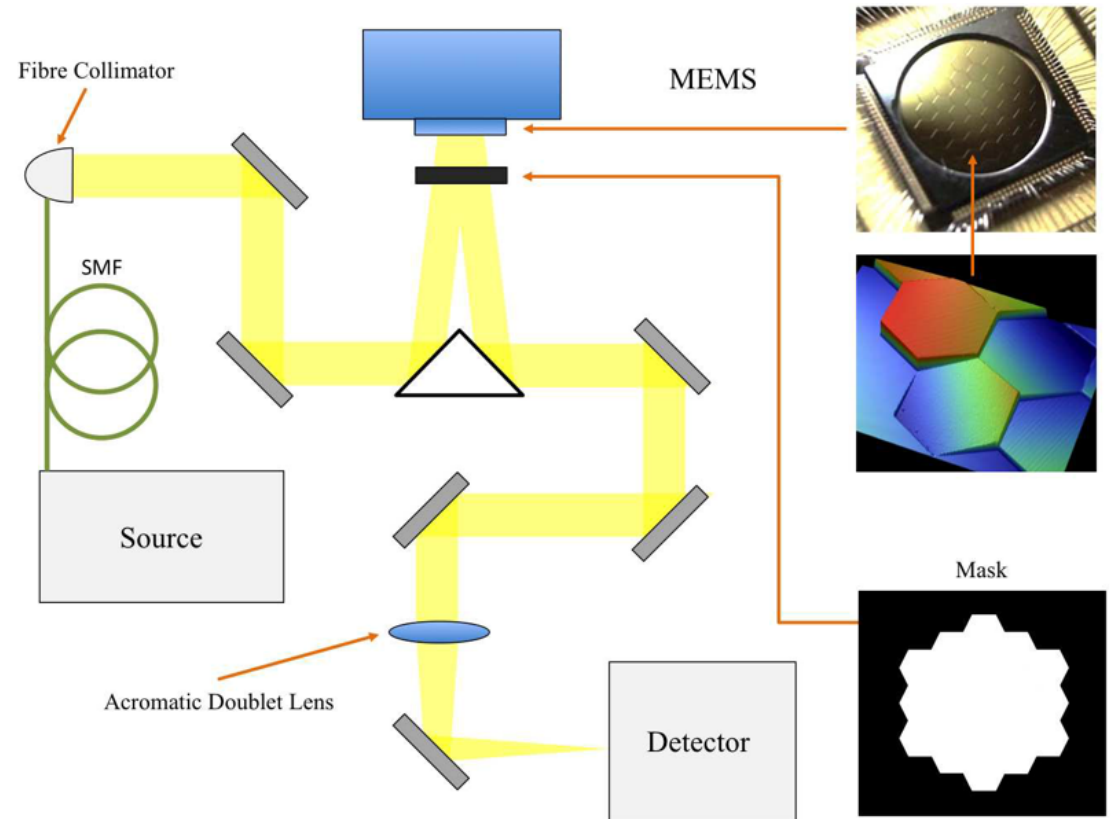
- The microelectromechanical (MEMS) segmented mirror from Dragonfly was used as a JWST analogue
- This has piston, tip and tilt on each segment with $\sim$ few nm precision
- Phasing JWST is hard – no apparatus in space!
- Ideal test case for the new wavefront sensor



Pope (2014)

Experimental Setup II

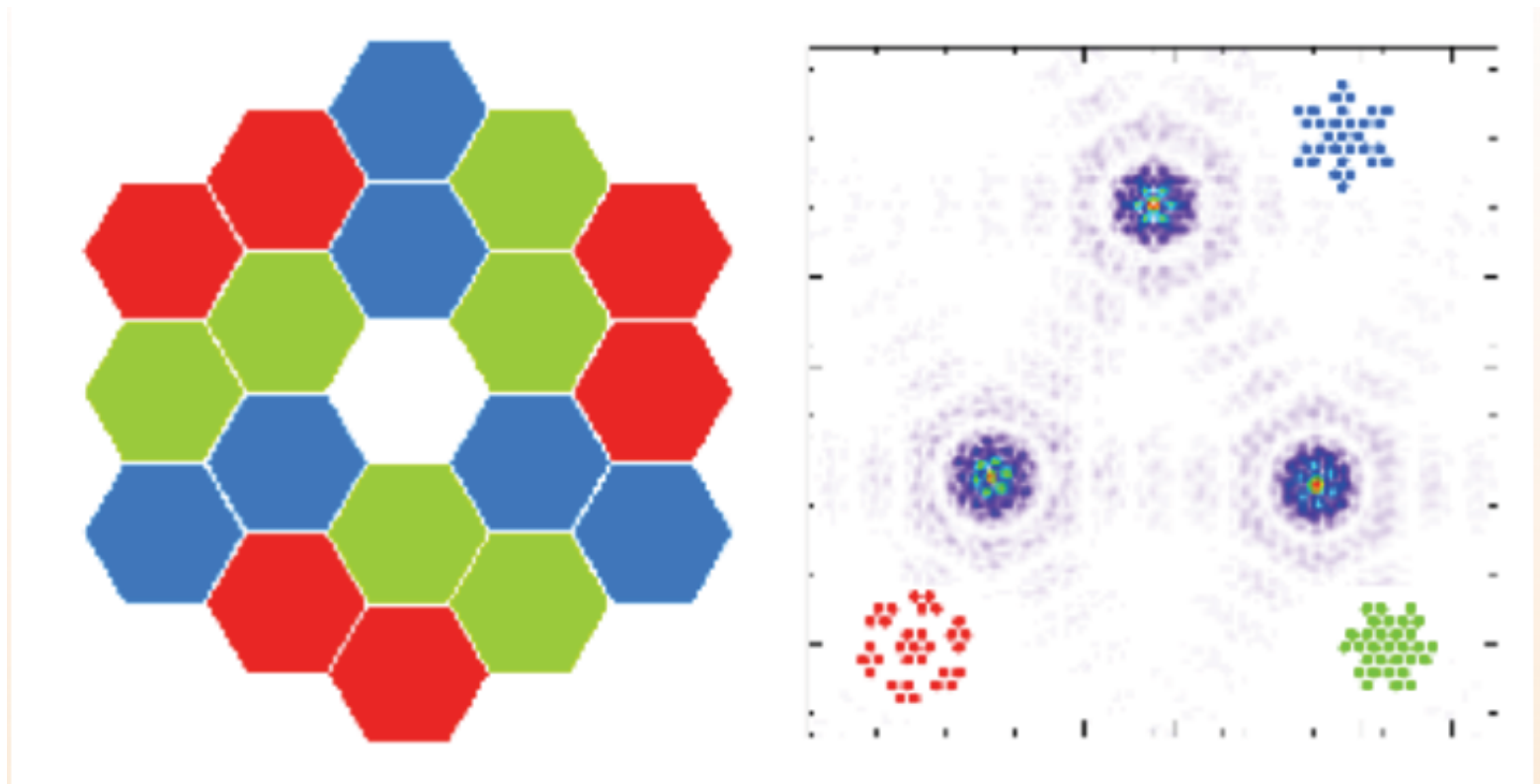
- Laser introduced from single mode fibre
- Passed to MEMS array and through mask
- Imaged onto Xenics IR camera



Pope (2014)

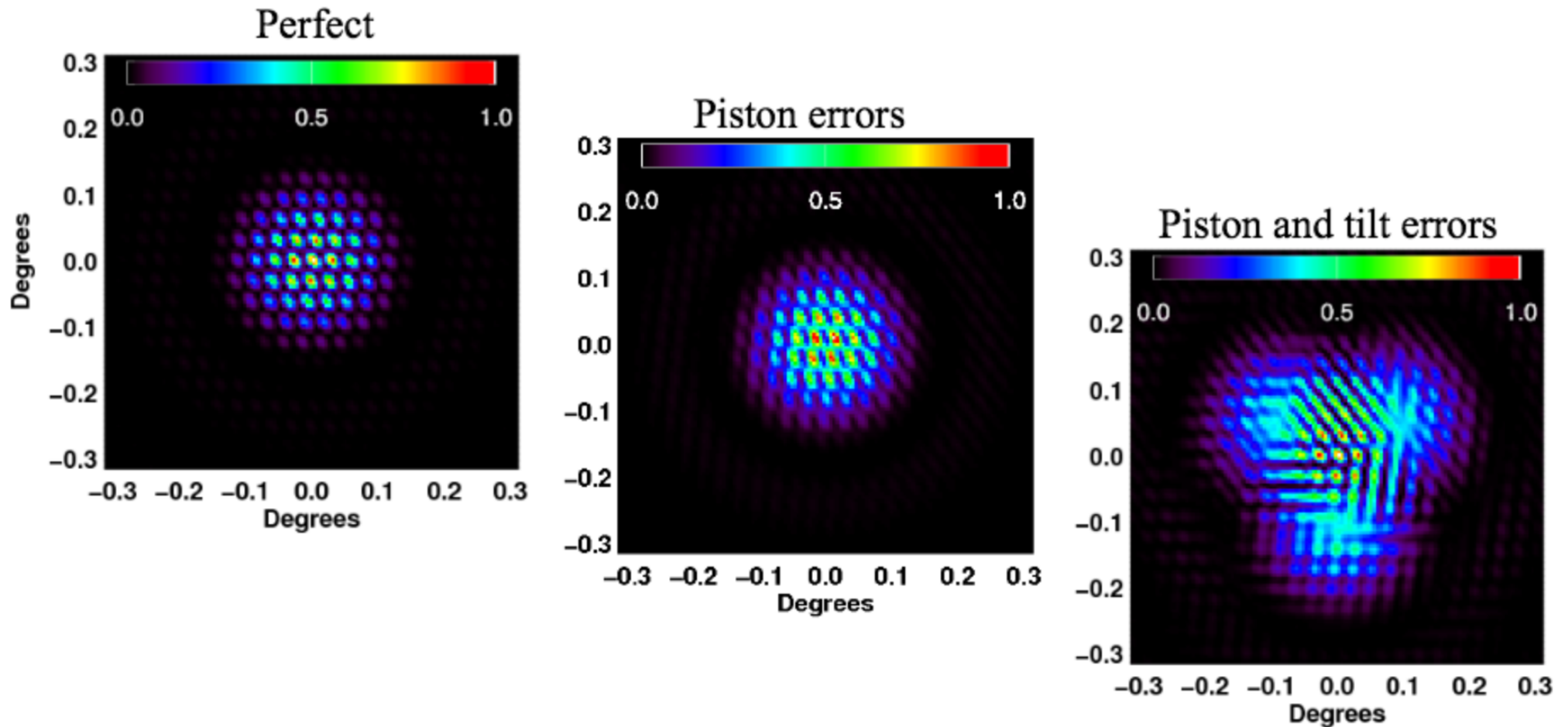
First Step - FICSM

- The first step in phasing a segmented mirror like this is the FICSM approach – ‘Fizeau interferometric cophasing of segmented mirrors’ (Cheetham et al.)



Pope (2014),
Cheetham (2014)

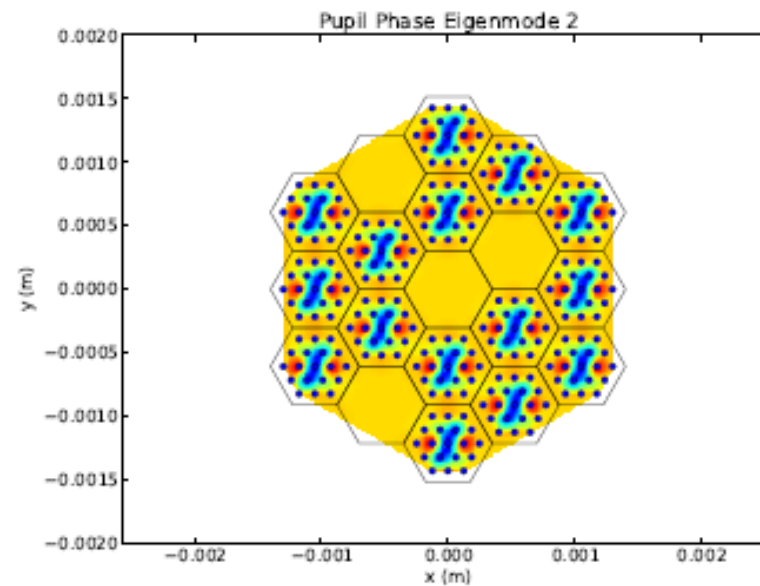
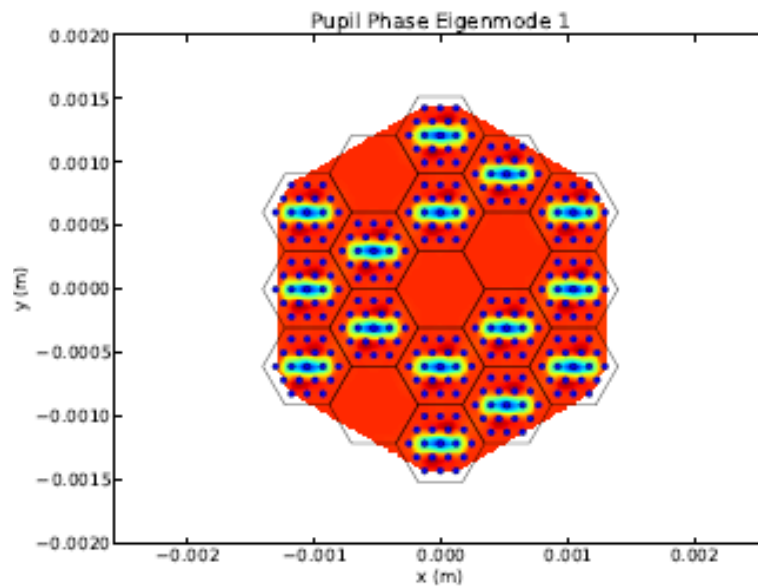
FICSM – Monochromatic data



Pope (2014),
Cheetham (2014)

Pupil Modes

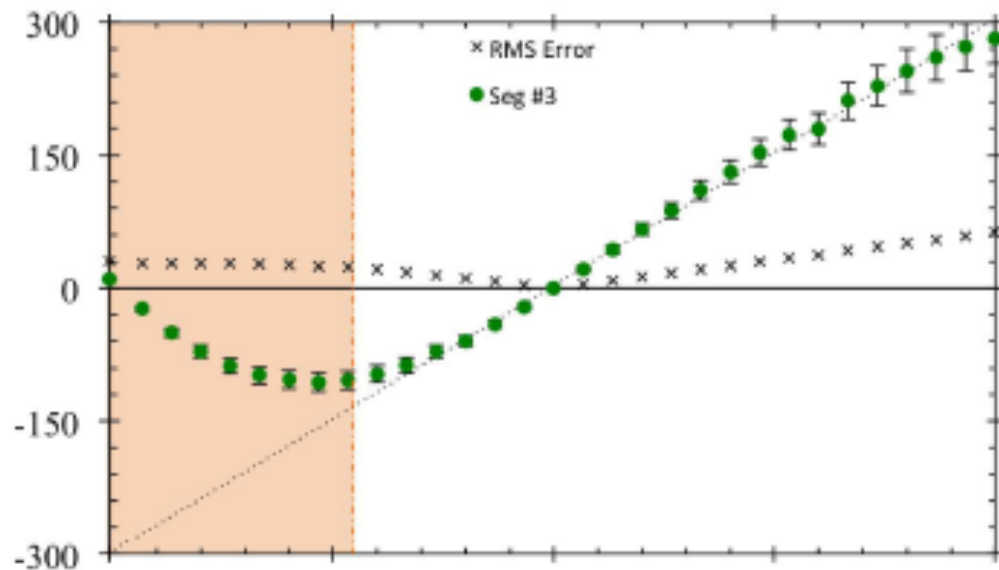
- Below: examples of normal modes of the discrete pupil model used in our experiment
- These play the role of the Zernike basis for expanding optical aberrations on a circular pupil



Pope (2014),
Cheetham (2014)

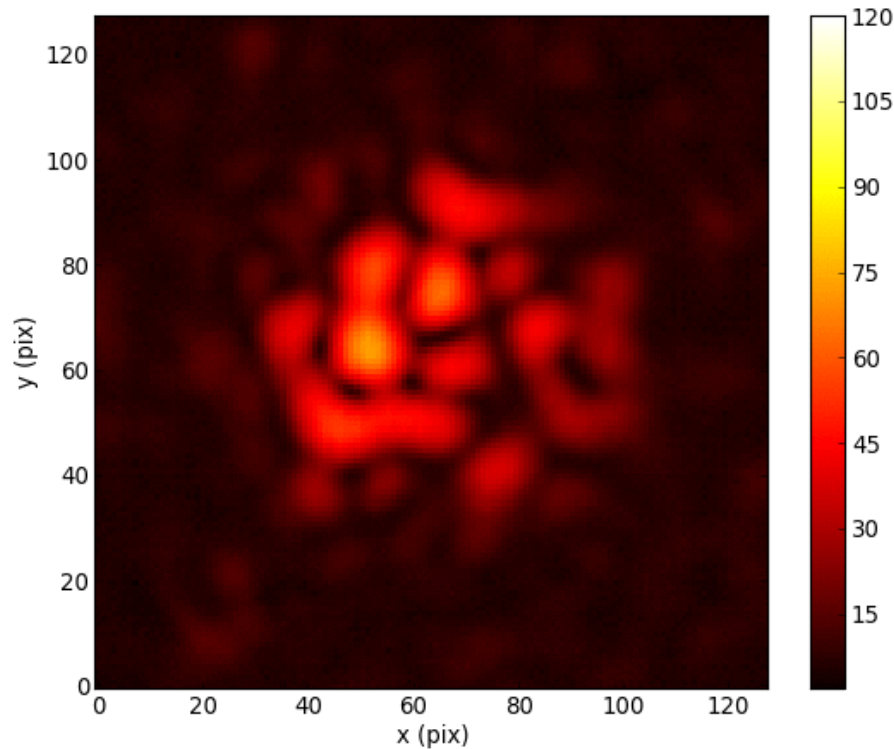
How well can we Measure a Single Segment?

- › Pistoned a single segment (3) in 20 nm steps from -300 to +300
- › Reconstruction is very accurate... within limits
- › You lose it when linearity fails
- › Phases are also correlated – sensing modes globally is a bad way to reconstruct phases on a single segment
- › When phasing the whole mirror in closed loop, this correlated error beats down to zero as you make the whole thing flat

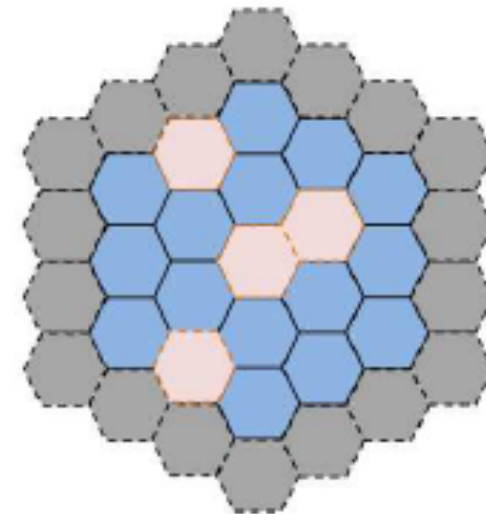


Pope (2014),
Cheetham (2014)

Restoring a PSF

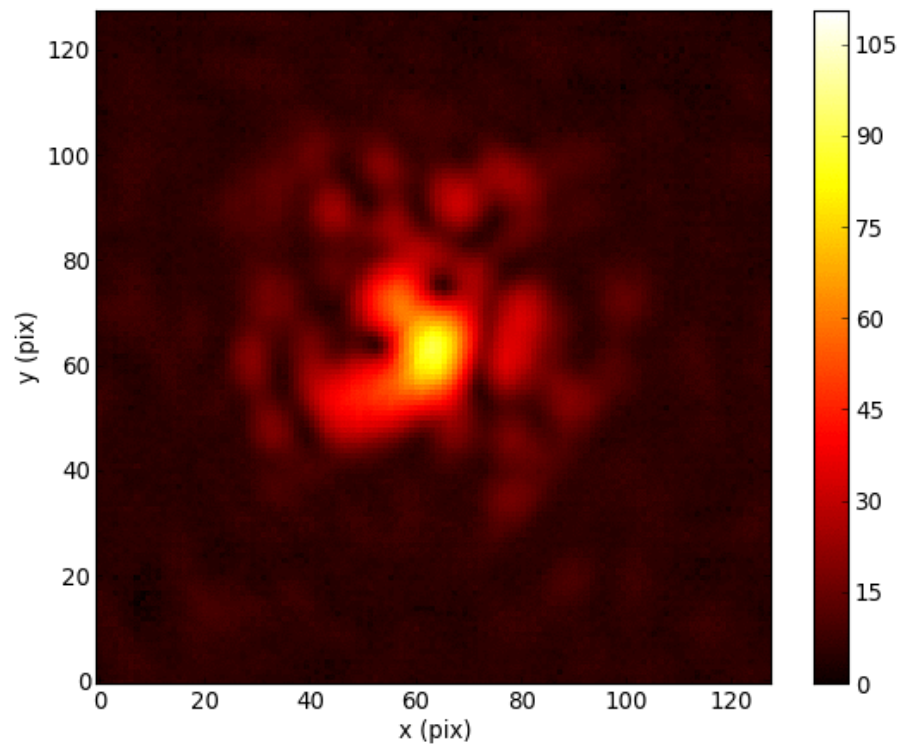


- Left: animation of a stretched PSF as our algorithm converges
- This is with a scalene triangle of segments removed

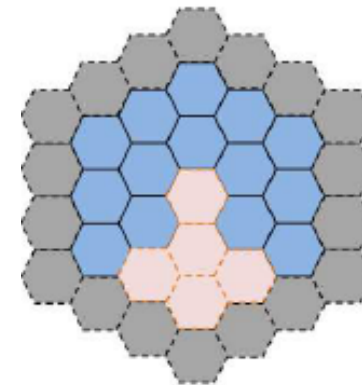


Pope (2014),
Cheetham (2014)

Restoring a PSF

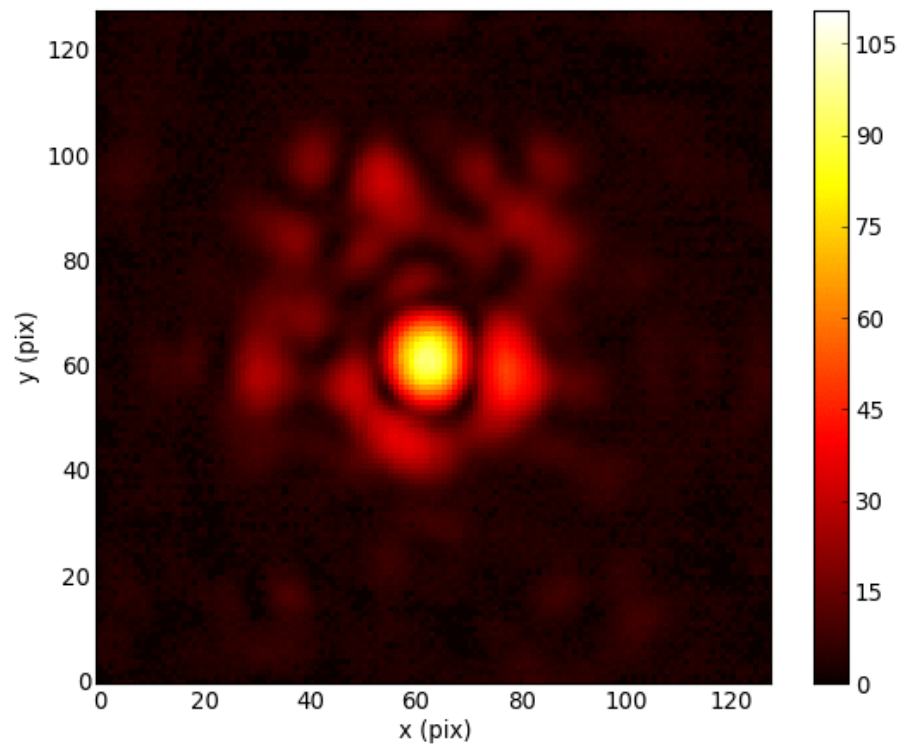


- Also works with a wedge removed

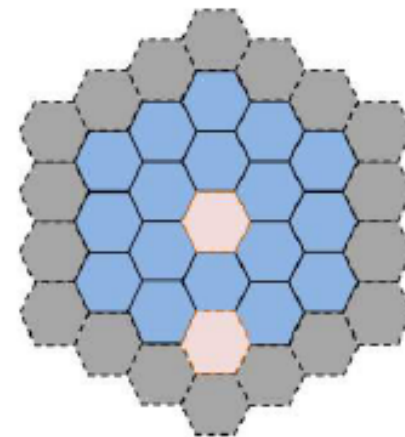


Pope (2014),
Cheetham (2014)

Restoring a PSF



- Or in fact a single segment!



Pope (2014),
Cheetham (2014)

Oxford-SWIFT at Palomar

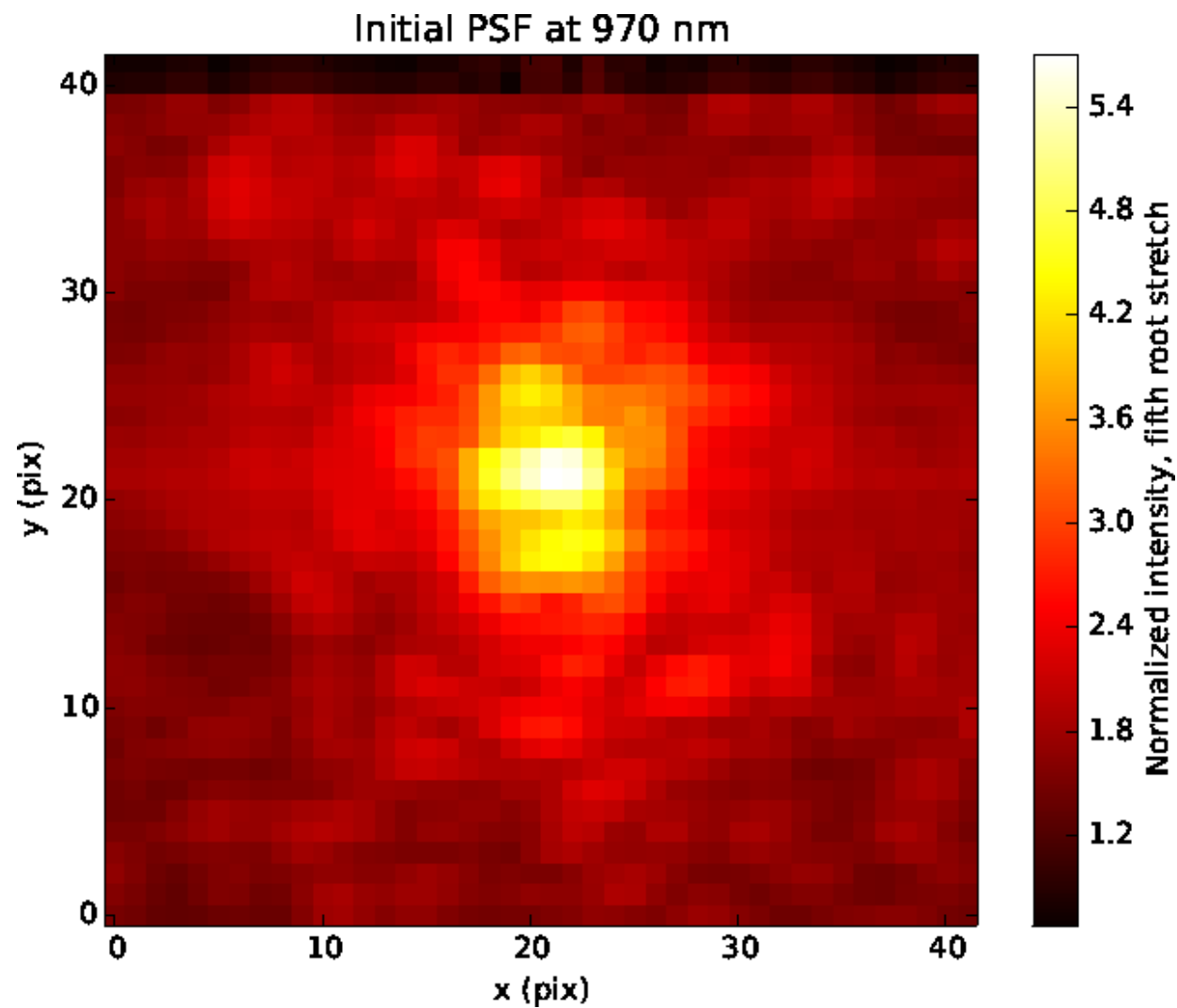
- Hale 200-inch telescope has the PALM-3000 extreme AO system – the highest order AO currently available for experiments
- Oxford has the Short Wavelength Integral Field specTrograph (SWIFT) on P3K – a high spatial and spectral resolution IFU from 650-1000 nm
- SWIFT has historically had problems with non common path error – never achieves even internal diffraction limit
 - Hard to correct with conventional methods, because of the optical layout
- Ideal test case for our wavefront sensing method

HODM Mask

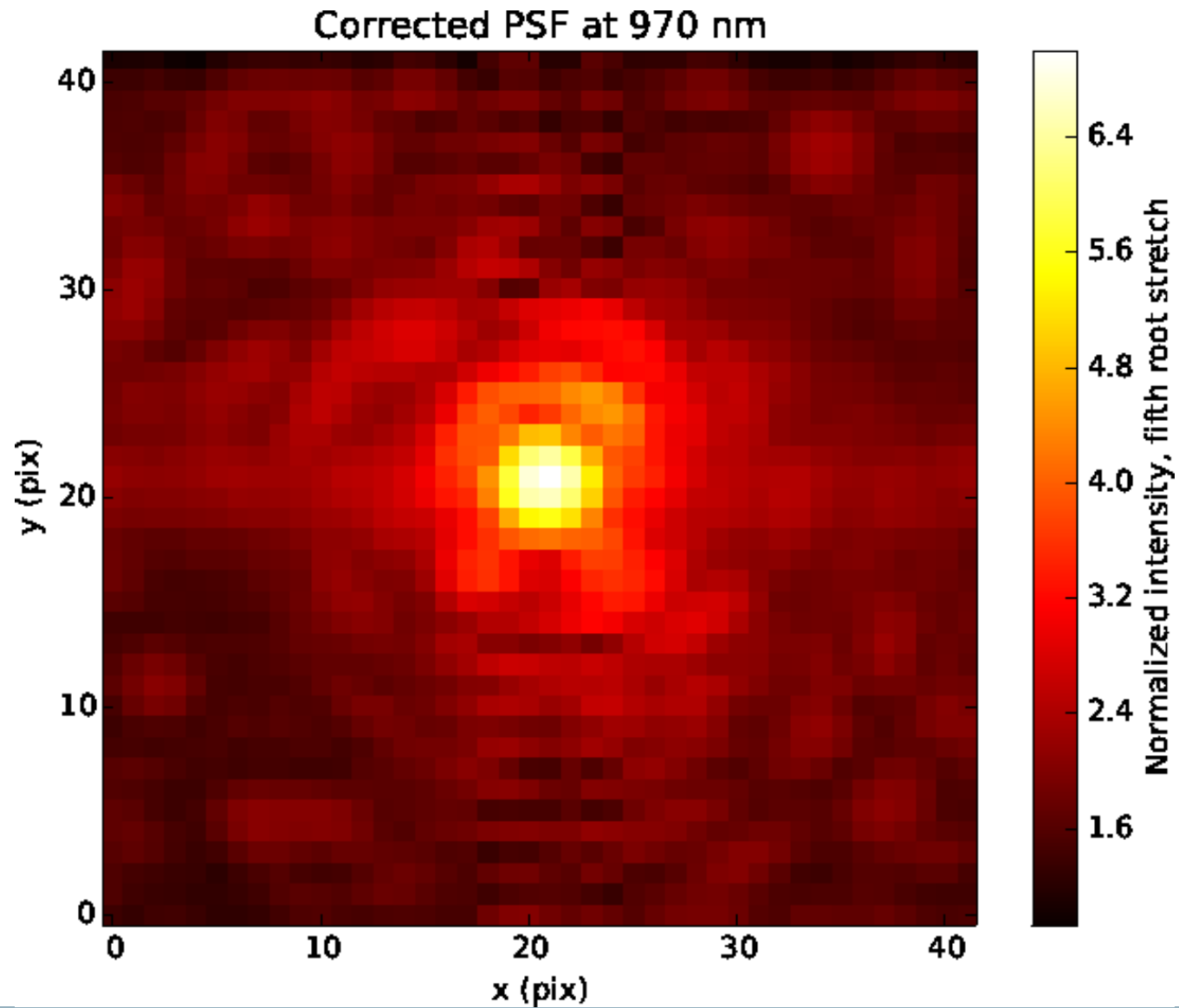
- Right: the mask we placed over the high order DM to get the pupil asymmetry
- This was probably overkill, but we wanted to make sure it worked the first time!



Before Phasing



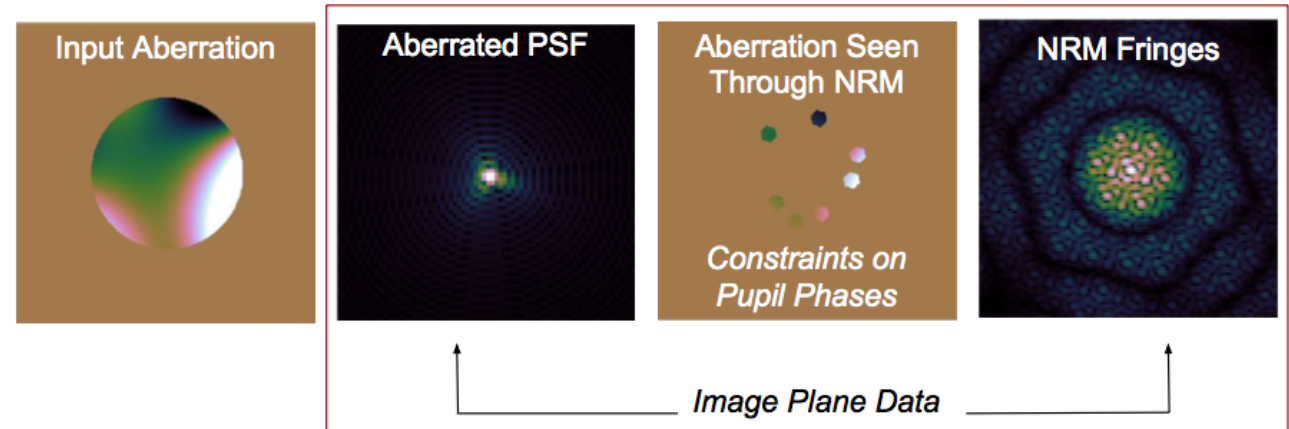
After Phasing



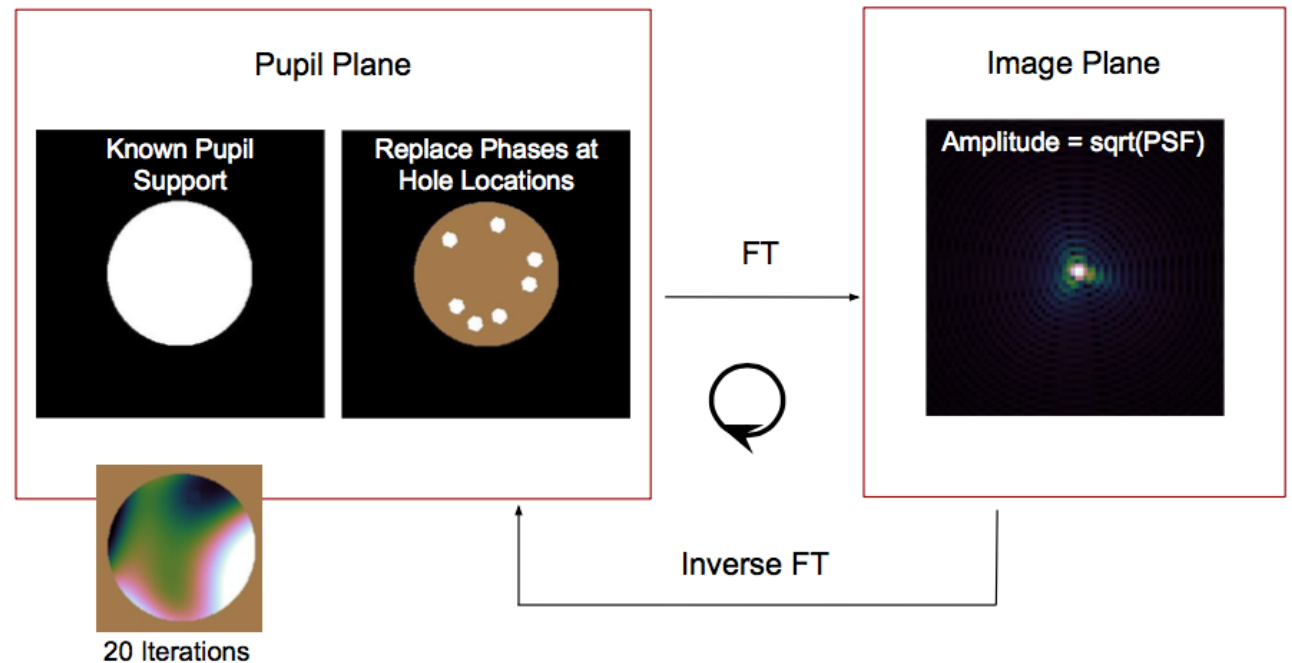
Masking Plus Full-Pupil

- Assume static aberration, or dual wavebands?
- Masking and the Gerchberg–Saxton algorithm can be combined (Greenbaum et al, submitted)

Preconditioning Pupil Phase Using NRM-Derived Constraints

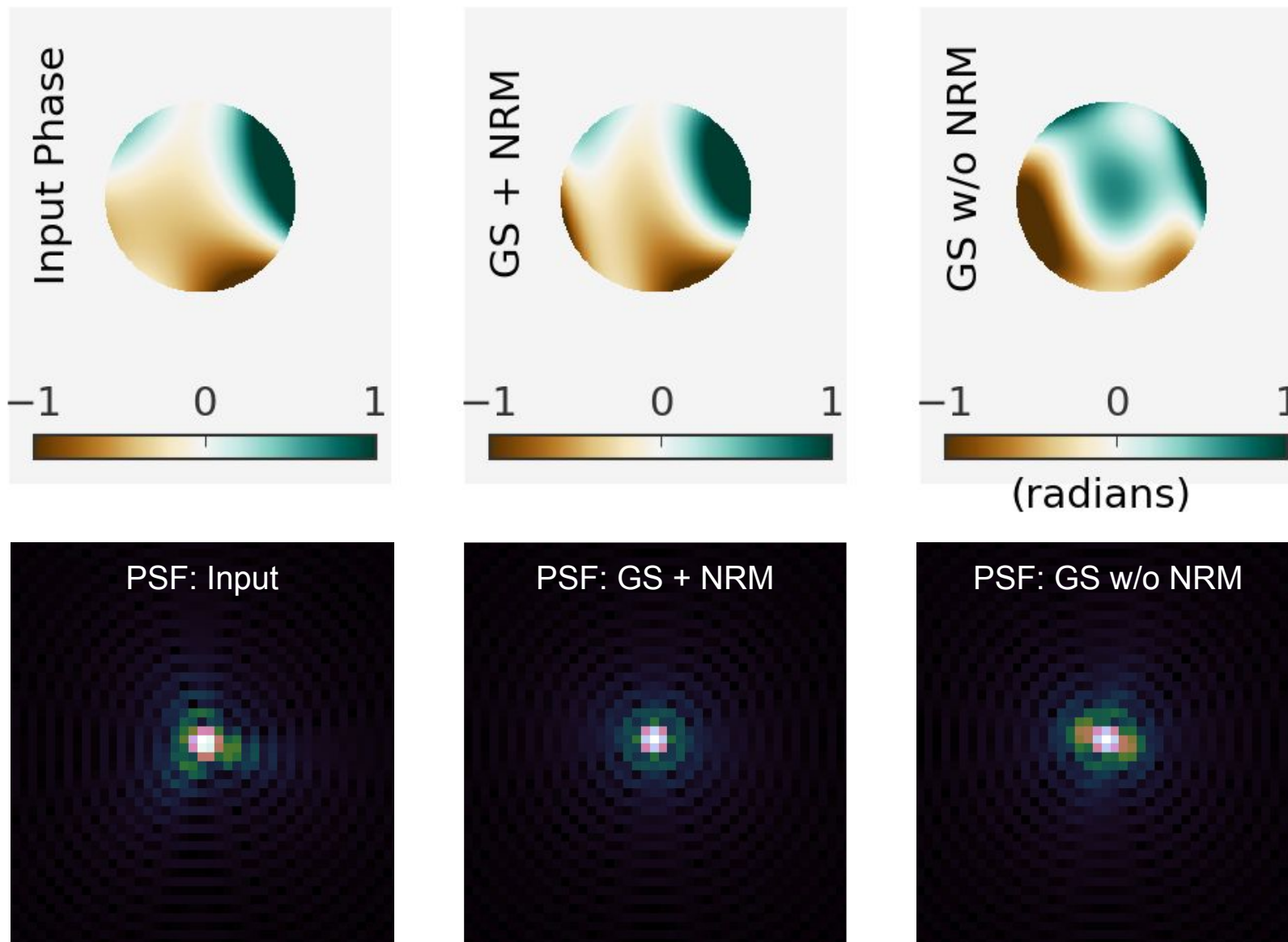


Start: Fix pupil geometry,
impose NRM phase constraints





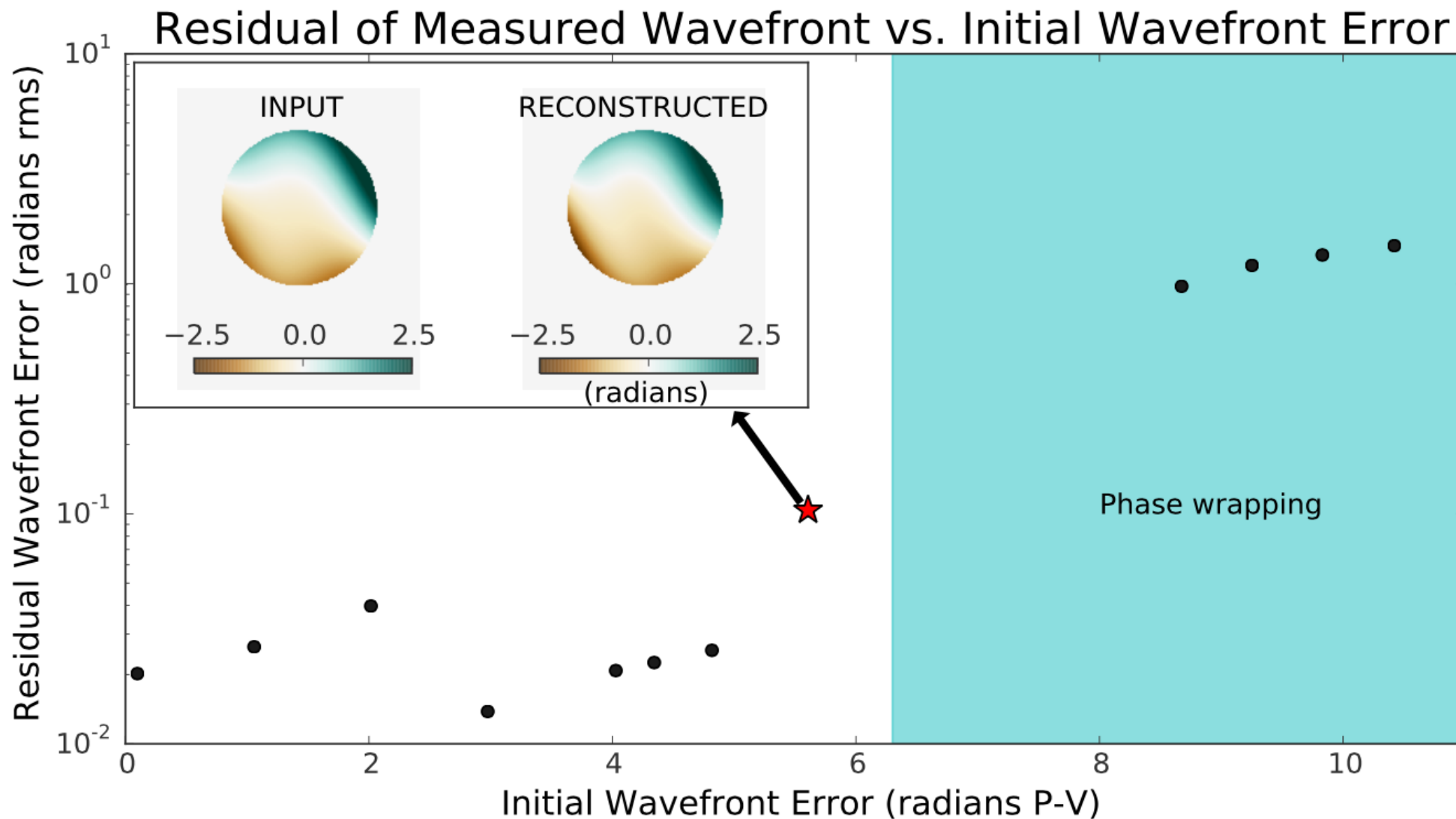
Great Results for Small Aberrations



Greenbaum et al (2016)



Great results for moderate aberrations



Greenbaum et al (2016)

- For K-band moderate-contrast imaging: Strehl above 50% for median seeing LGS with an on-axis reference with H=9. Piston, tilt, focus < 0.3 radians RMS $< 100\text{nm}$. $0.5 \times 1''$ field of view (i.e. IFS) OK.
 - For H-band high-contrast imaging: same but piston, tilt, focus $< 70\text{nm}$ RMS, and a K=8 reference star.
 - For Paschen-Beta observations, piston, tilt, focus < 0.5 radians RMS at 1282nm wavelength, i.e. RMS $< 100\text{nm}$.
- Better performance than this significantly increases contrast – it is the quasi-static terms that are most important in practice.*

GMTIFS Imager WFS Options

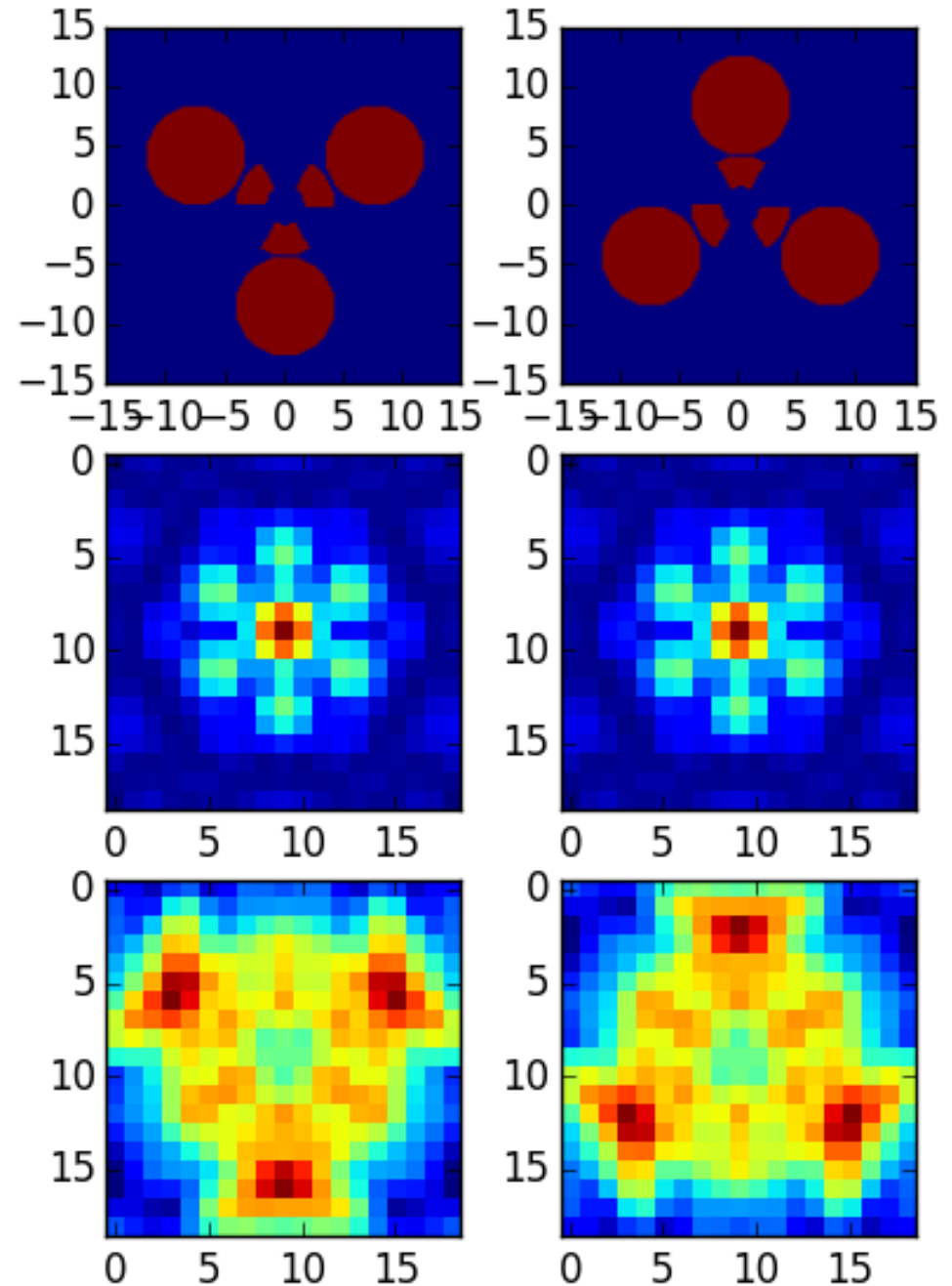
- GMTIFS is primarily an LGS instrument, with poor low order mode correction from LTAO.
- Image-plane wavefront sensing enables simultaneous science, and requires relatively simple optics only. As a baseline, the pupil could be split in two, ± 2 radians of phase defocus could be applied to the pupil.
- This wavefront sensor is highly non-linear when outside 1 radian of aberration, so would at least need an acquisition mode that can handle large piston offsets.
- The fixed 5 milli-arcsec pixel scale of the imager means that in order to sample the full core of an 8m PSF, 16×16 pixels are needed in H-band. Simply achieving 50% encircled energy at high piston values only requires 8×8 pixels.
- Assuming a 30% efficiency (atmosphere $\rightarrow$ detection) and a 50% 8m Strehl, back of the envelope calculations gives operation at mean photon counts = 2 x readout noise for the Hawaii detector at:

Band	Speed	Magnitude Limit
H	250Hz	13.2
H	125Hz	14.0
K	250Hz	12.3
K	125Hz	13.1

Ireland in prep.

Principle

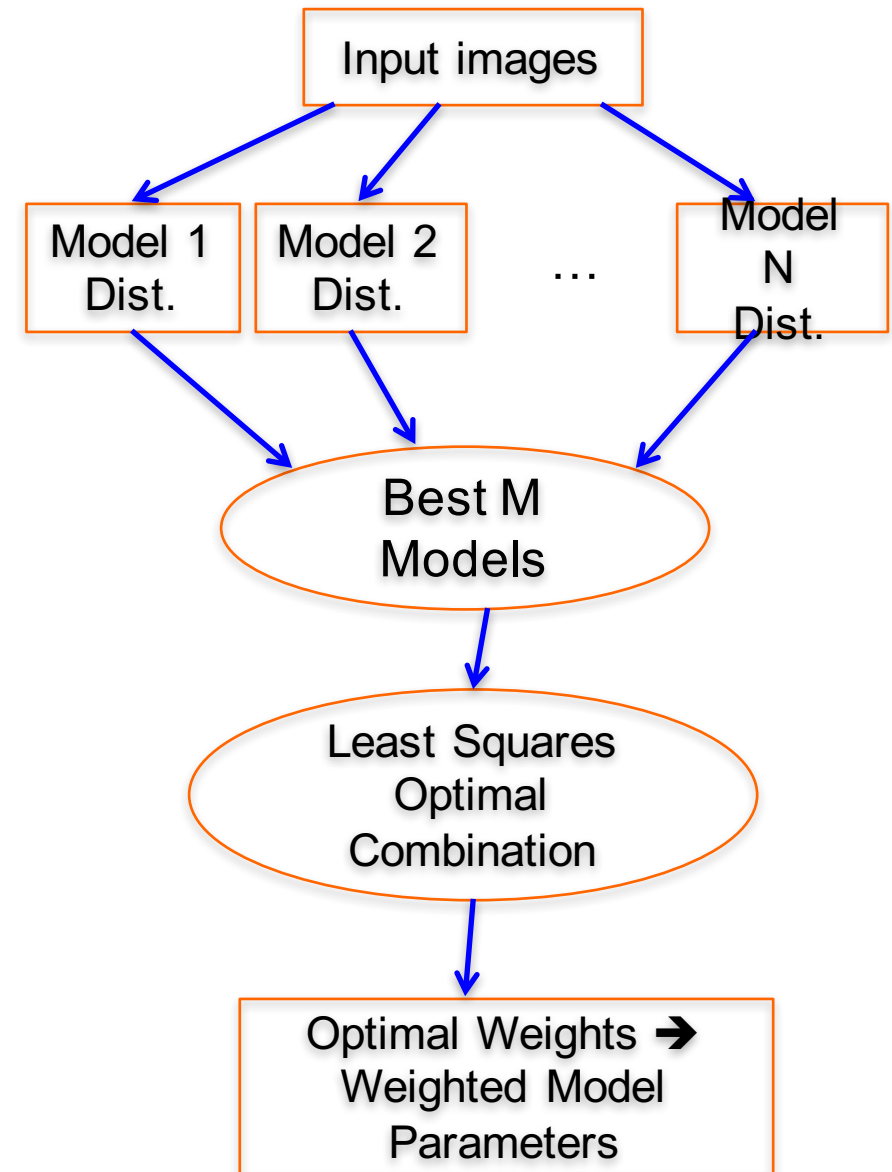
- Focal-plane wavefront sensors are in general *ambiguous*. E.g. a positive and negative focus image looks identical for a point-symmetric pupil
- An alternative is to split the pupil in 2 or more parts.
- One way to do this is an asymmetric pupil wavefront sensor (e.g. right, Martinache). Super-easy to manufacture, but not ideal in terms of sensitivity or requiring a particular pupil rotation.
- Another (slightly better) way is to just take images on either side of focus, or a pupil that uses 180 degree phase for the asymmetry...



Ireland in prep.

Non-Linear WFS Algorithm

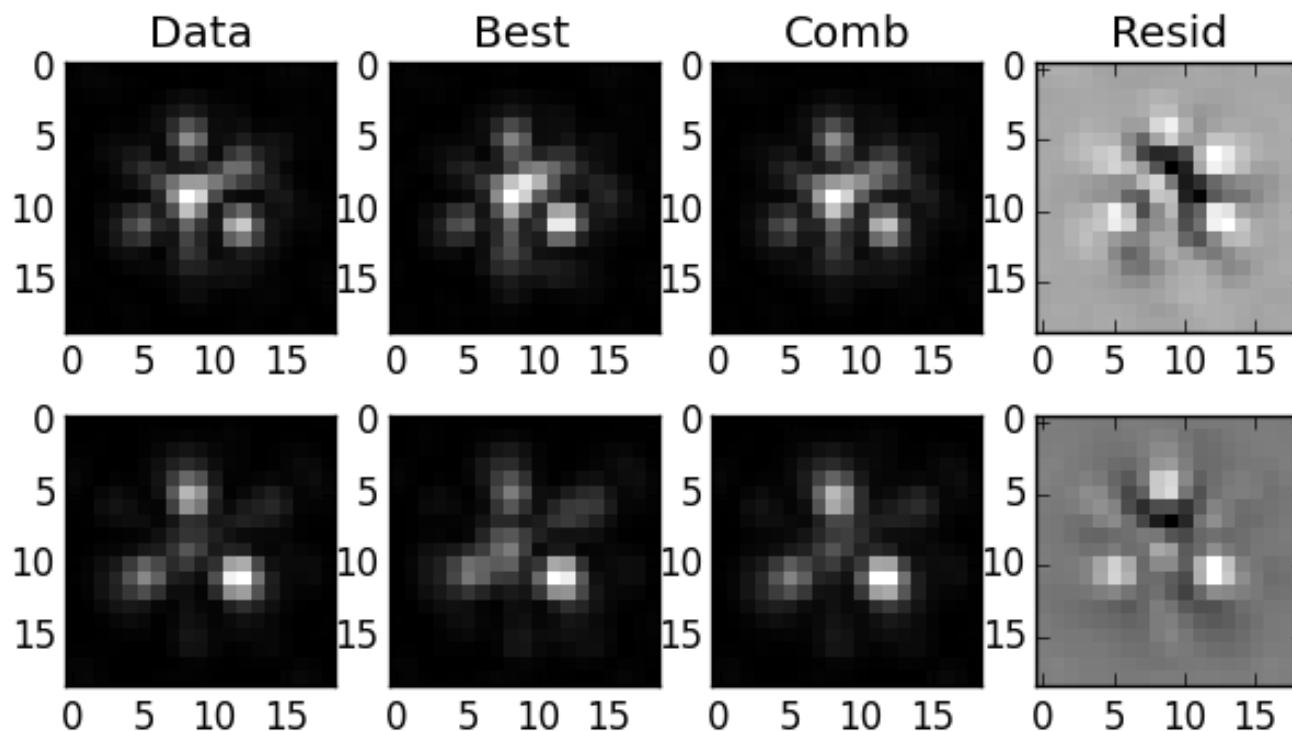
- In the past, focal-plane wavefront sensing has been seen as too difficult because linear algorithms only work at high Strehl.
- This remains true for sensing many modes... but for GMTIFS, if we have an LGS correction, arguably only 9 modes need to be sensed (tip/tilt, focus and 6 piston modes).
- Instead of a linear WFS algorithm, a *locally-linear* algorithm works, and is highly parallelisable....



Ireland in prep.

Simulations

- With a library of 250,000 PSFs on 19x19pixels, a simple python program on a laptop can compute the best-fit wavefront in <1s. Running at 250Hz is a simple CPU+GPU problem.
- RMS with over 1 wave of piston, focus, tilt is 0.16 radians. Smaller (photon-limited – as good as unmodulated pyramid) in the linear regime (after loop is closed).



Example analysis frame...

Input pistons:

-0.57 -2.58 0.12 -1.12 0.85 -1.84

Fitted pistons:

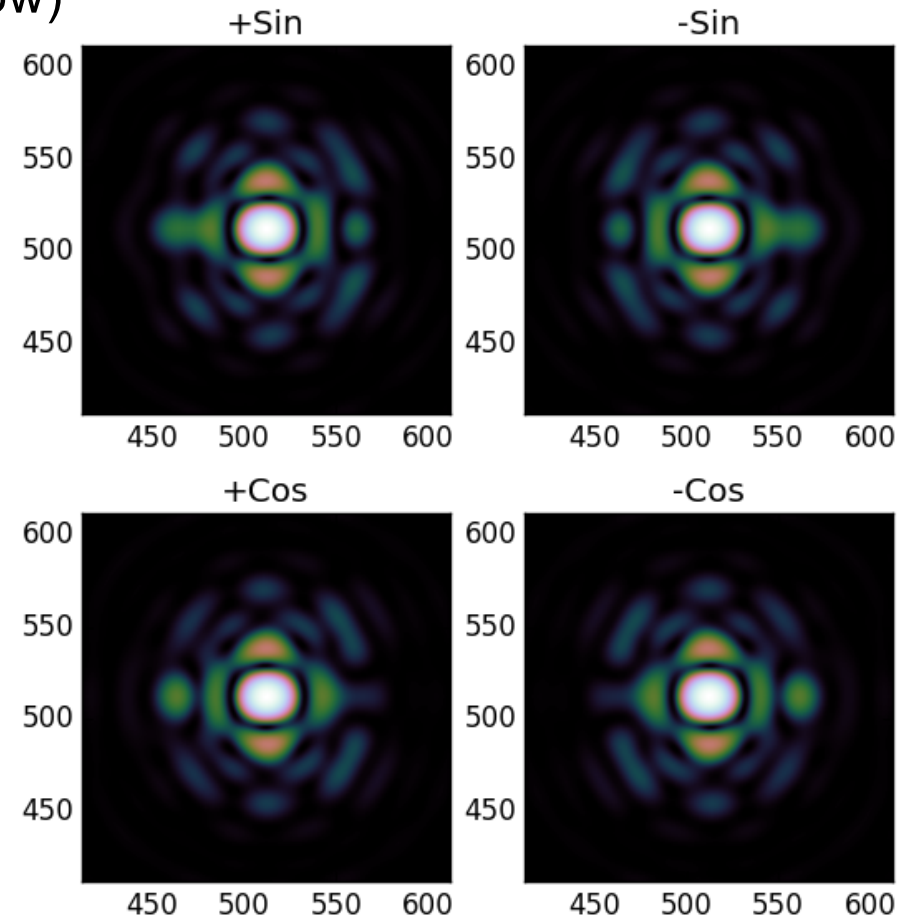
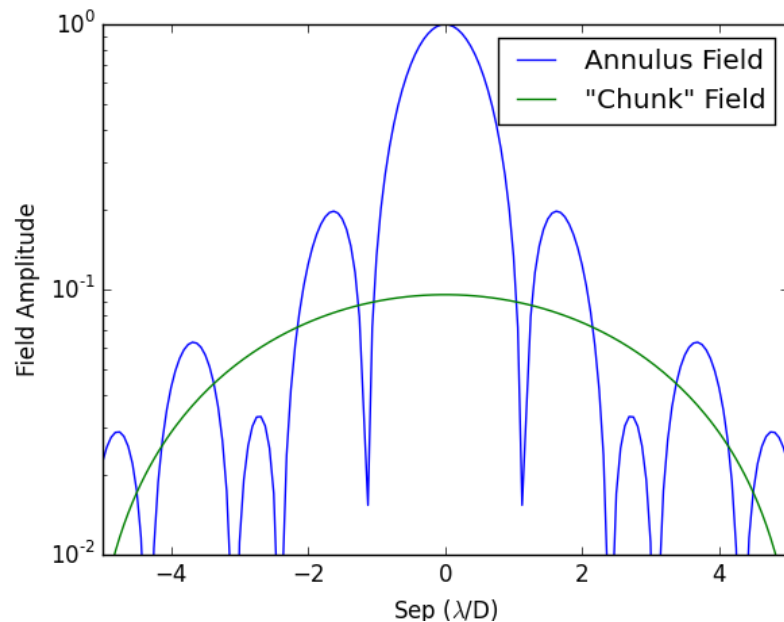
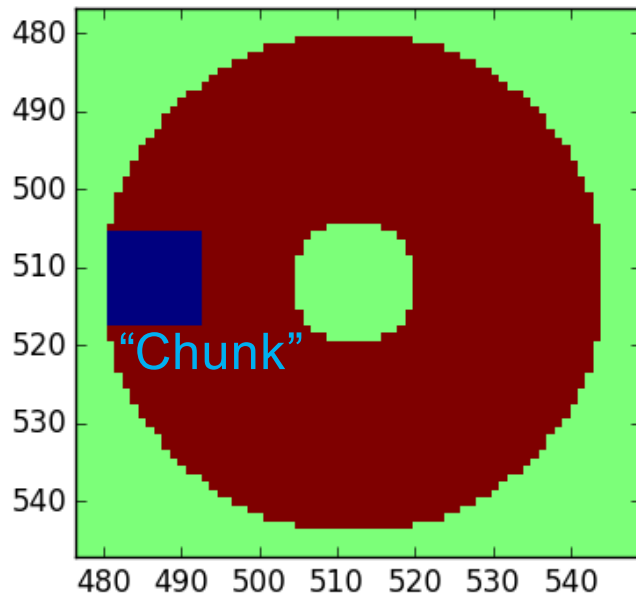
-0.60 -2.71 0.05 -1.07 0.91 -1.75

Additional focus, tilt terms,
plus 1 radian RMS over each
aperture

Ireland in prep.

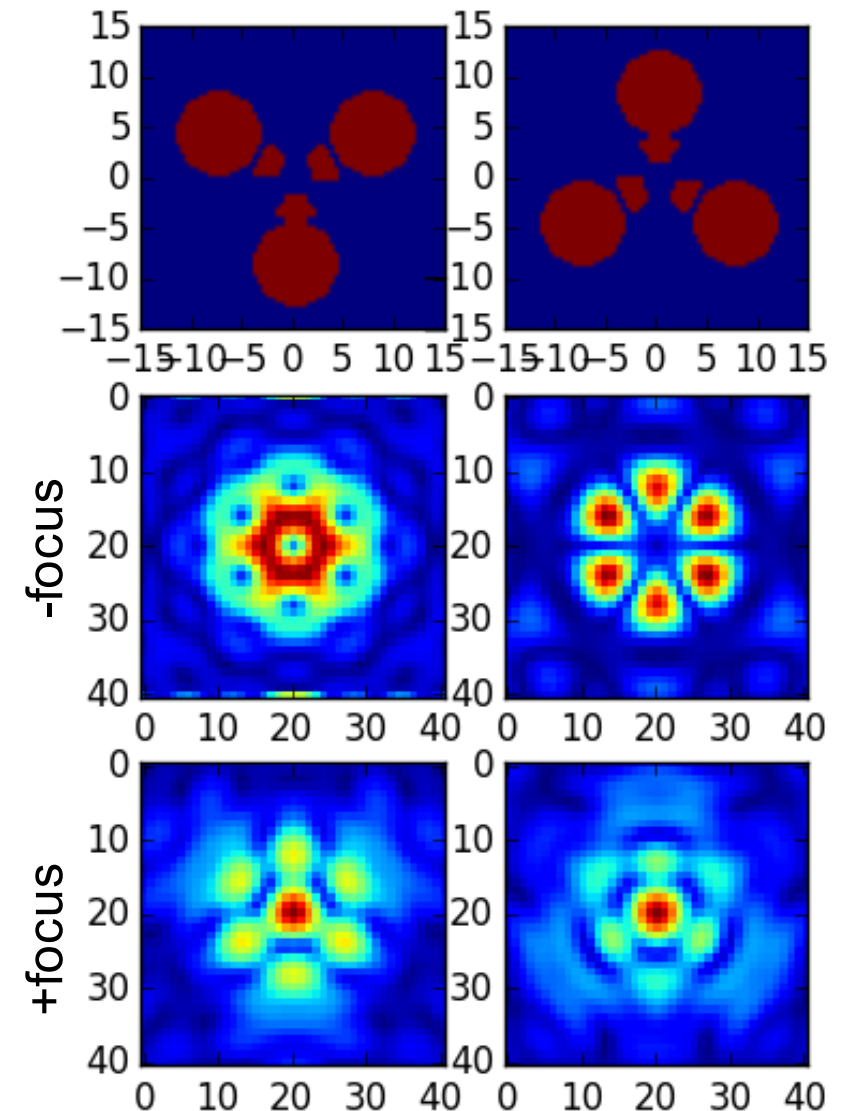
Asymmetric Pupil WFS in the Image Plane

- An asymmetric pupil is the sum of the pupil field and the asymmetric component.
- In the image plane, the asymmetric component breaks the degeneracy between the even aberrations of positive and negative sign ($2 \lambda/D$ below)



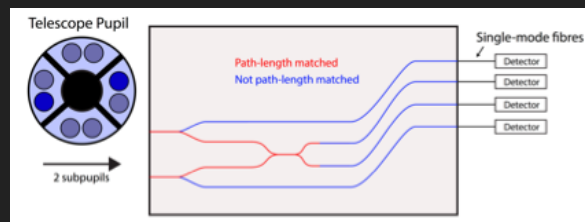
Extension to Coronagraphic Images

- For a leaky coronagraph, the photon-limited sensitivity of any image-plane WFS is the same, so long as aberration speckle amplitudes are smaller than diffraction speckle amplitudes.
- Once this condition isn't met, the WFS is nonlinear.
- Uncertain when this nonlinearity produces ambiguity or sensitivity loss, especially with an IFU.
- With e.g. stellar leakage or tip/tilt errors, asymmetric pupil wavefront sensing fails – but dual-image plane sensing works...

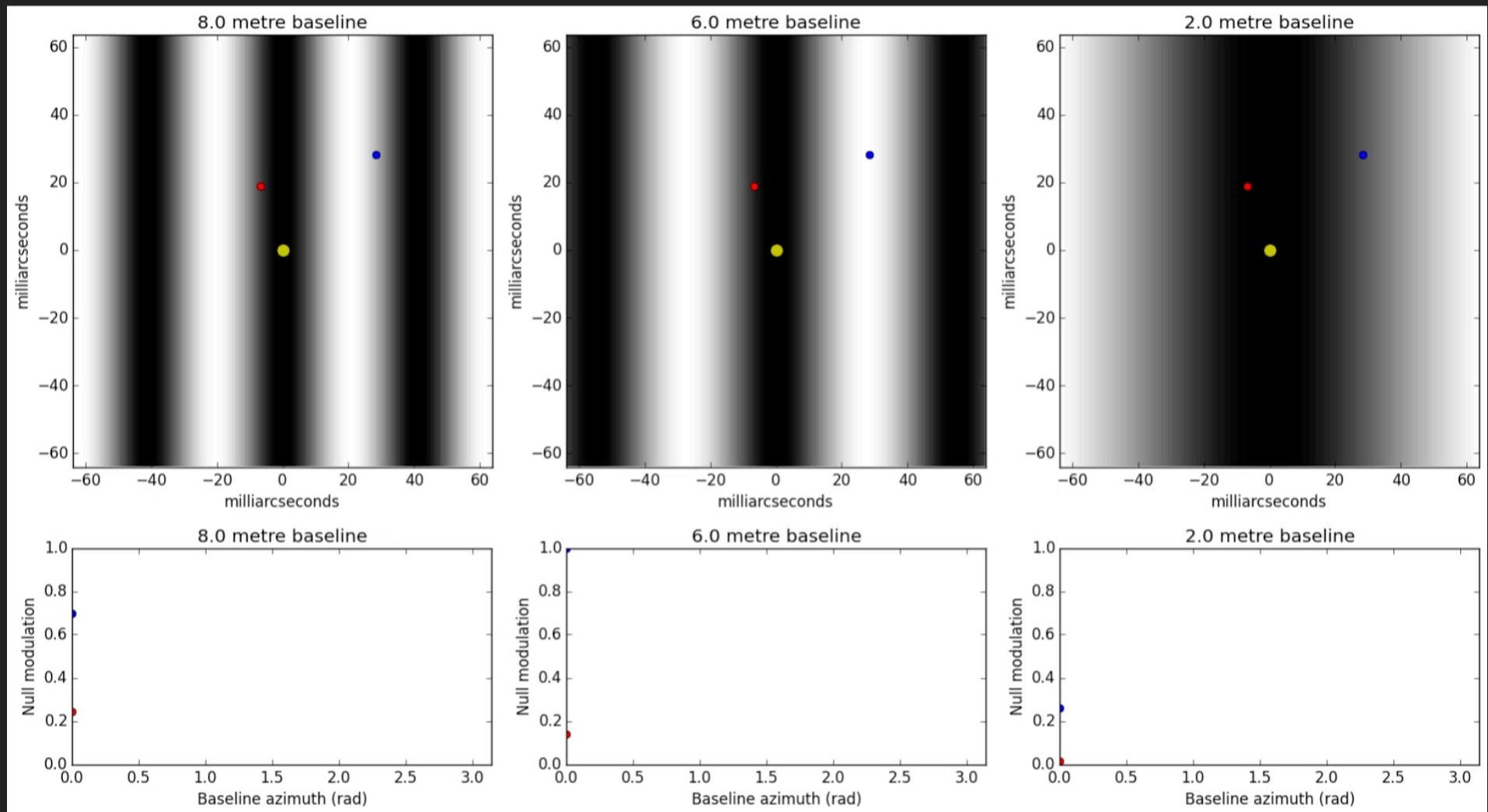


“GLINT”: Guided Light Interferometric Nulling Telescope (Barnaby Norris et al, USyd)

- ▶ Uses a 3D photonic chip (ULI) to destructively interfere starlight, revealing the faint planet nearby
 - ▶ Telescope pupil imaged onto chip
 - ▶ Remapping + interference via evanescent couplers in chip
 - ▶ 10s of outputs, encoding time domain signal as pupil rotates



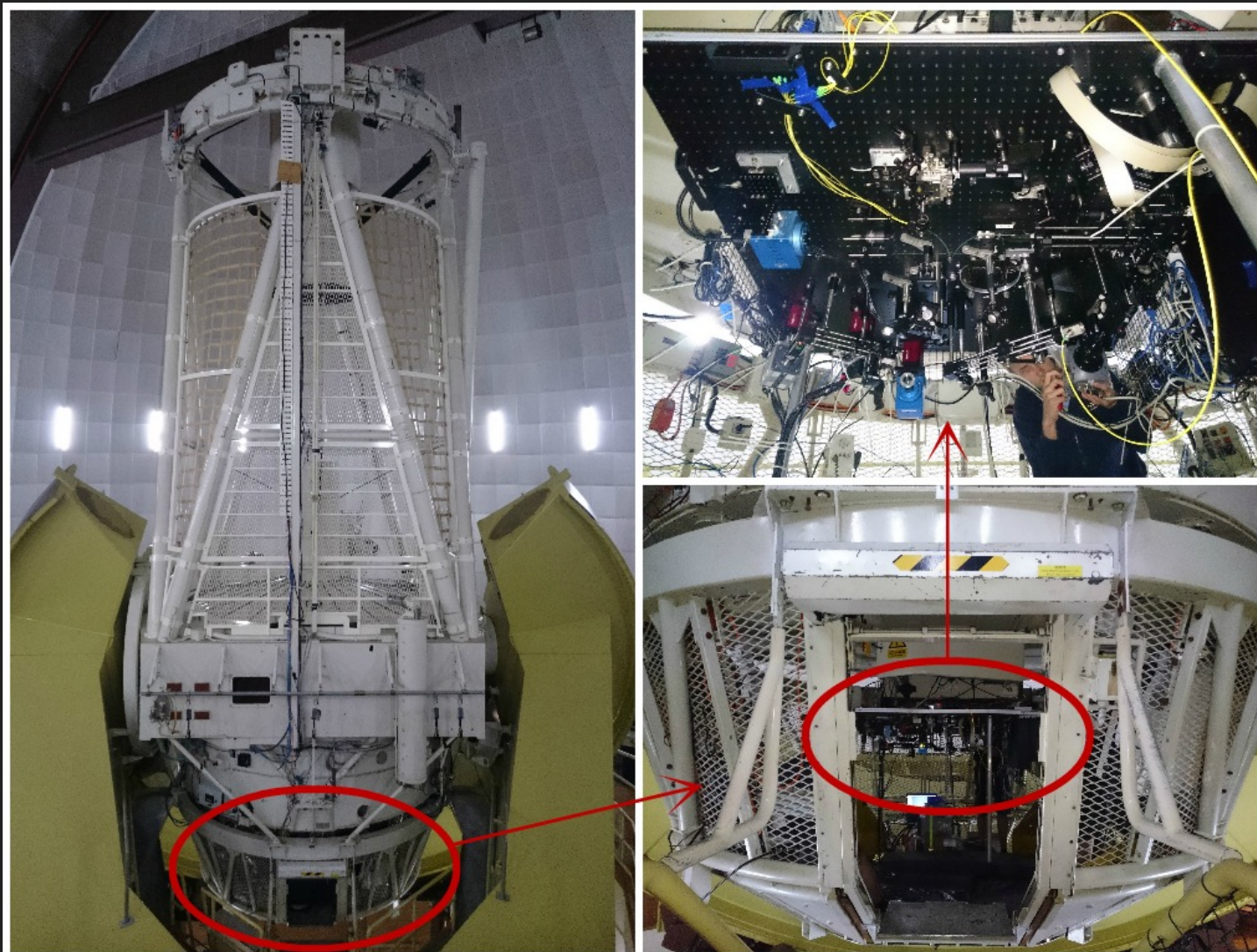
Single baseline nuller Concept



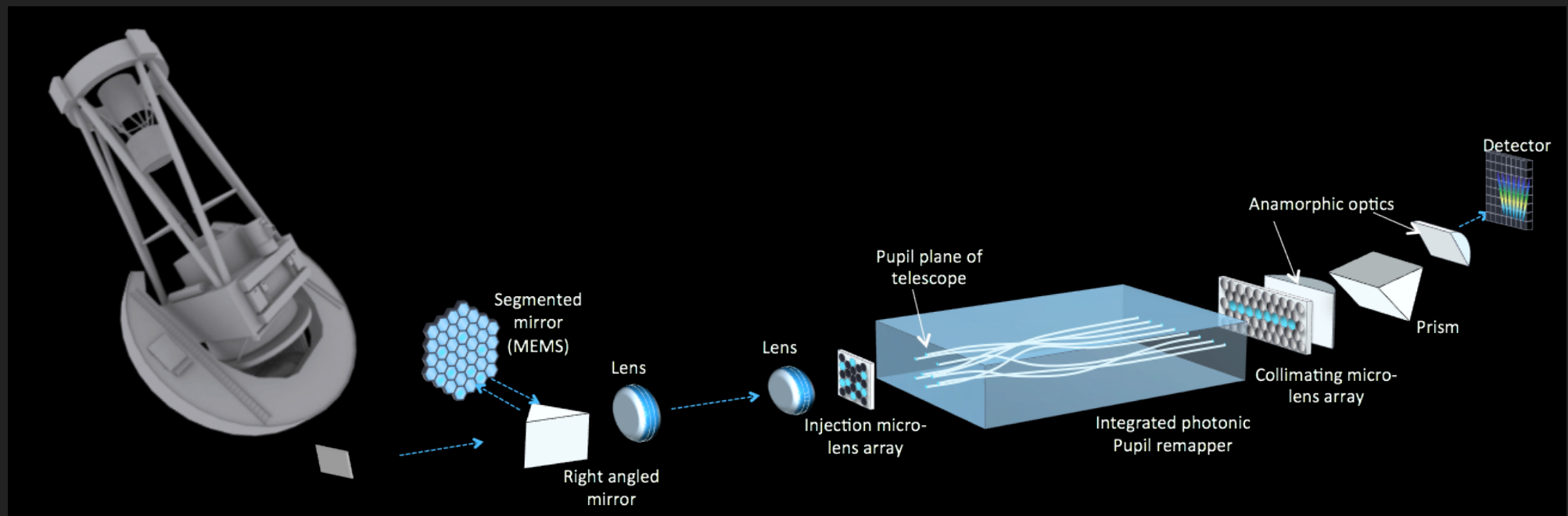
Previous test at AAT



Previous test at AAT



Glint @ subaru

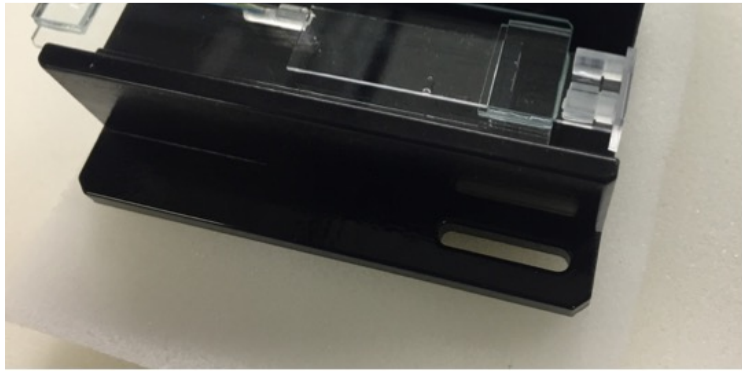


Photonic pupil remapper (NIR) - Remaps arbitrary 2D pattern into 1D

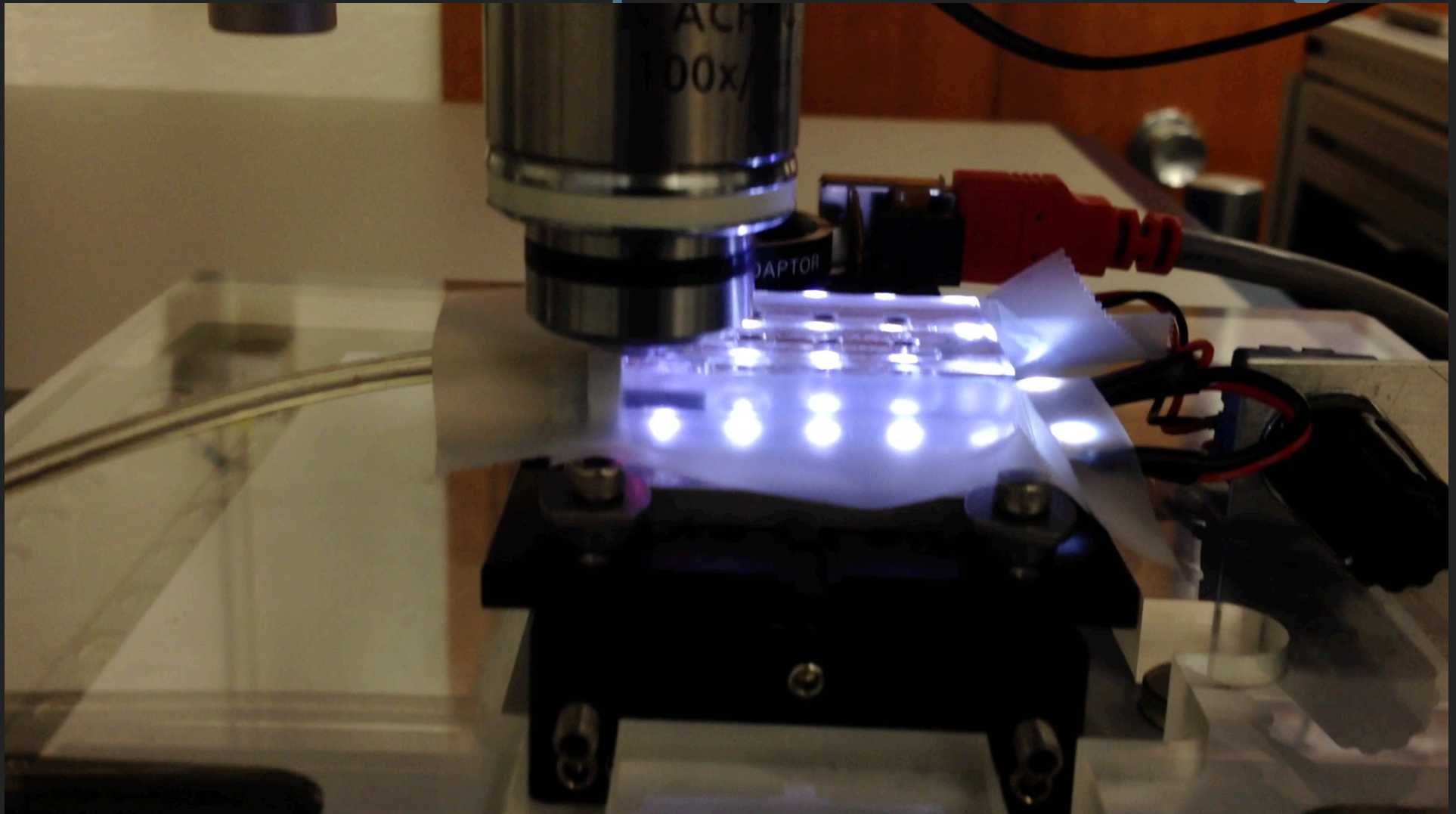
- Redundant (full pupil coverage) $\rightarrow$ non-redundant
- 1D $\rightarrow$ can be spectrally dispersed
- Single-mode waveguides $\rightarrow$ flat phase across sub-aperture



Glint @ subaru

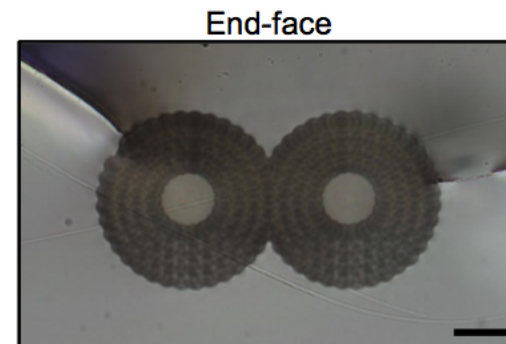
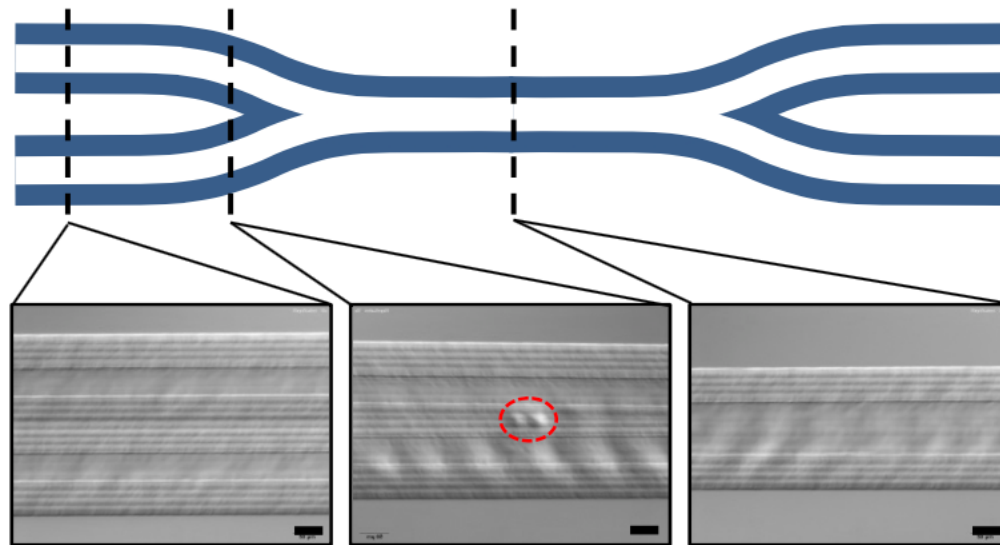


Photonic chip manufacturing



Next Steps...

- Efficient operation at 3-5 microns (Harry Kenchington Goldsmith @ ANU: 2D, A. Arriola @ Macquarie Uni: 3D). *See Harry's work at SPIE.*
- On-chip modulation.
- Second generation ELT instrument concept? Developments even more relevant for long-baseline interferometry (e.g. Planet Formation Imager).



4 micron 3D coupler in ZBLAN
(Gross et al. 2016)